CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International Advanced Subsidiary and Advanced Level

MARK SCHEME for the March 2016 series

9709 MATHEMATICS

9709/12

Paper 1 (Pure Mathematics), maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally
 independent unless the scheme specifically says otherwise; and similarly when there are
 several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a
 particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme.
 When two or more steps are run together by the candidate, the earlier marks are implied and
 full credit is given.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

- AEF Any Equivalent Form (of answer is equally acceptable)
 AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
 BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- CWO Correct Working Only often written by a 'fortuitous' answer
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)
- SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR-1 A penalty of MR-1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through ↓^h" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA-1 This is deducted from A or B marks in the case of premature approximation. The PA-1 penalty is usually discussed at the meeting.

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Mark Scheme

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Paper

Syllabus

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1	(i)	$80(x^4), -32(x^5)$	B1B1	2]	Fully simplified				
(ii)	$(-32+80p)(x^5) = 0$ p = 2/5 or $32/80$ oe	M1 A1√ [≜]	2]	Attempt to mult. relevant terms & put $= 0$				
2		$y = \frac{3x^3}{3} - \frac{2x^{-2}}{-2} (+c)$ 3 = -1 + 1 + c $y = x^3 + x^{-2} + 3$	B1B1 M1 A1	4]	Sub $x = -1, y = 3$. <i>c</i> must be present Accept $c = 3$ www				
3		a+11d = 17 $\frac{31}{2}(2a+30d) = 1023$ Solve simultaneous equations $d = 4, \ a = -27$ 31st term = 93	B1 B1 M1 A1 A1 [1	5]	At least one correct				
4 ((a)	$3x = -\sqrt{3} / 2$ $x = \frac{-\sqrt{3}}{6} \text{oe}$	M1 A1	2]	Accept -0.866 at this stage Or $\frac{-3}{6\sqrt{3}}$ or $\frac{-1}{2\sqrt{3}}$				
((b)	$(2\cos\theta - 1)(\sin\theta - 1) = 0$ $\cos\theta = 1/2 \text{ or } \sin\theta = 1$ $\theta = \pi/3 \text{ or } \pi/2$	M1 A1 A1A1 [4	4]	Reasonable attempt to factorise and solve Award B1B1 www Allow 1.05, 1.57. SCA1for both 60°, 90°				
5	(i)	Mid-point of $AB = (7, 3)$ soi Grad. of $AB = -2 \rightarrow \text{grad}$ of perp. bisector = $1/2$ soi Eqn of perp. bisector is $y - 3 = \frac{1}{2}(x - 7)$	B1 M1 A1	3]	Use of $m_1 m_2 = -1$				
(ii)	Eqn of CX is $y - 2 = -2(x - 1)$ $\frac{1}{2}x - \frac{1}{2} = -2x + 4$ x = 9/5, y = 2/5 $BX^2 = 7.2^2 + 1.4^2$ soi BX = 7.33	M1 DM1 A1 M1 A1 [1	5]	Using their original gradient and (1,2) Solve simultaneously dependent on both previous M's				

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	Page 5 Mark Scheme					Syllabus	Paper
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			r		1		
6	(i)	$A = 2\pi r^2 + 2\pi rh$	B1				
v	(1)		D 1				
		$\pi r^2 h = 1000 \rightarrow h = \frac{1000}{\pi r^2}$	M1				
		Sub for h into $A \rightarrow A = 2\pi r^2 + \frac{2000}{\pi}$ AG	A1				
		ľ		[3]			
(ii)	$\frac{dA}{dr} = 0 \implies 4\pi r - \frac{2000}{r^2} = 0$	M1A1	1	Attempt diff	ferentiation &	r set = 0
,	, II)	dr r^2 r^2			fferentiation & set $= 0$		
		r = 5.4	DM1	A1	Reasonable	attempt to so	lve to $r^3 =$
		$\frac{d^2 A}{dr^2} = 4\pi + \frac{4000}{r^3}$					
		$\frac{1}{dr^2} = 4\pi + \frac{1}{r^3}$					
		>0 hence MIN hence MOST EFFICIENT AG	B 1		Or convinci	ng alternative	e method
			21	[5]			, incuro a
				r - 1			
7	(i)	$CP = {}^{3}CA$ sol	М				
7	(i)	$CP = \frac{3}{5}CA$ soi	M1				
		3 $(1, 2)$					
		$CP = \frac{3}{5}(4\mathbf{i} - 3\mathbf{k}) = 2.4\mathbf{i} - 1.8\mathbf{k} \text{ AG}$	A1	[4]			
		5		[2]			
(ĩi)	$OP = 2.4\mathbf{i} + 1.2\mathbf{k}$	B1]		
,	<u>, II)</u>	BP = 2.4i - 2.4j + 1.2k	B1				
		DI = 2.71 = 2.73 + 1.2K	DI	[2]			
(i	ii)	BP.CP = 5.76 - 2.16 = 3.6	M1		Use of $x_1 x_2$	$+ y_1 y_2 + z_1 z_2$	
		$BP \mid CP \mid = \sqrt{2.4^2 + 2.4^2 + 1.2^2} \sqrt{2.4^2 + 1.8^2}$	M1		Product of n	noduli	
					1100000011		
		$\cos BPC = \frac{3.6}{\sqrt{12.96}\sqrt{9}} \left(=\frac{1}{3}\right)$	M1		All linked c	orrectly	
			A 1				
		Angle $BPC = 70.5^{\circ}$ (or 1.23 rads) cao	A1	[4]			
				[4]			
8	(i)	2a + 4b = 8	M1		Substitute ir	n-2 and -3	
	. /	$2a^2 + 3a + 4b = 14$	A1				
		$2a^{2} + 3a + (8 - 2a) = 14 \rightarrow (a + 2)(2a - 3) = 0$			Cult line	ato and all all	Prottorent
		2u = 5u + (0 - 2u) - 1 + - (u + 2)(2u - 5) - 0	M1		Sub linear in solution	nto quadratic	& allempt
		a = -2 or $3/2$	A 1			and allow CC	Al for aithor
		a = -2 or $5/2b = 3$ or $5/4$	A1 A1				A1 for either
			лі	[5]	(-2,3) or (3)	5/2, 3/4)	
				[~]			
	·••	$(1)^2$ 13			A 11	1 .	1
((ii)	$y = \left(x - \frac{1}{2}\right)^2 - \frac{13}{4}$ Attempt completing of square	M1A1	l	Allow with	<i>x/y</i> transpose	d
		$x - \frac{1}{2} = (\pm)\sqrt{y + \frac{13}{4}}$ oe	DM1		Allow with	<i>x/y</i> transpose	d
		$2^{-(-)}\sqrt{\frac{3}{2}}$ 4					
		$r^{-1}(.)$ 1 13	A1		Allow $v =$	Must be a	function of <i>x</i>
		$f^{-1}(x) = \frac{1}{2} - \sqrt{x + \frac{13}{4}}$ oe					
		2	B1√^		Allow >, -	$13/4 \leq x \leq 0$	$\circ, \left -\frac{13}{4}, \infty \right $ etc
		Domain of f^{-1} is $(x) \ge -13/4$		[5]	,		

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9	(a) (i)	$BAO = OBA = \frac{\pi}{2} - \alpha$		Allow use of	f 90° or 180°	
		$AOB = \pi - \left(\frac{\pi}{2} - \alpha\right) - \left(\frac{\pi}{2} - \alpha\right) = 2\alpha AG$	M1A1 [2]	Or other val	id reasoning	
	(ii)	$\frac{1}{2}r^2(2\alpha) - \frac{1}{2}r^2\sin 2\alpha \text{oe}$	B2,1,0 [2]	SCB1 for re	versed subtra	ction
	(b)	Use of $\alpha = \frac{\pi}{6}$, $r = 4$	B1B1			
		1 segment $S = \left(\frac{1}{2}\right) 4^2 \left(\frac{\pi}{3}\right) - \left(\frac{1}{2}\right) 4^2 \sin \frac{\pi}{3}$				
		$=\left(\frac{8\pi}{3}-4\sqrt{3}\right)$	M1	Ft their (ii),		
		Area <i>ABC</i> $T = \left(\frac{1}{2}\right) 4^2 \sin \frac{\pi}{3} \left(=4\sqrt{3}\right)$	B1	OR $AXB = \frac{T}{3}$		
		$T-3S = \left(\frac{1}{2}\right)4^2\sin\frac{\pi}{3} - 3$			$\frac{2\pi}{3}\left(=\frac{4\sqrt{3}}{3}\right)$	
		$\left[\left(\frac{1}{2}\right)4^2\left(\frac{\pi}{3}\right)-\left(\frac{1}{2}\right)4^2\sin\frac{\pi}{3}\right]$	M1	OR $3\left[\frac{T}{3}-S\right]$	$\begin{bmatrix} 3 \end{bmatrix} = 3 \begin{bmatrix} \frac{4\sqrt{3}}{3} \end{bmatrix} -$	$\left(\frac{8\pi}{3}-4\sqrt{3}\right)\right]$
		$16\sqrt{3}-8\pi$ cao	A1 [6]			
10	(i)	x = 1/3	B1 [1]			
	(ii)	$\frac{\mathrm{d}y}{\mathrm{d}x} = \left[\frac{2}{16}(3x-1)\right] [3]$	B1B1			
		When $x = 3 \frac{dy}{dx} = 3$ soi	M1			
		Equation of QR is $y-4=3(x-3)$ When $y=0$ $x=5/3$	M1 A1			
		when y = 0 x = 57.5	[5]			
	(iii)	Area under curve = $\left[\frac{1}{16 \times 3}(3x-1)^3\right] \left[\times \frac{1}{3}\right]$	B1B1			
		$\frac{1}{16\times9} \left[8^3 - 0 \right] = \frac{32}{9}$	M1A1	Apply limits	s: their $\frac{1}{3}$ and	13
		Area of $\Delta = 8/3$	B1			
		Shaded area $=\frac{32}{9} - \frac{8}{3} = \frac{8}{9}$ (or 0.889)	A1 [6]			
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