

<p>1 (i)</p>	$11^{-2} = \frac{1}{121}$	<p>B1 1</p>	$\frac{1}{121}$ ($\frac{1}{11^2} = B0$)
<p>(ii)</p>	$100^{\frac{3}{2}} = 1000$	<p>M1 A1 2</p>	<p>Square rooting or cubing soi 1000</p>
<p>(iii)</p>	$\sqrt{50} + \frac{6}{\sqrt{3}}$ $= 5\sqrt{2} + \frac{6\sqrt{3}}{3}$ $= 5\sqrt{2} + 2\sqrt{3}$	<p>B1</p> <p>M1</p> <p>A1 3</p> <p><u>6</u></p>	<p>$5\sqrt{2}$ (allow \pm)</p> <p>Attempt to rationalise $\frac{6}{\sqrt{3}}$ cao</p>
<p>2</p>	<p>$q=2$</p> <p>$r=3$</p> <p>$p=28$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1 $\sqrt{\quad}$ 4</p> <p><u>4</u></p>	<p>(allow embedded values)</p> <p>$qr^2 + 10 = p$ or other correct method</p>
<p>3(i)</p>	<p>$y = 5\sqrt{2x}$</p>	<p>M1</p> <p>A1 2</p>	<p>$\sqrt{2x}$ or $\sqrt{\frac{x}{2}}$ seen</p> <p>$y = 5\sqrt{2x}$</p>
<p>(ii)</p>	<p>Translation $\begin{pmatrix} 0 \\ -3 \end{pmatrix}$</p>	<p>B1</p> <p>B1 2</p> <p><u>4</u></p>	<p>Translation</p> <p>$\begin{pmatrix} 0 \\ -3 \end{pmatrix}$ o.e.</p>

<p>4</p>	<p>Either $y = 2x + 1$ or $y = \frac{x^2 + 11}{3}$ $x^2 - 6x + 8 = 0$ $(x - 2)(x - 4) = 0$ $x = 2 \quad x = 4$ $y = 5 \quad y = 9$</p> <p>OR $x = \frac{y - 1}{2}$ $\frac{(y - 1)^2}{4} - 3y + 11 = 0$ $y^2 - 14y + 45 = 0$ $(y - 5)(y - 9) = 0$ $y = 5 \quad y = 9$ $x = 2 \quad x = 4$</p>	<p>M1 A1 M1 A1 A1</p> <p><u>SR</u></p> <p>If solution by graphical methods: setting out to draw a parabola <u>and</u> a line M1 both correct A1 reading off of coordinates at intersection point(s) M1 one correct pair A1 second correct pair A1</p> <p>OR No working shown: one correct pair B1 second correct pair B1 full justification that these are the only solutions B3</p> <p><u>5</u></p>	<p>Substitute for x/y or attempt to get an equation in 1 variable only</p> <p>Obtain correct 3 term quadratic</p> <p>Correct method to solve 3 term quadratic</p> <p><u>or</u> one correct pair of values B1</p> <p>second correct pair of values B1 c.a.o</p>
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4721

Mark Scheme

January 2005

5			B1	Correct curve in +ve quadrant
			B1 2	in -ve quadrant
(i)			M1	Positive cubic with clearly seen max and min points
			A1	(-1,0) (0,0) (1,0) Any one point stated or marked on sketch
(ii)	(-1,0) (0,0) (1,0)		A1 3	Curve passes through all 3 points and no extras stated or marked on sketch
			B1	Graph <u>only</u> in bottom right hand quadrant
(iii)			B1 2	Correct graph, passing through origin
			<u>I</u>	

6 (i)	$49 - 4 \times -2 \times 3 = 73$		M1	Uses $b^2 - 4ac$
			A1	73
(ii)	2 real roots		B1 $\sqrt{3}$	2 real roots (ft from their value)
			M1	Attempts $b^2 - 4ac = 0$ (involving p) or attempts to complete square (involving p)
	or $2[(x + \frac{p+1}{4})^2 - \frac{(p+1)^2}{16} + 4] = 0$		A1	$(p+1)^2 - 64 = 0$ aef
			B1	$p = -9, 7$
	$p = -9, 7$		B1 4	$p = -9$ $p = 7$
			<u>I</u>	

<p>7 (i)</p> $\frac{dy}{dx} = 2x^3 - 3$ <p>(ii)</p> $y = 2x^3 + 2x^2 + 3x + 3$ $\frac{dy}{dx} = 6x^2 + 4x + 3$ <p>(iii)</p> $y = x^{\frac{1}{5}}$ $\frac{dy}{dx} = \frac{1}{5}x^{-\frac{4}{5}}$	<p>B1</p> <p>B1 2</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A1 4</p> <p>B1</p> <p>B1</p> <p>B1 3</p> <p><u>9</u></p>	<p>1 term correct</p> <p>Completely correct (+c is an error, but only penalise once)</p> <p>Attempt to expand brackets</p> $2x^3 + 2x^2 + 3x + 3$ <p>2 terms correct</p> <p>Completely correct</p> <p><u>SR</u> Recognisable attempt at product rule M1 one part correct A1 second part correct A1 final simplified answer A1</p> <p>$x^{\frac{1}{5}}$ soi</p> <p>$\frac{1}{5}x^c$</p> <p>$kx^{-\frac{4}{5}}$</p>
<p>8(i)</p> $2[10 + x + x] > 64$ <p>(ii)</p> $x(x+10) < 299$ $x^2 + 10x - 299 < 0$ $(x-13)(x+23) < 0$ <p>(iii)</p> $x > 11$ $(x-13)(x+23) < 0$ $-23 < x < 13$ $\therefore 11 < x < 13$	<p>B1 1</p> <p>B1</p> <p>B1 2</p> <p>B1 $\sqrt{\quad}$</p> <p>M2</p> <p>A1</p> <p>B1 5</p> <p><u>8</u></p>	<p>$20 + 4x > 64$ o.e.</p> <p>$x(x+10) < 299$</p> <p>Correctly shows $(x-13)(x+23) < 0$ AG</p> <p><u>SR</u> <u>Complete</u> proof worked backward B2</p> <p>$x > 11$ ft from their (i) Correct method to solve $(x-13)(x+23) < 0$ eg graph</p> <p>$-23 < x < 13$ seen in this form or as number line</p> <p><u>SR</u> if seen with no working B1</p>

9(i)	$\frac{dy}{dx} = 4x$	B1	4x
	At $x=3$, $\frac{dy}{dx} = 12$	B1 2	12
(ii)	Gradient of tangent = - 8 $4x = -8$ $x = -2$ $y = 8$	M1 A1 A1 3	$\frac{dy}{dx} = -8$ $x = -2$ $y = 8$
(iii)	Gradient = 6	B1 1	Gradient = or approaches 6
(iv)	$\frac{dy}{dx} = 2kx$ $x = 1$ $\frac{dy}{dx} = 2k$ $k = 3$	M1 M1 A1 $\sqrt{3}$	$\frac{dy}{dx} = 2kx$ $\frac{dy}{dx} = 2k$ $k = 3$ CWO
		<u>9</u>	

10(i)	Gradient DE = $-\frac{1}{2}$	B1 1	$-\frac{1}{2}$ (any working seen must be correct)
(ii)	$y-3 = -\frac{1}{2}(x-2)$ $x+2y-8=0$	M1 A1 A1 3	Correct equation for straight line, any gradient, passing through F $y-3 = -\frac{1}{2}(x-2)$ aef $x+2y-8=0$ (this form but can have fractional coefficients e.g. $\frac{1}{2}x + y - 4 = 0$
(iii)	Gradient EF = $\frac{4}{2} = 2$ $-\frac{1}{2} \times 2 = -1$	B1 B1 2	Correct supporting working must be seen Attempt to show that product of their gradients = - 1 o.e.
(iv)	DF = $\sqrt{4^2 + 3^2} = 5$	M1 A1 2	$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ used 5
(v)	DF is a diameter as angle DEF is a right angle. Mid-point of DF <u>or</u> centre of circle is $(0, 1\frac{1}{2})$ Radius = 2.5 $x^2 + (y - (\frac{3}{2}))^2 = (\frac{5}{2})^2$ $x^2 + y^2 - 3y + \frac{9}{4} = \frac{25}{4}$ $x^2 + y^2 - 3y - 4 = 0$	B1 B1 B1 B1 $\sqrt{\quad}$ B1 5	Justification that DF is a diameter Mid-point of DF <u>or</u> centre of circle is $(0, 1\frac{1}{2})$ Radius = 2.5 $x^2 + (y - (\frac{3}{2}))^2 = (\frac{5}{2})^2$ $x^2 + y^2 - 3y - 4 = 0$ obtained correctly with at least one line of intermediate working. <u>SR</u> For working that only shows $x^2 + y^2 - 3y - 4 = 0$ is equation for a circle with centre $(0, 1\frac{1}{2})$ B1 radius 2.5 B1
		<u>13</u>	

4721

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