



Q U A L I F I C A T I O N S A L L I A N C E

General Certificate of Education

Statistics 6380

SS03 Statistics 3

Mark Scheme

2006 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Key To Mark Scheme And Abbreviations Used In Marking

М	mark is for method				
m or dM	mark is dependent on one or more M marks and is for method				
А	mark is dependent on M or m marks and is for accuracy				
В	mark is independent of M or m marks and is for method and accuracy				
E	mark is for explanation				
\sqrt{or} ft or F	follow through from previous		_		
	incorrect result	MC	mis-copy		
CAO	correct answer only	MR	mis-read		
CSO	correct solution only	RA	required accuracy		
AWFW	anything which falls within	FW	further work		
AWRT	anything which rounds to	ISW	ignore subsequent work		
ACF	any correct form	FIW	from incorrect work		
AG	answer given	BOD	given benefit of doubt		
SC	special case	WR	work replaced by candidate		
OE	or equivalent	FB	formulae book		
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme		
–x EE	deduct <i>x</i> marks for each error	G	graph		
NMS	no method shown	с	candidate		
PI	possibly implied	sf	significant figure(s)		
SCA	substantially correct approach	dp	decimal place(s)		

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

SS03

Q	Solution	Marks	Total	Comments
1(a)	Ranks			
	Rank x Rank y 10 (1)10 (1)5 (6)9 (2)1 (10)8 (3)8 (3)7 (4)7 (4)6 (5)6 (5)5 (6)3 (8)4 (7)4 (7)3 (8)9 (2)2 (9)2 (9)1 (10)	M1 M1		Ranks effort made for <i>x</i> Ranks effort made for <i>y</i> (consistent)
	<i>r</i> _s = 0.273 (3 sig figs)	Β3	5	Alternative d = 0,4,7,1,1,1,1,7,1 $\sum d^2 = 120$ $r_s = 1 - \frac{6 \times 120}{10 \times 99} = 0.273$ M1 M1 A1 0.272 or 0.274 M1 M1 A0 sc $r = 0.27$, no method 3/5
(b)	H ₀ : ranks are independent in population H ₁ : ranks are not independent – an association does exist between x and y 2 tail 10 % sig level test stat $r_s = 0.273$ cv = 0.5636 since $ ts < 0.5636$ Accept H ₀ . No significant evidence at 10% level to suggest an association between municipal waste and CO ₂ emissions per capita – ranks are	B1 B1 M1 A1		Allow $\rho_s = 0$ $\rho_s \neq 0$ For cv For comparison ts/cv Allow small slip in r_s
	independent in the population.	E1	5	In context
	Total		10	

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ocation ne B1		
etc		
0 +		
.64 M1		<i>E</i> method for 4 correct, can be integers
.36 m1		All <i>E</i> correct, 1 dp, not integers
ml		sc Pool max 4 M1 m0 m1 A0 5.991 B0
		B1 M1 A0 sc Yates max 4 M1 m1 m0 A0 B1 B1 m0 A0
A1		Test stat 11.3 – 11.5 Allow M1 m1 m1 A1 if no method
B1 B1		For $v = 3$ For cv
ct H _o endent M1 A1	9	
ch more E1		If test muddled and used common sense
K and ly to E1	2	E1,0 If test ok, but wrong conclusion E1,0 c on (a)
ime E1		For 'staying the same'
E1		For 'staying the same'
ed B1		For saying there will be a change/increa
values E1		For identification of new ts doubling
e new $E2$	6	For 'staying the same' conclusion
e critical		For explanation in context Bigger test stat., cv same and explained context E2
	e new E2√	e new $E2\sqrt{6}$

4

Q	Solution	Marks	Total	Comments
3(a)	H ₀ : pop median, $\eta = \pounds 148.50$	B1		Correct pop median used
	$H \cdot non motion n > f148.50$	B1		Or pop average/pop mean Correct tail/direction
	H ₁ : pop median, $\eta > \pounds 148.50$	DI		
	1 tail 5%			
		M1		For differences X - £148.50
	diff £ 8.95 -1.85 3.80 3.10 8.60 rank 8 -2 6 3½ 7	M1		For ties, however ranked
		m1		For ranks, rank $1 =$ smallest
	3.65 -3.10 -0.90 16.25 10.10 5 -3 ¹ / ₂ -1 10 9			
	T = 2 + 6 + + 0 = 401/	1 ^		
	$T_{+} = 8 + 6 + \dots + 9 = 48\frac{1}{2}$ $T_{-} = 2 + 3\frac{1}{2} + 1 = 6\frac{1}{2}$	m1√		For totals
	Test stat $T = 6^{1/2}$	A1		For one correct total
	cv = 11 T < 11	B1 M1√		For cv Comparison cv/ts; ft however ranked
	Significant evidence at 5% level to reject	A1	10	Comparison evits, it nowever ranked
	H ₀			
(h)	There is significant avidence to suggest	E1	1	In context (might be in (a))
(b)	There is significant evidence to suggest that the median weekly wage for full-time	EI	1	In context (might be in (a))
	workers in company cafeterias has			
	increased from £148.50			
(c)(i)	Wilcoxon signed-test is preferred because	B1	1	Not 'more accurate'
	the magnitudes of the differences are		-	More powerful
	taken into account whereas, with the sign			More likely to detect a difference if one
	test, only the signs of the differences are used.			exists
	uscu.			
(ii)	Data not symmetrically distributed	B1 E1	2	Correct reasoning and explained well
	therefore Wilcoxon signed-rank cannot be			
	carried out Data given only as signs/preferences so			
	only sign test possible			
	T-4-1		14	
	Total		14	

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Q	Solution	Marks	Total	Comments
4(a)	H ₀ : Samples from identical populations	B1		Or H ₀ : $\eta_A = \eta_B = \eta_C = \eta_D$
	H ₁ : Samples not from identical populations 1% sig level	B1		H ₁ : at least two of $\eta_A, \eta_B, \eta_C, \eta_D$ do differ Or pop average B1 B0 Or H ₀ : no difference in pop medians H ₁ : one pop median does differ B1 B1 H ₀ : $\mu_A = \mu_B = \dots$ B1 B0
	Totals of ranks $T_A = 29$ $T_B = 55$ $T_C = 92$ $T_D = 77$ $n_A = 6$ $n_B = 6$ $n_C = 5$ $n_D = 5$	M1		Totals of ranks in each depth
	$\sum_{i=1}^{m} \frac{T_i^2}{n_i} = \frac{29^2}{6} + \frac{55^2}{6} + \frac{92^2}{5} + \frac{77^2}{5}$ $= 3522.933$	m1 m1		Correct numerators ft Correct denominators
	$H = \frac{12}{22 \times 23} \times 3522.933 - (3 \times 23)$	m1		
	= 14.5	A1		<i>H</i> 14.4 – 14.6
	Critical value from $\chi_3^2 = 11.345$ H > 11.345 Sig evidence to reject H ₀ and conclude that samples are not from identical populations	B1 m1 A1		Dep on M1 m1 m1
	There is significant evidence that at least two of the average alfalfa yields (from	E1		Difference in context
	methods A, B, C or D) do differ.	E1	12	Mention of 'at least two'
(b)	It would appear that the average yield for method C is significantly higher (as there	B1		Identification of method C with some reason
	is significant evidence of a difference detected in part (a) and C has the highest ranked yields) and this would be the	E1		Significant evidence to suggest that the average yield for C is certainly greater than the average yield for method A
	recommended method for greatest alfalfa yield.	E1	3	With reference to average ranks and clearly understood. Need at least 2 different, or refer to conclusion in (a)
	Total		15	

Q	Solution	Marks	Total	Comments
5(a)	H ₀ : pop median difference $\eta_d = 0$	B1		Not difference
	H ₁ : pop median difference $\eta_d \neq 0$			Not μ /average
	2 tail 10%			
	Signs: + + + + + + +	M1		Signs or WSR signed differences
	n = 9			
	test stat = $7^+/2^-$	A1		Test stat correct
	Model B(9. 0.5)	M1		Bin model seen to be used with $n = 9$
	0.0898 > 0.05 or $0.1796 > 0.10$	M1		Comparison of correct
	seen			B(9, 0.5) prob with 0.05 or 0.10
				Or use of identified $cr\{0,1\}$ or $\{8,9\}$ with
				prob 0.195
	Accept H ₀			
	No significant evidence at 10% level to doubt H_0	A1	6	
				sc Wilcoxon 4/6 max
				M1 for diffs and signs:
				4, 6, 5, 23, -5, -5, 19, 24, 20
				(ranks 1, 5, 3, 8, -3, -3, 6, 9, 7)
				A1 total correct 6 or 39
				M1 comparing total with cv: $cv = 8$, $T = 6$
				sc one-tail max 4/6
				$H_0 \eta = 0$
				$\begin{array}{c} H_0 & \eta = 0 \\ H_1 & \eta > 0 \end{array}$
				$H_1 \eta > 0$ B1 M1 A1 M1 M0 A0
(b)	There is no significant evidence to suggest			
	that either aerosol A or B is preferable as			
	there is no significant difference in	E1√	1	Explanation in context
ļ	average effectiveness			
	Total		7	

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6	H ₀ : Samples are taken from identical	B1		Hypotheses referring to population
	populations			averages also acceptable
	H ₁ : Samples are not taken from identical	B1		Refer to μ : B1 B0
	populations (population average weight			
	differs)			
	2 tail 5%			
	Ranks	M1		For ranks as one group
	E Side 14 18 7 ¹ / ₂ 17 9 5 16 7 ¹ / ₂ 15	M1		At least 12 correct. (Ties not necessary
	W Side 2 4 10 12 1 3 11 13 6	A1		7,8 OK)
				Other alternative methods acceptable
	$T_{\rm E} = 14 + 18 + \dots + 15 = 109$	m1		For totals of ranks in each group
	$T_{\rm W} = 2 + 5 + \dots + 6 = 62$			
	$U_{\rm E} = 109 - \frac{9 \times 10}{2} = 64$	m1		For Unternated
	2	1111		For U attempted
	$U_{\rm W} = 62 - \frac{9 \times 10}{2} = 17$			
	Test stat $U = 17$	A1		For U correct – either
				Method not seen, award full marks
	cv = 18	B1		For consistent cv with U
				cv = 63 acceptable
	U = 17 < 18	M1		For comparison <i>U</i> /cv
	Reject H ₀	A1		-
	Significant evidence at the 5% level to			
	suggest that the population average			
	weight for plants from the East Side	E1	12	In context
	differs from the population average			
	weight for plants from the West Side			
	Total		12	
	TOTAL		75	