CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International Advanced Level

MARK SCHEME for the October/November 2014 series

9709 MATHEMATICS

9709/31

Paper 3, maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √^{*} implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

- AEF Any Equivalent Form (of answer is equally acceptable)
- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- CWO Correct Working Only often written by a 'fortuitous' answer
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)
- SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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Obta Obta (i) (ii) Subs	Camblaw of the loin a correctin answer xState or impUse correctObtain answMake recogJustify a state	ridge International A Level – October/November 2014ogarithm of a powerlinear equation in any form, e.g. $x = (x - 2) \ln 3$ = 22.281oly ordinates 2, 1.1547, 1, 1.1547formula, or equivalent, with $h = \frac{1}{6}\pi$ and four ordinates	yllabus 9709	Pap 31 M1 A1 B1 M1 A1	[3]
Obta Obta (i) (ii) Subs	law of the lo in a correct in answer x State or imp Use correct Obtain answ Make recog Justify a sta	begarithm of a power linear equation in any form, e.g. $x = (x - 2) \ln 3$ = 22.281 bly ordinates 2, 1.1547, 1, 1.1547 formula, or equivalent, with $h = \frac{1}{6}\pi$ and four ordinates wer 1.95 nisable sketch of $y = \operatorname{cosec} x$ for the given interval	9709	M1 A1 A1 B1 M1 A1 B1	[3]
Obta Obta (i) (ii) Subs	in a correct in answer x State or imp Use correct Obtain answ Make recog Justify a sta	linear equation in any form, e.g. $x = (x - 2) \ln 3$ = 22.281 bly ordinates 2, 1.1547, 1, 1.1547 formula, or equivalent, with $h = \frac{1}{6}\pi$ and four ordinates ver 1.95 nisable sketch of $y = \operatorname{cosec} x$ for the given interval		A1 A1 B1 M1 A1 B1	[3] [3]
(ii) Subs	Use correct Obtain answ Make recog Justify a sta	formula, or equivalent, with $h = \frac{1}{6}\pi$ and four ordinates ver 1.95 nisable sketch of $y = \operatorname{cosec} x$ for the given interval		M1 A1 B1	[3]
Subs	Make recog Justify a sta	nisable sketch of $y = \operatorname{cosec} x$ for the given interval		B1	[3]
Subs	Justify a sta				
	stituto x			DI	[2]
	since $x = -$	$\frac{1}{3}$, equate result to zero or divide by $3x + 1$ and equate the remainder	to zero		
and	obtain a corr	vect equation, e.g. $-\frac{1}{27}a + \frac{1}{9}b - \frac{1}{3} + 3 = 0$		B1	
Subs Obta Solv	stitute $x = 2$ a and a correct e for <i>a</i> or for	and equate result to 21 or divide by $x - 2$ and equate constant remaind equation, e.g. $8a + 4b + 5 = 21$ r b	ler to 21	M1 A1 M1 A1	[5]
(i)	Use chain ru Obtain eithe	the correctly at least once $er \frac{dx}{dt} = \frac{3\sin t}{\cos^4 t} \text{ or } \frac{dy}{dt} = 3\tan^2 t \sec^2 t \text{ , or equivalent}$		M1 A1	
				M1	
				A1	[4]
(ii)	Use Pythage	Dras		B1 M1 A1	[3]
(i)	Substitute z	$= 1 + i$ and obtain $w = \frac{1+2i}{1+i}$		B1	
	EITHER:	or equivalent Simplify numerator to 3 + i or denominator to 2	inator,	M1 A1	
	OR:	Obtain two equations in x and y, and solve for x or for y 3 1 1 1 1 1 1 1 1 1 1		M1	
		Obtain $x = \frac{3}{2}$ or $y = \frac{1}{2}$, or equivalent		A1	
		Obtain final answer $\frac{3}{2} + \frac{1}{2}i$, or equivalent		A1	[4]
	Subs Obta Solv Obta (i) (ii)	Substitute $x = 2$ a Obtain a correct Solve for <i>a</i> or for Obtain $a = 12$ an (i) Use chain ru Obtain eithe $Use \frac{dy}{dx} = \frac{dy}{dt}$ Obtain the g (ii) State a correct Use Pythage Obtain the g (i) Substitute <i>z</i> <i>EITHER</i> :	Substitute $x = 2$ and equate result to 21 or divide by $x - 2$ and equate constant remained Obtain a correct equation, e.g. $8a + 4b + 5 = 21$ Solve for a or for b Obtain $a = 12$ and $b = -20$ (i) Use chain rule correctly at least once Obtain either $\frac{dx}{dt} = \frac{3 \sin t}{\cos^4 t}$ or $\frac{dy}{dt} = 3 \tan^2 t \sec^2 t$, or equivalent Use $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$ Obtain the given answer (ii) State a correct equation for the tangent in any form Use Pythagoras Obtain the given answer (i) Substitute $z = 1 + i$ and obtain $w = \frac{1+2i}{1+i}$ <i>EITHER</i> : Multiply numerator and denominator by the conjugate of the denom or equivalent Simplify numerator to $3 + i$ or denominator to 2 Obtain final answer $\frac{3}{2} + \frac{1}{2}i$, or equivalent <i>OR</i> : Obtain two equations in x and y , and solve for x or for y Obtain $x = \frac{3}{2}$ or $y = \frac{1}{2}$, or equivalent	Substitute $x = 2$ and equate result to 21 or divide by $x - 2$ and equate constant remainder to 21 Obtain a correct equation, e.g. $8a + 4b + 5 = 21$ Solve for <i>a</i> or for <i>b</i> Dotain <i>a</i> = 12 and <i>b</i> = -20 (i) Use chain rule correctly at least once Obtain either $\frac{dx}{dt} = \frac{3 \sin t}{\cos^4 t}$ or $\frac{dy}{dt} = 3 \tan^2 t \sec^2 t$, or equivalent $U_{Se} \frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$ Obtain the given answer (ii) State a correct equation for the tangent in any form Use Pythagoras Obtain the given answer (ii) Substitute $z = 1 + i$ and obtain $w = \frac{1+2i}{1+i}$ <i>EITHER</i> : Multiply numerator and denominator by the conjugate of the denominator, or equivalent Simplify numerator to 3 + i or denominator to 2 Obtain final answer $\frac{3}{2} + \frac{1}{2}i$, or equivalent <i>OR</i> : Obtain two equations in <i>x</i> and <i>y</i> , and solve for <i>x</i> or for <i>y</i> Obtain $x = \frac{3}{2}$ or $y = \frac{1}{2}$, or equivalent	Substitute $x = 2$ and equate result to 21 or divide by $x - 2$ and equate constant remainder to 21M1Obtain a correct equation, e.g. $8a + 4b + 5 = 21$ A1Solve for a or for bM1Obtain $a = 12$ and $b = -20$ A1(i) Use chain rule correctly at least onceM1Obtain either $\frac{dx}{dt} = \frac{3sint}{\cos^4 t}$ or $\frac{dy}{dt} = 3tan^2 tsec^2 t$, or equivalentA1Use $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$ M1Obtain the given answerM1(ii) State a correct equation for the tangent in any formB1Use PythagorasM1Obtain the given answerM1(i) Substitute $z = 1 + i$ and obtain $w = \frac{1+2i}{1+i}$ B1EITHER:Multiply numerator and denominator by the conjugate of the denominator, or equivalentSimplify numerator to $3 + i$ or dup, and solve for x or for y A1Obtain $x = \frac{3}{2}$ or $y = \frac{1}{2}$, or equivalentA1

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	(ii)	<i>EITHER</i> : Substitute $w = z$ and obtain a 3-term quadratic equation in z, e.g. $iz^2 + z - i = 0$ Solve a 3-term quadratic for z or substitute $z = x + iy$ and use a method to solve for x and y <i>OR</i> : Substitute $w = x + iy$ and obtain two correct equations in x and real and imaginary parts Solve for x and y $-1 \pm \sqrt{3} i$		B1 M1	
		Obtain a correct solution in any form, e.g. $z = \frac{-1 \pm \sqrt{3} i}{2i}$		A1	
		Obtain final answer $-\frac{\sqrt{3}}{2} + \frac{1}{2}i$		A1	[4]
6	(i)	Integrate and reach $bx \ln 2x - c \int x \cdot \frac{1}{x} dx$, or equivalent		M1*	
		Obtain $x \ln 2x - \int x \cdot \frac{1}{x} dx$, or equivalent		A1	
		Obtain integral $x \ln 2x - x$, or equivalent Substitute limits correctly and equate to 1, having integrated twice Obtain a correct equation in any form, e.g. $a \ln 2a - a + 1 - \ln 2 = 1$ Obtain the given answer	M1(6	A1 dep*) A1 A1	[6]
	(ii)	Use the iterative formula correctly at least once Obtain final answer 1.94 Show sufficient iterations to 4 d.p. to justify 1.94 to 2d.p. or show that there is change in the interval (1.935, 1.945).	s a sign	M1 A1 A1	[3]
7	(i)	Separate variables correctly and attempt to integrate at least one side Obtain term $\ln R$ Obtain $\ln x - 0.57x$ Evaluate a constant or use limits $x = 0.5$, $R = 16.8$, in a solution containing ter $a \ln R$ and $b \ln x$ Obtain correct solution in any form	ms of the fori	B1 B1 B1 m M1 A1	
		Obtain a correct expression for <i>R</i> , e.g. $R = xe^{(3.80 - 0.57x)}$, $R = 44.7xe^{-0.57x}$		711	
		$R = 33.6xe^{(0.285 - 0.57x)}$	01	A1	[6]
	(ii)	Equate $\frac{dR}{dx}$ to zero and solve for x		M1	
		State or imply $x = 0.57^{-1}$, or equivalent, e.g. 1.75 Obtain $R = 28.8$ (allow 28.9)		A1 A1	[3]
8	(i)	Use $\sin(A + B)$ formula to express $\sin 3\theta$ in terms of trig. functions of 2θ and θ Use correct double angle formulae and Pythagoras to express $\sin 3\theta$ in terms of Obtain a correct expression in terms of $\sin\theta$ in any form Obtain the given identity [SR: Give M1 for using correct formulae to express RHS in terms of $\sin\theta$ and then M1A1 for expressing in terms of $\sin\theta$ and $\sin 3\theta$ only, or in terms of $\cos\theta$, $\sin\theta$, $\cos 2\theta$ and $\sin 2\theta$, then A1 for obtaining the given identity.]	of sin $ heta$	M1 M1 A1 A1	[4]

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	(ii)	Substitute t	for x and obtain the given answer	B1	[1]	
	(11)	Substitute	for x and obtain the given answer	DI	[*	
	(iii)	•	a correct method to find a value of x	M1		
				A1 + A1	[4]	
		Solutions	with more than 3 answers can only earn a maximum of $A1 + A1$.]			
			A B C			
9	(i)	State or im	ply the form $\frac{A}{1-x} + \frac{B}{2-x} + \frac{C}{(2-x)^2}$	B1		
			ect method to determine a constant	M1		
			a of A = 2, B = -1, C = 3	A1		
			econd value	A1		
		Obtain a th		A1	[5]	
		[The altern	ative form $\frac{A}{1-x} + \frac{Dx+E}{(2-x)^2}$, where $A = 2, D = 1, E = 1$ is marked			
		B1M1A1A	1A1 as above.]			
	(ii)	Use correct	t method to find the first two terms of the expansion			
			$(2-x)^{-1}, (2-x)^{-2}, (1-\frac{1}{2}x)^{-1}$ or $(1-\frac{1}{2}x)^{-2}$	M1		
			rect unsimplified expansions up to the term in x^2 tial fraction $A1\sqrt{+}A1$	$\wedge + A1$		
		-			1	
		Obtain fina	I answer $\frac{9}{4} + \frac{5}{2}x + \frac{39}{16}x^2$, or equivalent	A1	[5]	
		[Symbolic	binomial coefficients, e.g. $\begin{pmatrix} -1 \\ 1 \end{pmatrix}$ are not sufficient for M1. The \checkmark is on A,B,C	C.]		
			<i>D</i> , <i>E</i> form of partial fractions, give M1 A1 \checkmark A1 \checkmark for the expansions then, [1] for multiplying out fully and A1 for the final answer.]			
			e of an attempt to expand $(x^2 - 8x + 9)(1 - x)^{-1}(2 - x)^{-2}$, give M1A1A1 for			
			ions, M1 for multiplying out fully, and A1 for the final answer.]			
		the expansi	ions, wit for multiplying out fully, and fit for the final answer.]			
10	(i)	EITHER:	Find \overrightarrow{AP} (or \overrightarrow{PA}) for a point P on l with parameter λ ,			
			e.g. $\mathbf{i} - 17\mathbf{j} + 4\mathbf{k} + \lambda(-2\mathbf{i} + \mathbf{j} - 2\mathbf{k})$	B1		
			Calculate scalar product of \overrightarrow{AP} and a direction vector for <i>l</i> and equate to zet	ro M1		
			Solve and obtain $\lambda = 3$	A1		
			Carry out a complete method for finding the length of <i>AP</i> Obtain the given answer 15 correctly	M1 A1		
		001.				
		<i>OR</i> 1:	Calling $(4, -9, 9)$ B, state \overrightarrow{BA} (or \overrightarrow{AB}) in component form, e.g. $-\mathbf{i} + 17\mathbf{j} - 4$	k B1		
			Calculate vector product of BA and a direction vector for l ,	271		
			e.g. $(-\mathbf{i} + 17\mathbf{j} - 4\mathbf{k}) \times (-2\mathbf{i} + \mathbf{j} - 2\mathbf{k})$	M1		
			Obtain correct answer, e.g. $-30\mathbf{i} + 6\mathbf{j} + 33\mathbf{k}$	A1		
			Divide the modulus of the product by that of the direction vector Obtain the given answer correctly	M1 A1		
		OR2:	State \overrightarrow{BA} (or \overrightarrow{AB}) in component form	B1		
		OR2.	Use a scalar product to find the projection of BA (or AB) on l	M1		
			Obtain correct answer in any form, e.g. $\frac{27}{\sqrt{9}}$	A1		
			Use Pythagoras to find the perpendicular	M1		
				1711		

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		Obtain the given answer correctly		A1	
(OR3:	State \overrightarrow{BA} (or \overrightarrow{AB}) in component form		B1	
	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	Use a scalar product to find the cosine of <i>ABP</i>		M1	
		Obtain correct answer in any form, e.g. $\frac{27}{\sqrt{9}.\sqrt{306}}$		A1	
		Use trig. to find the perpendicular		M1	
		Obtain the given answer correctly		A1	
0	OR4:	State \overrightarrow{BA} (or \overrightarrow{AB}) in component form		B1	
		Find a second point C on l and use the cosine rule in triangle ABC to the cosine rule ABC to the cosine rule in triangle ABC to the cosine rule in triangle ABC to the cosine rule			
		cosine of angle A , B , or C , or use a vector product to find the area of A	4BC	M1	
		Obtain correct answer in any form		A1	
		Use trig. or area formula to find the perpendicular		M1	
,	2.0.5	Obtain the given answer correctly \overrightarrow{D} (\overrightarrow{D} (\overrightarrow{D})) \overrightarrow{D} (\overrightarrow{D}) \overrightarrow{D} (\overrightarrow{D}) \overrightarrow{D} (\overrightarrow{D}) \overrightarrow{D}) \overrightarrow{D}) \overrightarrow{D} (\overrightarrow{D}) \overrightarrow{D}) \overrightarrow{D} (\overrightarrow{D}) \overrightarrow{D}) \overrightarrow{D} (\overrightarrow{D}) \overrightarrow{D}) \overrightarrow{D}) \overrightarrow{D} (\overrightarrow{D}) \overrightarrow{D}) \overrightarrow{D}) \overrightarrow{D}) (\overrightarrow{D}) \overrightarrow{D}) (\overrightarrow{D}) \overrightarrow{D}) (\overrightarrow{D})) (\overrightarrow{D}) (\overrightarrow{D}))) (\overrightarrow{D})) (\overrightarrow{D}))) (\overrightarrow{D}))) (\overrightarrow{D}))) (\overrightarrow{D})))) (\overrightarrow{D}))) ((()		A1	
C	OR5:	State correct AP (or PA) for a point P on l with parameter λ in any for	orm	B1	
		Use correct method to express AP^2 (or AP) in terms of λ Obtain a correct expression in any form,		M1	
		e.g. $(1-2\lambda)^2 + (-17+\lambda)^2 + (4-2\lambda)^2$		A1	
		Carry out a method for finding its minimum (using calculus, algebra			
		or Pythagoras)		M1	
		Obtain the given answer correctly		A1	[5]
(ii)) EITHER				
		equate constant terms or equate the coefficient of λ to zero, obtaining	ig an		
		equation in a and b		M1*	
		Obtain a correct equation, e.g. $4a - 9b - 27 + 1 = 0$		A1	
		Obtain a second correct equation, e.g. $-2a + b + 6 = 0$	M1(.	A1	
		Solve for a or for b Obtain $a = 2$ and $b = -2$	MI(C	dep*)	
(OR:	Obtain $a = 2$ and $b = -2$ Substitute coordinates of a point of <i>l</i> and obtain a correct equation,		A1	
C	JK.	e.g. $4a - 9b = 26$		B1	
		<i>EITHER</i> : Find a second point on l and obtain an equation in a and	h	M1*	
		Obtain a correct equation	0	A1	
		<i>OR</i> : Calculate scalar product of a direction vector for <i>l</i> and a v	vector		
		normal to the plane and equate to zero		M1*	
		Obtain a correct equation, e.g. $-2a + b + 6 = 0$		A1	
		Solve for <i>a</i> or for <i>b</i>	M1(0	dep*)	
		Obtain $a = 2$ and $b = -2$		A1	[5]