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Mathematics

MD02

(Specification 6360)

Decision 2

Final

Mark Scheme

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Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
√or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
−x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MD02

1(a) $x = 4$ y = 12 z = 13 B1
(c) G Float = 3 (d) One of their CPs correct height B_1 B_2 and correct durations B_1 B_2 B_3 B_4 B_4 B_5 B_6 B_7 B_8 B_9
Float = 3 One of their CPs correct height B_1 and correct durations B_1 , D_1 , D_2 , D_3 , D_4 , D_4 , D_4 , D_5 , D_6 , D_7 , D_8 ,
B, D, H, J and C, E, I correct A1 and correct durations
11 10 9
Number of workers 6
A starting at 0 and ending at 3 F starting at 6 and ending at 11 G starting at 13 and ending at 14 A1 A1 A1 A1 A1 A1 A1 A1 A1 A1
(e) New earliest J 22 days B1 assuming activities continuous
Minimum extra time 5 days B1 2 assuming activities continuous Total 14

Q Q			Solution			Marks	Total	Comments
Ų			Solution			Marks	Total	Comments
2(a)	Hungarian algorithm used to find minimum total Each new entry gives measure of points not scored					E1		First E1– fairly generous for idea of "minimising" or "points not scored". Second E1 is strict.
	⇒ Hunga maximum	rian al total s	core	ow find	ls		2	200000 21 10 00000
(b)	Replacing	<i>x</i> by 3	5-x					
	8	6	10	0	4			
	2	13	18	6	6			
	12	6	10	2	14			
	13	6	6	8	4	B1		Must see this table
	8	8	16	14	8			
	8	6	10	0	4			
	0	0 11	16	4	4 4	M1		reducing rows; ft one slip from above &
	10	4	8	0	12	1711		allow one further slip
	9	2	2	4	0			anow one further stip
	0	0	8	6	0			
	8	6	8	0	4			
	0	11	14	4	4			
	10	4	6	0	12	A1cso	3	check working is correct since most
	9	2	0	4	0			values in final table are given.
	0	0	6	6	0			$(p = 14 \ q = 9)$
(c)	Lines cove	ering	R_4 , R_5 are	ad C_1 , (C_4	B1		4 correct lines
	8	2	4	0	0	M1		subtracting 4 from each uncovered and
	0	7	10	4	0			adding 4 to each double covered
	10	0	2	0	8			(condone 2 slips)
	13	2	0	8	0			
	4	0	6	10	0	A1	3	all correct
(d)(i)	B1 and D3	3				M1		or one full matching with rings etc
		A4	B1 C2	D3 E	5	A1		one correct matching
		A5	B1 C4	D3 E	2	A1	3	second correct and no others
(**	m . 1 . 1 . 1 . 1 . 1 . 1	2				D.1		
(ii)	Total = 15	3			7D 4 7	B1	1	
					Total		12	

Q	Solution	Marks	Total	Comments
3(a)	For each pair of strategies	E2,1		E1 for general idea of
	Roz gain + Colum gain = 0		2	Roz gain + Colum gain = 0
(b)	Colum's max are -2 , 3, -1 min (colum max) = -2	E1		must see these values for E1
	\Rightarrow play safe is C_1	B1	2	
(c)(i)	Delete R_2 (PI by further work) Since R_3 dominates R_2	M1 A1	2	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
(ii)	Let Roz play R_1 with prob p			
	C_1 expected gain: $-2p - 3(1-p) = p - 3$ $C_2 : -6p + 3(1-p) = 3 - 9p$ $C_3 : -p - 4(1-p) = 3p - 4$	M1 A1		2 expressions unsimplified ft their matrix all correct
	$ \begin{array}{c} 3 \\ 0 \\ -3 \\ -4 \end{array} $	M1 A1		plotting 3 expected gains for $0 \le p \le 1$ correct gains plotted accurately
	Solving $p-3 = 3-9p$ $\Rightarrow 10p = 6$	m1		choosing highest point of 'their' region or correct pair solved
	$p = \frac{3}{5}$	A1		
	\Rightarrow Roz plays R_1 with probability $\frac{3}{5}$ and			
	R_3 with probability $\frac{2}{5}$	E1cao	7	must see R_1 and R_3
	Total		13	

Q	Solution	Marks	Total	Comments
4(a)(i)	x-column	B1		
	pivot = 6	B1		
	$\left\{ \begin{array}{c} \frac{2}{2} = 1 \ , \ \frac{3}{6} = \frac{1}{2} \ \end{array} \right. \left(\text{ and } \frac{1}{2} < 1 \right) \right\}$	F.1	2	need to see correct quotients considered
	smallest positive quotient	E1	3	negative value must be mentioned as being considered but rejected
(ii)	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	M1		row operations
	$0 0 13 1 3 -\frac{1}{3} 0 1$	A1		1st, 2nd or 4th row correct
	0 1 -5 0 -1 ± 0 ±	A1		another of these 3 correct
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	A1	4	all correct (condone multiples of rows)
(b)(i)	No negatives in top row	E1	1	but must have no negative values in "their" top row
(ii)	One (inequality still has slack)	B1	1	
(c)(i)	P=7	B1√		FT their tableau
	$x = \frac{1}{2}$, $y = 0$, $z = 1$	B1 cao	2	condone one slip in final tableau
(ii)	Substituting "their" values from (c) (i)			
	$\frac{1}{2}k + 0 + 3 = 7$	M1		
	$\Rightarrow k = 8$	A1	2	
			13	

Q			So	lution		Marks	Total	Comments
5 (a)	Stage	Stata	From	Calculation				
5(a)	1	G	Т	Calculation	15			
		Н	Т		17	D 1		stopp 1 somment
		I	Т		26	B1		stage 1 correct
			_					
	2	D	G H	6 + 15	21 ← 20			
		Е	G G	3 + 17 $-3 + 15$	12			
		Е	Н	-3 + 13 -6 + 17	11	M1		7 values at stage 2 attempted
			I	-13 + 26	13 ←			with 5 unsimplified calculations correct
		F	Н	-7 + 17	10			
			I	-14 + 26	12 ←	A1		stage 2 correct
	3	A	D	<u>-4 + 21</u>	17	M1		use of two of "their" maxima from
		В	E D	6 + 13	19 ← 33 ←			Stage 2 to Stage 3
		В	E	12 + 21 16 + 13	29			
			F	18 + 12	30			
		С	E	14 + 13	27 ←			
			F	13 + 12	25	A1		stage 3 correct
						AI		stage 3 correct
	4	S	Α	12 + 19	31*			
			В	-2 + 33	31*	A 1		4.0.11.1
			С	3 + 27	30	A1cso	6	stage 4 & all other values correct
(b)	Maxin	num pi	ofit =	31		B1√		£31 million
	SAE	IT a	nd S	BDGT		B1		one correct path
						B1	3	second correct path and no other
					Total		9	

02 (cont)						
Q		Solution		Marks	Total	Comments
6 (a)	10 + 13 - 1 +	17		M1		3 values added and -1 (condone one slip)
	=	39		A1	2	
(b)(i)	<i>DE</i> 12			B1		on Figure 2
()()	FG 7			B1	2	
(ii)	arc	forward	backward	D1	_	
(II)	SA	3	Dackwai u 1			
	AB	1	1			
	BT	0	1			
	SC	0	2			
	CA	0	1			
	AD	0	1			
	CD	1	1			
	DE	1	2			
	BE	1	3	M1		at least 6 pairs correct on Figure 3
	ET	2	3	1711		(must have arrows)
	SF	1	1			(must have arrows)
	FC	1	2			
	FD	1	0			
	FG	0	1		•	
	DG	2	1	A1	2	all correct
	EG	1	1			
	GT	2	3			
(iii)	Table	2	3			
(111)		E4 Ela		3.41		
	Path	Extra Flow		M1		1 correct path and extra flow
	SABET	1				
	SFDGT	1		A1		all correct
	SACDGT	1				
						DEG triangle may have different flows
						with implications to triangle GET.
	Network					
		A	$\stackrel{\mathcal{X}^0}{\longrightarrow}$ B			
	1		$\overline{X_2}$			
	2 ¹	23	1 1/0	0		
	// x	8// 1	43	1		
	0 0	χ_0	\ D 1.	$E \xrightarrow{2^1}$		
	$s \leftarrow \frac{3}{2}$	$\overline{\overline{x_2}}$	\searrow $\stackrel{\longrightarrow}{}$ $\stackrel{\longrightarrow}{}$	$\xrightarrow{E} \xrightarrow{\overline{x_4}}$	\longrightarrow T	
		0,4	/ \	/ 04		
	10	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	$\frac{1}{2} \frac{1}{2} \frac{2}{10} \frac{1}{1}$	01/2		
	x2	2	23	54		
		F	$\stackrel{\circ}{\stackrel{\longleftarrow}{=}}$			
		I.	1 6			
				M1		1 path correctly augmented forward and
				101 1		backward
				A 1	4	but must have earned M1 in part (b)(ii)
				A1	4	network correct
	3. C. C	_		P. 1		
(c)(i)	Max flow = 3	1		B1	1	

Q	Solution	Marks	Total	Comments
6(c) cont. (ii)	Max flow	B2		correct flow of 37
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			condone 2 slips or omissions in flow of 37 or "correct" feasible flow of 36 for SC1
			2	
(d)	Cut through AB, AD, CD, FD and FG	B1	1	$\left\{ S,A,C,F \right\} \left\{ B,D,E,G,T \right\}$
	Total		14	
	TOTAL		75	