

Edexcel Maths FP1

Past Paper Pack

2009–2014

**6667/01**

# Edexcel GCE

## Further Pure Mathematics FP1

## Advanced/Advanced Subsidiary

## Friday 30 January 2009 – Afternoon

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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[illegible]

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## Mathematical Formulae (Orange)

Nil

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

In the boxes above, write your centre number, candidate number, your surname, initials and signature.

Check that you have the correct question paper.

Answer ALL the questions. Write your answers in the spaces provided in this question paper.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 10 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

You must ensure that your answers to parts of questions are clearly labelled.

You should show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.

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(5)

(b) Hence, or otherwise, find the value of  $\sum_{r=11}^{20} (6r^2 + 4r - 1)$ .

- (1)

(3)



$$f(x) = 3\sqrt{x} + \frac{18}{\sqrt{x}} - 20$$

- (a) Show that the equation  $f(x) = 0$  has a root  $\alpha$  in the interval  $[1.1, 1.2]$ . (2)
- (b) Find  $f'(x)$ . (3)
- (c) Using  $x_0 = 1.1$  as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x)$  to find a second approximation to  $\alpha$ , giving your answer to 3 significant figures. (4)

[illegible]

Prove by induction that  $u_n = 5 \times 6^{n-1} + 1$ , for  $n \geq 1$ .

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



(3)

(3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



- (b) Show on an Argand diagram the point  $P$  representing  $z_1$  and the point  $Q$  representing  $z_2$ .

- The circle passing through the points  $O$ ,  $P$  and  $Q$  has centre  $C$ . Find

- (e) the exact value of the radius of the circle. (2)

This image shows a full page of blank, lined paper. It features approximately 20 evenly spaced horizontal grey lines across its entire width, providing a template for writing or drawing. The margins are consistent on all sides.

$$\mathbf{A} = \begin{pmatrix} 3\sqrt{2} & 0 \\ 0 & 3\sqrt{2} \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \mathbf{C} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

- (e) Find the area of triangle  $OR'S'$  and deduce the area of triangle  $ORS$ . (3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



(a) Show  $z_1$  and  $z_2$  on a single Argand diagram.

(1)

(b) the value of  $|z_1|$ ,

(2)

(c) the value of  $\arg z_1$ , giving your answer in radians to 2 decimal places,

(2)

(d)  $\frac{z_2}{z_1}$  in the form  $a+bi$ , where  $a$  and  $b$  are real.

(3)

where  $k$  is a constant to be found.

(b) Hence evaluate  $\sum_{r=21}^{40} r(r+1)(r+3)$ .

(2)







(a) show that  $2.2 < \alpha < 2.3$

(2)

- (b) Taking 2.2 as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x) = x^3 - x^2 - 6$  to obtain a second approximation to  $\alpha$ , giving your answer to 3 decimal places.

(5)

- (c) Use linear interpolation once on the interval  $[2.2, 2.3]$  to find another approximation to  $\alpha$ , giving your answer to 3 decimal places.

(3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

**5.**

(a) Find  $\mathbf{R}^2$  in terms of  $a$  and  $b$ .

(3)

(b) find the value of  $a$  and the value of  $b$ .

(5)

[illegible]

- (b) Write down the coordinates of the focus  $S$  of  $C$ . (1)

- $$y+tx=8t+4t^3 \tag{5}$$

(d) Find the area of triangle  $PSN$  in terms of  $t$ , giving your answer in its simplest form. (4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(a) Find the value of  $a$  for which the matrix  $\mathbf{A}$  is singular.

(2)

(b) Find  $\mathbf{B}^{-1}$ .

(3)

Given that  $Q$  has coordinates  $(k - 6, 3k + 12)$ , where  $k$  is a constant,

(c) show that  $P$  lies on the line with equation  $y = x + 3$ .

(3)

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# Edexcel GCE

## Further Pure Mathematics FP1

## Advanced/Advanced Subsidiary

## Monday 1 February 2010 – Afternoon

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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[illegible]

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### Mathematical Formulae (Pink)

Nil

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A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

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There are 9 questions in this question paper. The total mark for this paper is 75.

There are 24 pages in this question paper. Any blank pages are indicated.

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Find, showing your working,

- (a)  $\frac{z_1}{z_2}$  in the form  $a + bi$ , where  $a$  and  $b$  are real,

(3)

- (b) the value of  $\left| \frac{z_1}{z_2} \right|$ ,

(2)

- (c) the value of  $\arg \frac{z_1}{z_2}$ , giving your answer in radians to 2 decimal places.

(2)



$$f(x) = 3x^2 - \frac{11}{x^2}$$

The equation  $f(x) = 0$  has a root  $\alpha$  between 1.3 and 1.4

- (b) Starting with the interval  $[1.3, 1.4]$ , use interval bisection to find an interval of width 0.025 which contains  $\alpha$ .
- (3)**

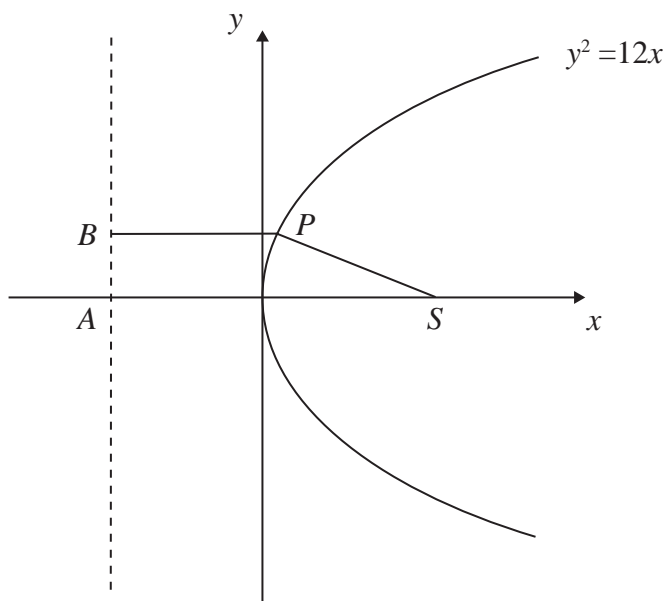
- (c) Taking 1.4 as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x)$  to obtain a second approximation to  $\alpha$ , giving your answer to 3 decimal places. (5)

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4.



**Figure 1**

Figure 1 shows a sketch of part of the parabola with equation  $y^2 = 12x$ .

The point  $P$  on the parabola has  $x$ -coordinate  $\frac{1}{3}$ .

The point  $S$  is the focus of the parabola.

(a) Write down the coordinates of  $S$ .

**(1)**

The points  $A$  and  $B$  lie on the directrix of the parabola.

The point  $A$  is on the  $x$ -axis and the  $y$ -coordinate of  $B$  is positive.

Given that  $ABPS$  is a trapezium,

(b) calculate the perimeter of  $ABPS$ .

**(5)**

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$$\mathbf{A} = \begin{pmatrix} a & -5 \\ 2 & a+4 \end{pmatrix}, \text{ where } a \text{ is real.}$$

- (a) Find  $\det \mathbf{A}$  in terms of  $a$ .

(2)

- (b) Show that the matrix  $\mathbf{A}$  is non-singular for all values of  $a$ .

(3)

Given that  $a = 0$ ,

- (c) find  $\mathbf{A}^{-1}$ .

(3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(a) write down the other complex root of the equation.

(1)

(b) Find the value of  $c$  and the value of  $d$ .

(5)

(c) Show the three roots of this equation on a single Argand diagram.

(2)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(a) Show that the tangent to  $H$  at  $P$  has equation

The tangents to  $H$  at the points  $A$  and  $B$  meet at the point  $(15c, -c)$ .

(b) Using the formulae for  $\sum_{r=1}^n r$  and  $\sum_{r=1}^n r^3$ , show that

(c) Hence evaluate  $\sum_{r=15}^{25} (r^3 + 3r + 2)$

**(2)**

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

$$\mathbf{M} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

- (e) Find the coordinates of  $C$ . (2)

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# Edexcel GCE

## Further Pure Mathematics FP1

## Advanced/Advanced Subsidiary

## Tuesday 22 June 2010 – Afternoon

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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[illegible]

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Mathematical Formulae (Pink)

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Nil

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

## Instructions to Candidates

Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer to each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

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There are 9 questions in this question paper. The total mark for this paper is 75.

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## Advice to Candidates

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(a) Show that  $z^2 = -5 - 12i$ .

(2)

Find, showing your working,

(b) the value of  $|z^2|$ ,

(2)

(c) the value of  $\arg(z^2)$ , giving your answer in radians to 2 decimal places.

(2)

(d) Show  $z$  and  $z^2$  on a single Argand diagram.

**(1)**



(a) Given that  $a = 2$ , find  $\mathbf{M}^{-1}$ .

(3)

(b) Find the values of  $a$  for which  $\mathbf{M}$  is singular.

(2)



$$f(x) = x^3 - \frac{7}{x} + 2, \quad x > 0$$

- (a) Show that  $f(x) = 0$  has a root  $\alpha$  between 1.4 and 1.5 (2)
- (b) Starting with the interval  $[1.4, 1.5]$ , use interval bisection twice to find an interval of width 0.025 that contains  $\alpha$ . (3)
- (c) Taking 1.45 as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x) = x^3 - \frac{7}{x} + 2$  to obtain a second approximation to  $\alpha$ , giving your answer to 3 decimal places. (5)



Given that  $f(x) = (x+3)(x^2+ax+b)$ , where  $a$  and  $b$  are real constants,

- (a) find the value of  $a$  and the value of  $b$ .

(2)

- (b) Find the three roots of  $f(x) = 0$ .

(4)

- (c) Find the sum of the three roots of  $f(x) = 0$ .

(1)

[illegible]



6. Write down the  $2 \times 2$  matrix that represents

(a) an enlargement with centre  $(0, 0)$  and scale factor 8, (1)

(b) a reflection in the  $x$ -axis. (1)

Hence, or otherwise,

(c) find the matrix **T** that represents an enlargement with centre  $(0, 0)$  and scale factor 8, followed by a reflection in the  $x$ -axis. (2)

$$\mathbf{A} = \begin{pmatrix} 6 & 1 \\ 4 & 2 \end{pmatrix} \text{ and } \mathbf{B} = \begin{pmatrix} k & 1 \\ c & -6 \end{pmatrix}, \text{ where } k \text{ and } c \text{ are constants.}$$

(d) Find **AB**. (3)

Given that **AB** represents the same transformation as **T**,

(e) find the value of  $k$  and the value of  $c$ . (2)

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$$\sum_{r=1}^n (r+2)(r+3) = \frac{1}{3}n(n^2 + an + b),$$
$$\sum_{r=n+1}^{2n} (r+2)(r+3) = \frac{1}{3}n(7n^2 + 27n + 26)$$

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**Edexcel GCE**  
**Further Pure Mathematics FP1**  
**Advanced/Advanced Subsidiary**  
Monday 31 January 2011 – Afternoon  
Time: 1 hour 30 minutes

[illegible]

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Mathematical Formulae (Pink)

Nil

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$$z = 5 - 3i, \quad w = 2 + 2i$$

(a)  $z^2$ ,

(2)

$$(b) \quad \frac{z}{w}.$$

(3)

**(Total 5 marks)**



The root  $\alpha$  of the equation  $f(x) = 0$  lies in the interval  $[1.6, 1.8]$ .

- (4)

- (2)

- (4)



$$\sum_{r=1}^n r(r+1)(r+5) = \frac{1}{4}n(n+1)(n+2)(n+7)$$

(5)

$$\sum_{r=20}^{50} r(r+1)(r+5)$$

(2)

6.

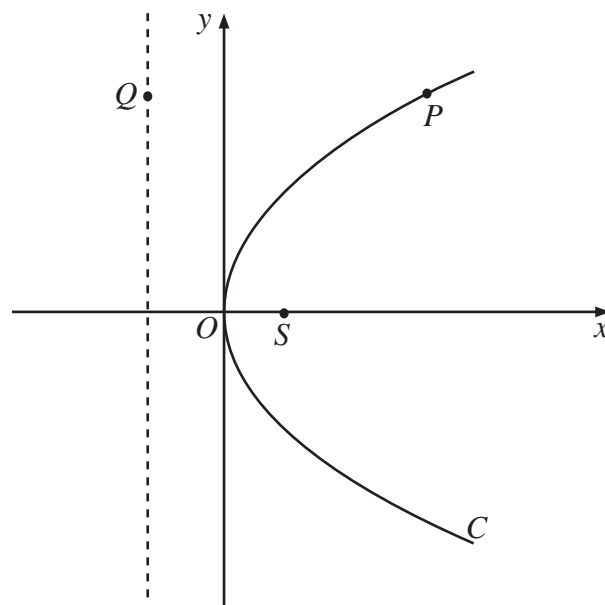
**Figure 1**

Figure 1 shows a sketch of the parabola  $C$  with equation  $y^2 = 36x$ .  
The point  $S$  is the focus of  $C$ .

(a) Find the coordinates of  $S$ . (1)

(b) Write down the equation of the directrix of  $C$ . (1)

Figure 1 shows the point  $P$  which lies on  $C$ , where  $y > 0$ , and the point  $Q$  which lies on the directrix of  $C$ . The line segment  $QP$  is parallel to the  $x$ -axis.

Given that the distance  $PS$  is 25,

(c) write down the distance  $QP$ , (1)

(d) find the coordinates of  $P$ , (3)

(e) find the area of the trapezium  $OSPQ$ . (2)

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7.  $z = -24 - 7i$

(a) Show  $z$  on an Argand diagram. (1)

(b) Calculate  $\arg z$ , giving your answer in radians to 2 decimal places. (2)

It is given that

$$w = a + bi, \quad a \in \mathbb{R}, b \in \mathbb{R}$$

Given also that  $|w| = 4$  and  $\arg w = \frac{5\pi}{6}$ ,

(c) find the values of  $a$  and  $b$ , (3)

(d) find the value of  $|zw|$ . (3)



$$\mathbf{A} = \begin{pmatrix} 2 & -2 \\ -1 & 3 \end{pmatrix}$$

- (1)

- (2)

(2)

(4)



Leave  
blank

**10.** The point  $P\left(6t, \frac{6}{t}\right)$ ,  $t \neq 0$ , lies on the rectangular hyperbola  $H$  with equation  $xy = 36$ .

(a) Show that an equation for the tangent to  $H$  at  $P$  is

$$y = -\frac{1}{t^2}x + \frac{12}{t} \quad (5)$$

The tangent to  $H$  at the point  $A$  and the tangent to  $H$  at the point  $B$  meet at the point  $(-9, 12)$ .

(b) Find the coordinates of  $A$  and  $B$ . (7)

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# Edexcel GCE

## Further Pure Mathematics FP1

## Advanced/Advanced Subsidiary

## Wednesday 22 June 2011 – Morning

Time: 1 hour 30 minutes

### Materials required for examination

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Mathematical Formulae (Pink)

### Items included with question papers

Nil

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[illegible]

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(a) Find the modulus of  $z_1$ .

**(1)**

(b) Find, in radians, the argument of  $z_1$ , giving your answer to 2 decimal places.

**(2)**

The solutions to the quadratic equation

$$z^2 - 10z + 28 = 0$$

are  $z_2$  and  $z_3$ .

(c) Find  $z_2$  and  $z_3$ , giving your answers in the form  $p \pm i\sqrt{q}$ , where  $p$  and  $q$  are integers.

(3)

(d) Show, on an Argand diagram, the points representing your complex numbers  $z_1$ ,  $z_2$  and  $z_3$ .

(2)

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- (4)

- $$\mathbf{B} = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$$

(2)

- $$\mathbf{C} = \begin{pmatrix} k+1 & 12 \\ k & 9 \end{pmatrix}$$

(3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



$$f(x) = x^2 + \frac{5}{2x} - 3x - 1, \quad x \neq 0$$

- (2)

**(4)**

This image shows a full page of blank, lined paper. It features approximately 20 evenly spaced horizontal grey lines across its entire width, providing a template for writing or drawing. The margins are consistent on all sides.

$$\mathbf{A} = \begin{pmatrix} -4 & a \\ b & -2 \end{pmatrix}, \text{ where } a \text{ and } b \text{ are constants.}$$

(a) find the value of  $a$  and the value of  $b$ .

(4)

Using your values of  $a$  and  $b$ ,

(b) find the area of quadrilateral  $S$ .

(4)

[illegible]



$$\sum_{r=1}^n (2r-1)^2 = \frac{1}{3}n(2n+1)(2n-1)$$

(6)

$$\sum_{r=n+1}^{3n} (2r-1)^2 = \frac{2}{3}n(an^2 + b)$$

(4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(a) Find the equation of the directrix of  $C$ .

(2)

$$x - ty + 12t^2 = 0$$

(4)

(c) Find the coordinates of  $X$ .

(4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.











(b) Show that the equation of the normal to  $C$  at  $P$  is  $y + tx = 8t + 4t^3$ . (5)

[illegible]

- (b) Describe fully the transformation represented by  $\mathbf{P}$ . (2)

(c) Find  $\mathbf{QR}$ . (2)

- (d) Find the determinant of  $\mathbf{QR}$ . (2)

- (e) Using your answer to part (d), find the area of  $T''$ . (3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

are  $z_1$ ,  $z_2$  and  $z_3$ .

- (a) Given that  $z_1 = 3 + i$ , find  $z_2$  and  $z_3$ .

(4)

- (b) Show, on a single Argand diagram, the points representing  $z_1$ ,  $z_2$  and  $z_3$ .

(2)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(b) Using the result in part (a), show that

(c) Calculate the exact value of  $\sum_{r=20}^{50} (r^3 - 2)$ . (3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



$$\mathbf{A} = \begin{pmatrix} 0 & 1 \\ 2 & 3 \end{pmatrix}$$

- (2)

- (4)

[illegible]

(a) Show that the equation of the tangent at  $P$  is  $x + p^2y = 6p$ .

(4)

(b) Write down the equation of the tangent at  $Q$ .

(1)

(c) Find, as single fractions in their simplest form, the coordinates of  $R$  in terms of  $p$  and  $q$ .

(4)





6667/01

# Edexcel GCE

## Further Pure Mathematics FP1

## Advanced/Advanced Subsidiary

## Friday 1 June 2012 – Morning

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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[illegible]

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Mathematical Formulae (Pink)

Nil

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them.**

In the boxes above, write your centre number, candidate number, your surname, initials and signature.

Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer to each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 10 questions in this question paper. The total mark for this paper is 75.

There are 32 pages in this question paper. Any blank pages are indicated.

You must ensure that your answers to parts of questions are clearly labelled.

You should show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.

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**P40688A**

W850/R6667/57570 5/5/4



*Turn over*

PEARSON

(a) Show that  $f(4) = 0$

(1)

(b) Use algebra to solve  $f(x) = 0$  completely.

(4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(2)

$$\mathbf{C} = \begin{pmatrix} 3 & 2 \\ 8 & 6 \end{pmatrix}, \quad \mathbf{D} = \begin{pmatrix} 5 & 2k \\ 4 & k \end{pmatrix}, \text{ where } k \text{ is a constant}$$
$$\mathbf{E} = \mathbf{C} + \mathbf{D}$$

(4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

$$f(x) = x^2 + \frac{3}{4\sqrt{x}} - 3x - 7, \quad x > 0$$

Taking 4 as a first approximation to  $\alpha$ , apply the Newton-Raphson process once to  $f(x)$  to obtain a second approximation to  $\alpha$ . Give your answer to 2 decimal places.

(6)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

4. (a) Use the standard results for  $\sum_{r=1}^n r^3$  and  $\sum_{r=1}^n r$  to show that

$$\sum_{r=1}^n (r^3 + 6r - 3) = \frac{1}{4}n^2(n^2 + 2n + 13)$$

for all positive integers  $n$ .

(5)

- (b) Hence find the exact value of

$$\sum_{r=16}^{30} (r^3 + 6r - 3)$$

(2)

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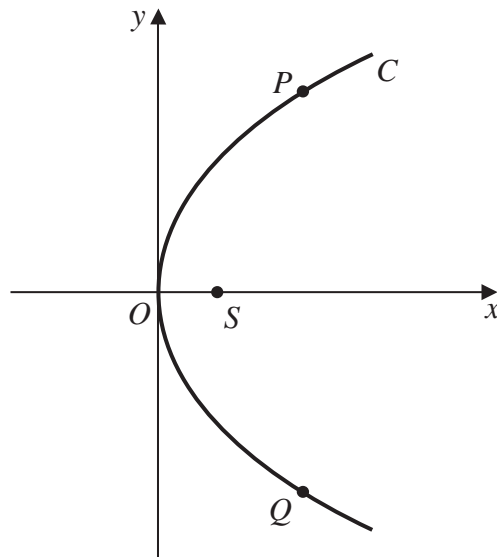


Figure 1 shows a sketch of the parabola  $C$  with equation  $y^2 = 8x$ . The point  $P$  lies on  $C$ , where  $y > 0$ , and the point  $Q$  lies on  $C$ , where  $y < 0$ . The line segment  $PQ$  is parallel to the  $y$ -axis.

(a) write down the  $y$ -coordinate of  $P$ ,

(b) find the  $x$ -coordinate of  $P$ . (2)

(c) Find an equation for  $l$  in the form  $ax + by + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers. (4)

[illegible]

$$f(x) = \tan\left(\frac{x}{2}\right) + 3x - 6, \quad -\pi < x < \pi$$

- (a) Show that the equation  $f(x) = 0$  has a root  $\alpha$  in the interval  $[1, 2]$ . (2)
- (b) Use linear interpolation once on the interval  $[1, 2]$  to find an approximation to  $\alpha$ .  
Give your answer to 2 decimal places. (3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(a) Calculate  $\arg z$ , giving your answer in radians to 2 decimal places.

(2)

(b)  $z + z^2$  in the form  $a + bi\sqrt{3}$ , where  $a$  and  $b$  are integers,

(3)

(c)  $\frac{z+7}{z-1}$  in the form  $c + d\mathrm{i}\sqrt{3}$ , where  $c$  and  $d$  are integers.

(4)

$$w \equiv \lambda - 3i$$

where  $\lambda$  is a real constant, and  $\arg(4 - 5i + 3w) = -\frac{\pi}{2}$ ,

(d) find the value of  $\lambda$ .

(2)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.





9. 
$$\mathbf{M} = \begin{pmatrix} 3 & 4 \\ 2 & -5 \end{pmatrix}$$

(a) Find  $\det \mathbf{M}$ .

(1)

The transformation represented by  $\mathbf{M}$  maps the point  $S(2a - 7, a - 1)$ , where  $a$  is a constant, onto the point  $S'(25, -14)$ .

(b) Find the value of  $a$ .

(3)

The point  $R$  has coordinates  $(6, 0)$ .

Given that  $O$  is the origin,

(c) find the area of triangle  $ORS$ .

(2)

Triangle  $ORS$  is mapped onto triangle  $OR'S'$  by the transformation represented by  $\mathbf{M}$ .

(d) Find the area of triangle  $OR'S'$ .

(2)

Given that

$$\mathbf{A} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$

(e) describe fully the single geometrical transformation represented by  $\mathbf{A}$ .

(2)

The transformation represented by  $\mathbf{A}$  followed by the transformation represented by  $\mathbf{B}$  is equivalent to the transformation represented by  $\mathbf{M}$ .

(f) Find  $\mathbf{B}$ .

(4)

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6667/01

# Edexcel GCE

## Further Pure Mathematics FP1

## Advanced/Advanced Subsidiary

## Monday 28 January 2013 – Morning

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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[illegible]

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### Mathematical Formulae (Pink)

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Nil

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them.**

In the boxes above, write your centre number, candidate number, your surname, initials and signature.

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Full marks may be obtained for answers to ALL questions.

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There are 9 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

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You must ensure that your answers to parts of questions are clearly labelled.

You should show sufficient working to make your methods clear to the Examiner.

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**P41485A**

W850/R6667/57570 5/5/5/5/6/



*Turn over*

PEARSON

1. Show, using the formulae for  $\sum_{r=1}^n r$  and  $\sum_{r=1}^n r^2$ , that

$$\sum_{r=1}^n 3(2r-1)^2 = n(2n+1)(2n-1), \text{ for all positive integers } n.$$

(5)



$$z = \frac{50}{3+4i}$$

(a)  $z$ ,

(2)

(b)  $z^2$ .

(2)

Find

(c)  $|z|$ ,

(2)

(d)  $\arg z^2$ , giving your answer in degrees to 1 decimal place.

(2)

[illegible]

(a) Find  $f'(x)$ .

(2)

The equation  $f(x) = 0$  has a root  $\alpha$  in the interval  $[4.5, 5.5]$ .

- (b) Using  $x_0 = 5$  as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x)$  to find a second approximation to  $\alpha$ , giving your answer to 3 significant figures.

(4)



- (1)**

**(1)**

(1)

- (2)

- (2)

[illegible]



- (2)

$$\mathbf{X} = \begin{pmatrix} 1 & a \\ 3 & 2 \end{pmatrix}, \text{ where } a \text{ is a constant.}$$

- (2)

$$\mathbf{Y} = \begin{pmatrix} 1 & -1 \\ 3 & 2 \end{pmatrix}$$

- (2)

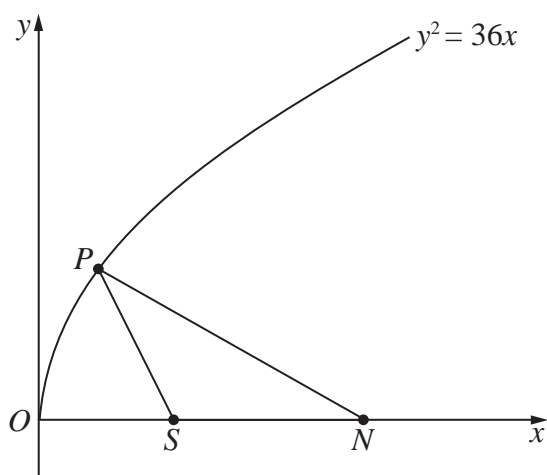
Given that  $B$  has coordinates  $(1 - \lambda, 7\lambda - 2)$ , where  $\lambda$  is a constant,

- (4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.







### Figure 1

The point  $P(4, 12)$  lies on the parabola.

- (a) Find an equation for the normal to the parabola at  $P$ . (5)

This normal meets the  $x$ -axis at the point  $N$  and  $S$  is the focus of the parabola, as shown in Figure 1.

- (b) Find the area of triangle  $PSN$ . (4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



(4)

[illegible]

(a) Show that the equation  $f(x) = 0$  has a root  $\alpha$  in the interval  $[2.5, 3]$ .

(2)

- (b) Use linear interpolation once on the interval  $[2.5, 3]$  to find an approximation for  $\alpha$ , giving your answer to 2 decimal places.

(3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.







(b) Hence show that

(4)

[illegible]

(a) Show that an equation of the tangent to the parabola at  $P$  is

$$py - x = ap^2 \quad (4)$$

(b) Write down the equation of the tangent at  $Q$ . (1)

(c) Find, in terms of  $p$  and  $q$ , the coordinates of  $R$ , giving your answers in their simplest form.

(d) find the value of  $pq$ . (2)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(2)

(4)

(3)

(2)

$$\mathbf{A} = \begin{pmatrix} 6 & -2 \\ -4 & 1 \end{pmatrix}$$

(a) Prove that

$$\mathbf{A}^2 = 7\mathbf{A} + 2\mathbf{I} \quad (2)$$

(b) Hence show that

$$\mathbf{A}^{-1} = \frac{1}{2}(\mathbf{A} - 7\mathbf{I}) \quad (2)$$

Given that  $Q$  has coordinates  $(2k + 8, -2k - 5)$ , where  $k$  is a constant,

(c) find, in terms of  $k$ , the coordinates of  $P$ . (4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

$$u_{n+1} = 4u_n - 9n, \quad n \geq 1$$

$$u_n = 4^n + 3n + 1$$

(b) Prove by induction that, for  $m \in \mathbb{Z}^+$ ,

$$\begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}^m = \begin{pmatrix} 2m+1 & -4m \\ m & 1-2m \end{pmatrix}$$







$$\mathbf{A} = \begin{pmatrix} 2k+1 & k \\ -3 & -5 \end{pmatrix}, \text{ where } k \text{ is a constant}$$

$$\mathbf{B} = \mathbf{A} + 3\mathbf{I}$$

(a)  $\mathbf{B}$  in terms of  $k$ ,

(2)

(b) the value of  $k$  for which  $\mathbf{B}$  is singular.

(2)

(ii) Given that

$$\mathbf{C} = \begin{pmatrix} 2 \\ -3 \\ 4 \end{pmatrix}, \quad \mathbf{D} = (2 \ -1 \ 5)$$

and

$$\mathbf{E} = \mathbf{CD}$$

find **E**.

(2)



(a) Show that the equation  $f(x) = 0$  has a root  $\alpha$  between  $x = 2$  and  $x = 2.5$  (2)

- (b) Starting with the interval  $[2, 2.5]$  use interval bisection twice to find an interval of width 0.125 which contains  $\alpha$ .
- (3)**

(c) Taking  $-1.5$  as a first approximation to  $\beta$ , apply the Newton-Raphson process once to  $f(x)$  to obtain a second approximation to  $\beta$ .  
Give your answer to 2 decimal places. (5)



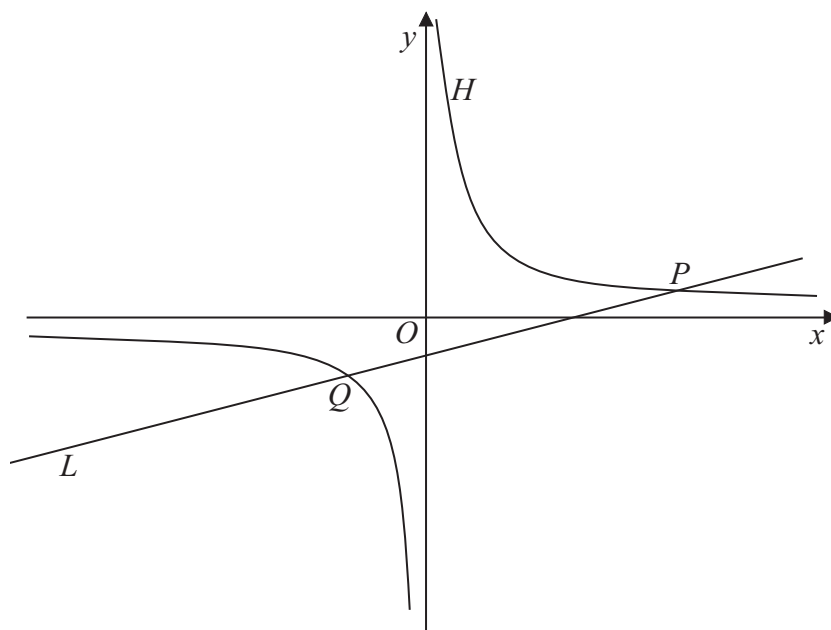


Figure 1 shows a rectangular hyperbola  $H$  with parametric equations

$$x = 3t, \quad y = \frac{3}{t}, \quad t \neq 0$$

(a) Show that  $L$  intersects  $H$  where  $4t^2 - 5t - 6 = 0$

(3)

(b) Hence, or otherwise, find the coordinates of points  $P$  and  $Q$ .

(5)

[illegible]

$$\mathbf{A} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 2 & 3 \\ 1 & 4 \end{pmatrix}$$

(a) Find the matrix  $\mathbf{P}$ .

(2)

(b) find the area of triangle  $T$ .

(3)

(c) Find the matrix  $\mathbf{Q}$ .

(2)





(b) Hence, show that

where  $a$ ,  $b$  and  $c$  are integers to be found. (4)





$$\sum_{r=1}^{24} (r^3 - 4r)$$

(ii) Use the standard results for  $\sum_{r=1}^n r^2$  and  $\sum_{r=1}^n r$  to show that

$$\sum_{r=0}^n (r^2 - 2r + 2n + 1) = \frac{1}{6}(n+1)(n+a)(bn+c)$$

(6)

Write your name here

Surname

Other names

**Pearson Edexcel**  
**International**  
**Advanced Level**

Centre Number

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Candidate Number

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# Further Pure Mathematics FP1

## Advanced/Advanced Subsidiary

Wednesday 29 January 2014 – Morning  
**Time: 1 hour 30 minutes**

Paper Reference

**6667A/01****You must have:**

Mathematical Formulae and Statistical Tables (Pink)

Total Marks

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

**Instructions**

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

**Information**

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

**Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

**P43019A**

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5/5/5/

**PEARSON**

- (b) Starting with the interval  $[1, 1.4]$ , use interval bisection twice to find an interval of width 0.1 which contains  $\alpha$ .
- (3)**

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

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Question 1 continued

Lined area for writing the answer to Question 1.

Q1

Mark box for Q1.

(Total 5 marks)



The triangle  $T$  is transformed to the triangle  $T'$  by the transformation represented by  $\mathbf{A}$ .

Given that the area of triangle  $T'$  is twice the area of triangle  $T$ , find the possible values of  $k$ .

(4)

(ii) Given that

$$\mathbf{B} = \begin{pmatrix} 1 & -2 & 3 \\ -2 & 5 & 1 \end{pmatrix}, \quad \mathbf{C} = \begin{pmatrix} 2 & 8 \\ 0 & 2 \\ 1 & -2 \end{pmatrix}$$

find **BC**.

(3)



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Question 2 continued

Handwriting practice lines for Question 2 continued.

(Total 7 marks)

Q2

Mark box for Q2







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Question 3 continued

Handwriting practice lines for Question 3 continued.

(Total 4 marks)

Q3

Mark box for Q3





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Question 4 continued

Handwriting practice area with 30 horizontal lines.

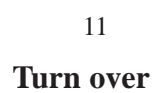
Q4

Mark box for Q4

(Total 5 marks)









1041



6. (a) Use the standard results for  $\sum_{r=1}^n r^3$  and  $\sum_{r=1}^n r$  to show that for all positive integers  $n$ ,

$$\sum_{r=1}^n r(r+1)(r-1) = \frac{1}{4}n(n+1)(n-1)(n+a)$$

where  $a$  is an integer to be determined.

(4)

- (b) Hence find the value of  $n$ , where  $n > 1$ , that satisfies

$$\sum_{r=1}^n r(r+1)(r-1) = 10 \sum_{r=1}^n r^2$$

(5)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



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Question 6 continued

Lined area for writing the answer to Question 6.



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**Question 6 continued**



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Question 6 continued

Lined area for writing the answer to Question 6.

Q6

(Total 9 marks)



$$\mathbf{P} = \begin{pmatrix} 3a & -2a \\ -b & 2b \end{pmatrix}, \quad \mathbf{M} = \begin{pmatrix} -6a & 7a \\ 2b & -b \end{pmatrix};$$

(a) Find  $\mathbf{P}^{-1}$ , leaving your answer in terms of  $a$  and  $b$ .

(3)

$$\mathbf{M} = \mathbf{PQ}$$

(b) find the matrix  $\mathbf{Q}$ , giving your answer in its simplest form.

(3)

[illegible]

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Question 7 continued

Handwriting practice lines for Question 7 continued.

(Total 6 marks)

Q7

Mark box for Q7











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Question 8 continued

Lined area for writing the answer to Question 8.

(Total 12 marks)

Q8





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Question 9 continued

Lined area for writing the answer to Question 9.





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Question 9 continued

Lined area for writing the answer to Question 9.

(Total 8 marks)

Q9

Mark box for Question 9.













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**Question 10 continued**

**Q10**

**(Total 11 marks)**

**TOTAL FOR PAPER: 75 MARKS**

**END**





where  $p$  is an integer.

- (a) Find  $\frac{z_1}{z_2}$  in the form  $a + bi$  where  $a$  and  $b$  are real. Give your answer in its simplest form in terms of  $p$ .

Given that  $\left| \frac{z_1}{z_2} \right| = 13$ ,

- (b) find the possible values of  $p$ .

(4)

(4)

$$f(x) = x^3 - \frac{5}{2x^{\frac{3}{2}}} + 2x - 3, \quad x > 0$$

- (a) Show that the equation  $f(x) = 0$  has a root  $\alpha$  in the interval  $[1.1, 1.5]$ . (2)
- (b) Find  $f'(x)$ . (2)
- (c) Using  $x_0 = 1.1$  as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x)$  to find a second approximation to  $\alpha$ , giving your answer to 3 decimal places. (3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



- (4)

- $\mathbf{C} = \begin{pmatrix} 2k & -2 \\ 3 & k \end{pmatrix}$ , where  $k$  is a real number

(3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

(b) Hence show that

where  $a$  and  $b$  are constants to be found.

(3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.





















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Question 9 continued

Handwriting practice area with horizontal lines.

(Total 6 marks)

Q9

Mark box for Q9

TOTAL FOR PAPER: 75 MARKS

END



Centre No.						Paper Reference							Surname	Initial(s)
Candidate No.						<b>6</b>	<b>6</b>	<b>6</b>	<b>7</b>	<b>/</b>	<b>0</b>	<b>1 R</b>	Signature	

Paper Reference(s)

**6667/01R**

# Edexcel GCE

## Further Pure Mathematics FP1

## Advanced/Advanced Subsidiary

## Tuesday 10 June 2014 – Morning

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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[illegible]

### Materials required for examination

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Mathematical Formulae (Pink)

### Items included with question papers

Nil

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them.**

## Instructions to Candidates

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Answer ALL the questions.

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*Turn over*

PEARSON



(a) Show that the equation  $f(x) = 0$  has a root  $\alpha$  in the interval  $[2, 3]$ .

(2)

(b) Use linear interpolation once on the interval  $[2, 3]$  to find an approximation to  $\alpha$ .

Give your answer to 3 decimal places.

(3)

(c) The equation  $f(x) = 0$  has another root  $\beta$  in the interval  $[-1, 0]$ . Starting with this interval, use interval bisection to find an interval of width 0.25 which contains  $\beta$ .

(4)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

$$\mathbf{M} = \begin{pmatrix} 3 & k \\ -2 & 3 \end{pmatrix}, \quad \text{where } k \text{ is a positive constant.}$$

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

$$z = \frac{p + 2i}{3 + pi}$$

(a) Express  $z$  in the form  $a + bi$  where  $a$  and  $b$  are real. Give your answer in its simplest form in terms of  $p$ .

(4)

(b) Given that  $\arg(z) = \theta$ , where  $\tan \theta = 1$  find the possible values of  $p$ .

(5)

[illegible]



(b) Calculate the value of  $\sum_{r=10}^{50} r(r^2 - 3)$  (3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.





$$y + px = 2ap + ap^3 \quad (5)$$

(b) Write down an equation of the normal to  $C$  at the point  $P'$ . (1)

(c) Find, in terms of  $a$  and  $p$ , the coordinates of  $Q$ .

(d) find the area of the quadrilateral  $SPQP'$ . (3)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



An equation for the tangent to  $H$  at  $P$  is given by

$$y = -\frac{1}{t^2}x + \frac{2c}{t}$$

The points  $A$  and  $B$  lie on  $H$ .

The tangent to  $H$  at  $A$  and the tangent to  $H$  at  $B$  meet at the point  $\left(-\frac{6}{7}c, \frac{12}{7}c\right)$ .

Find, in terms of  $c$ , the coordinates of  $A$  and the coordinates of  $B$ .

(5)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



$$u_n = 4^{n+1} - 2^{n+3}$$


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**Question 9 continued**

**Q9**

**(Total 12 marks)**

**TOTAL FOR PAPER: 75 MARKS**

**END**



## Further Pure Mathematics FP1

Candidates sitting FP1 may also require those formulae listed under Core Mathematics C1 and C2.

### Summations

$$\sum_{r=1}^n r^2 = \frac{1}{6} n(n+1)(2n+1)$$

$$\sum_{r=1}^n r^3 = \frac{1}{4} n^2 (n+1)^2$$

### Numerical solution of equations

The Newton-Raphson iteration for solving  $f(x) = 0$ :  $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$

### Conics

	Parabola	Rectangular Hyperbola
Standard Form	$y^2 = 4ax$	$xy = c^2$
Parametric Form	$(at^2, 2at)$	$\left(ct, \frac{c}{t}\right)$
Foci	$(a, 0)$	Not required
Directrices	$x = -a$	Not required

### Matrix transformations

Anticlockwise rotation through  $\theta$  about  $O$ :  $\begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$

Reflection in the line  $y = (\tan \theta)x$ :  $\begin{pmatrix} \cos 2\theta & \sin 2\theta \\ \sin 2\theta & -\cos 2\theta \end{pmatrix}$

In FP1,  $\theta$  will be a multiple of  $45^\circ$ .



## Core Mathematics C1

### *Mensuration*

$$\text{Surface area of sphere} = 4\pi r^2$$

$$\text{Area of curved surface of cone} = \pi r \times \text{slant height}$$

### *Arithmetic series*

$$u_n = a + (n - 1)d$$

$$S_n = \frac{1}{2}n(a + l) = \frac{1}{2}n[2a + (n - 1)d]$$

## Core Mathematics C2

Candidates sitting C2 may also require those formulae listed under Core Mathematics C1.

### *Cosine rule*

$$a^2 = b^2 + c^2 - 2bc \cos A$$

### *Binomial series*

$$(a+b)^n = a^n + \binom{n}{1} a^{n-1}b + \binom{n}{2} a^{n-2}b^2 + \dots + \binom{n}{r} a^{n-r}b^r + \dots + b^n \quad (n \in \mathbb{N})$$

$$\text{where } \binom{n}{r} = {}^nC_r = \frac{n!}{r!(n-r)!}$$

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{1 \times 2} x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{1 \times 2 \times \dots \times r} x^r + \dots \quad (|x| < 1, n \in \mathbb{R})$$

### *Logarithms and exponentials*

$$\log_a x = \frac{\log_b x}{\log_b a}$$

### *Geometric series*

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r}$$

$$S_\infty = \frac{a}{1-r} \text{ for } |r| < 1$$

### *Numerical integration*

$$\text{The trapezium rule: } \int_a^b y \, dx \approx \frac{1}{2} h \{ (y_0 + y_n) + 2(y_1 + y_2 + \dots + y_{n-1}) \}, \text{ where } h = \frac{b-a}{n}$$