

1. Jean regularly takes a break from work to go to the post office. The amount of time Jean waits in the queue to be served at the post office has a continuous uniform distribution between 0 and 10 minutes.

(a) Find the mean and variance of the time Jean spends in the post office queue. (3)

(b) Find the probability that Jean does not have to wait more than 2 minutes. (2)

Jean visits the post office 5 times.

(c) Find the probability that she never has to wait more than 2 minutes. (2)

Jean is in the queue when she receives a message that she must return to work for an urgent meeting. She can only wait in the queue for a further 3 minutes.

Given that Jean has already been queuing for 5 minutes,

(d) find the probability that she must leave the post office queue without being served. (3)



2. In a large college 58% of students are female and 42% are male. A random sample of 100 students is chosen from the college. Using a suitable approximation find the probability that more than half the sample are female.

(7)



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5. Sue throws a fair coin 15 times and records the number of times it shows a head.

(a) State the distribution to model the number of times the coin shows a head. (2)

Find the probability that Sue records

(b) exactly 8 heads, (2)

(c) at least 4 heads. (2)

Sue has a different coin which she believes is biased in favour of heads. She throws the coin 15 times and obtains 13 heads.

(d) Test Sue's belief at the 1% level of significance. State your hypotheses clearly. (6)



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Question 5 continued

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6. A call centre agent handles telephone calls at a rate of 18 per hour.
- (a) Give two reasons to support the use of a Poisson distribution as a suitable model for the number of calls per hour handled by the agent. (2)

 - (b) Find the probability that in any randomly selected 15 minute interval the agent handles
 - (i) exactly 5 calls,
 - (ii) more than 8 calls. (5)

The agent received some training to increase the number of calls handled per hour. During a randomly selected 30 minute interval after the training the agent handles 14 calls.

- (c) Test, at the 5% level of significance, whether or not there is evidence to support the suggestion that the rate at which the agent handles calls has increased. State your hypotheses clearly. (6)



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7. A random variable X has probability density function given by

$$f(x) = \begin{cases} \frac{1}{2}x & 0 \leq x < 1 \\ kx^3 & 1 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

where k is a constant.

(a) Show that $k = \frac{1}{5}$ **(4)**

(b) Calculate the mean of X . **(4)**

(c) Specify fully the cumulative distribution function $F(x)$. **(7)**

(d) Find the median of X . **(3)**

(e) Comment on the skewness of the distribution of X . **(2)**



