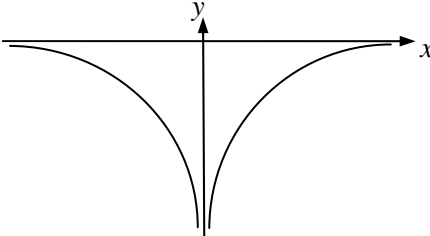
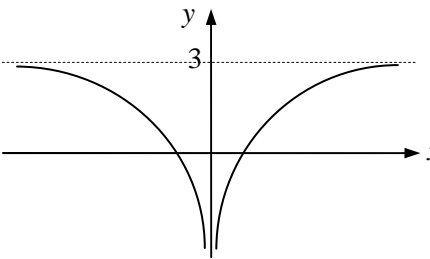
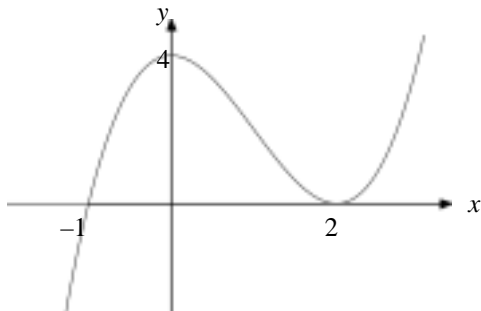


1 (i)	1	B1	1
(ii)	$\frac{1}{3}$	M1	$\frac{1}{9^2}$ or $\frac{1}{\sqrt{9}}$ soi
		A1	$\frac{2}{3}$ 3
2 (i)		B1*	Reasonably correct curve for $y = -\frac{1}{x^2}$ in 3 rd and 4 th quadrants only
		B1 dep*	2 Very good curves in curve for $y = -\frac{1}{x^2}$ in 3 rd and 4 th quadrants
		SC	If 0, very good single curve in either 3 rd or 4 th quadrant and nothing in other three quadrants. B1
(ii)		M1	Translation of their $y = -\frac{1}{x^2}$ vertically
		A1	2 Reasonably correct curve, horizontal asymptote soi at $y = 3$
(iii)	$y = -\frac{2}{x^2}$	B1	1 5
3 (i)	$\frac{12(3 - \sqrt{5})}{(3 + \sqrt{5})(3 - \sqrt{5})}$	M1	Multiply numerator and denom by $3 - \sqrt{5}$
	$= \frac{12(3 - \sqrt{5})}{9 - 5}$	A1	$(3 + \sqrt{5})(3 - \sqrt{5}) = 9 - 5$
	$= 9 - 3\sqrt{5}$	A1	3
(ii)	$3\sqrt{2} - \sqrt{2}$	M1	Attempt to express $\sqrt{18}$ as $k\sqrt{2}$
	$= 2\sqrt{2}$	A1	$\frac{2}{5}$ 5

4 (i)	$(x^2 - 4x + 4)(x + 1)$	M1		Attempt to multiply a 3 term quadratic by a linear factor or to expand all 3 brackets with an appropriate number of terms (including an x^3 term)
		A1		Expansion with at most 1 incorrect term
	$= x^3 - 3x^2 + 4$	A1	3	Correct, simplified answer

(ii)



B1		+ve cubic with 2 or 3 roots
B1		Intercept of curve labelled (0, 4) or indicated on y-axis
B1	3	(-1, 0) and turning point at (2, 0) labelled or indicated on x-axis and no other x intercepts
		6

5	$k = x^2$	M1*		Use a substitution to obtain a quadratic or factorise into 2 brackets each containing x^2
	$4k^2 + 3k - 1 = 0$			
	$(4k - 1)(k + 1) = 0$	M1		Correct method to solve a quadratic
	$k = \frac{1}{4}$ (or $k = -1$)	dep		
	$x = \pm \frac{1}{2}$	A1		Attempt to square root to obtain $x = \pm \frac{1}{2}$ and no other values
				5

6	$y = 2x + 6x^{-\frac{1}{2}}$	M1		Attempt to differentiate
	$\frac{dy}{dx} = 2 - 3x^{-\frac{3}{2}}$	A1		$kx^{-\frac{3}{2}}$
		A1		Completely correct expression (no +c)
	When $x = 4$, gradient = $2 - \frac{3}{\sqrt{4^3}}$	M1		Correct evaluation of either $4^{-\frac{3}{2}}$ or $4^{-\frac{1}{2}}$
	$= \frac{13}{8}$	A1	5	
				5

7	$2(6 - 2y)^2 + y^2 = 57$	M1*		substitute for x/y or attempt to get an equation in 1 variable only
		A1		correct unsimplified expression
	$2(36 - 24y + 4y^2) + y^2 = 57$			
	$9y^2 - 48y + 15 = 0$	A1		obtain correct 3 term quadratic
	$3y^2 - 16y + 5 = 0$			
	$(3y - 1)(y - 5) = 0$	M1		correct method to solve 3 term quadratic
	$y = \frac{1}{3}$ or $y = 5$	dep		
	$x = \frac{16}{3}$ or $x = -4$	A1		SC If A0 A0, one correct pair of values, spotted or from correct factorisation
				6
				6
				B1

<p>8 (i) $2(x^2 + \frac{5}{2}x)$</p> $= 2\left[\left(x + \frac{5}{4}\right)^2 - \frac{25}{16}\right]$ $= 2\left(x + \frac{5}{4}\right)^2 - \frac{25}{8}$	<p>B1</p> <p>M1</p> <p>A1</p>	<p>$\left(x + \frac{5}{4}\right)^2$</p> <p>$q = -2p^2$</p> <p>$q = -\frac{25}{8}$ c.w.o.</p>
<p>(ii) $\left(-\frac{5}{4}, -\frac{25}{8}\right)$</p>	<p>B1✓</p> <p>B1✓</p>	<p>2</p>
<p>(iii) $x = -\frac{5}{4}$</p>	<p>B1</p>	<p>1</p>
<p>(iv) $x(2x + 5) > 0$</p> $x < -\frac{5}{2}, x > 0$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>Correct method to find roots</p> <p>$0, -\frac{5}{2}$ seen</p> <p>Correct method to solve quadratic inequality.</p> <p>(not wrapped, strict inequalities, no 'and')</p> <p>4</p> <p>10</p>
<p>9 (i) $\frac{4+p}{2} = -1, \frac{5+q}{2} = 3$</p> $p = -6$ $q = 1$	<p>M1</p> <p>A1</p> <p>A1</p>	<p>Correct method (may be implied by one correct coordinate)</p> <p>3</p>
<p>(ii) $r^2 = (4 - 1)^2 + (5 - 3)^2$</p> $r = \sqrt{29}$	<p>M1</p> <p>A1</p>	<p>Use of $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ for either radius or diameter</p> <p>2</p>
<p>(iii) $(x+1)^2 + (y-3)^2 = 29$</p> $x^2 + y^2 + 2x - 6y - 19 = 0$	<p>M1</p> <p>M1</p> <p>A1</p>	<p>$(x+1)^2$ and $(y-3)^2$ seen</p> <p>$(x \pm 1)^2 + (y \pm 3)^2 = \text{their } r^2$</p> <p>Correct equation in correct form</p> <p>3</p>
<p>(iv) gradient of radius = $\frac{3-5}{-1-4}$</p> $= \frac{2}{5}$ <p>gradient of tangent = $-\frac{5}{2}$</p> $y - 5 = -\frac{5}{2}(x - 4)$ $y = -\frac{5}{2}x + 15$	<p>M1</p> <p>A1</p> <p>B1✓</p> <p>M1</p> <p>A1</p>	<p>uses $\frac{y_2 - y_1}{x_2 - x_1}$</p> <p>oe</p> <p>oe</p> <p>correct equation of straight line through (4, 5), any non-zero gradient</p> <p>oe 3 term equation e.g. $5x + 2y = 30$</p> <p>5</p> <p>13</p>

10(i) $\frac{dy}{dx} = 6x^2 + 10x - 4$
 $6x^2 + 10x - 4 = 0$
 $2(3x^2 + 5x - 2) = 0$
 $(3x - 1)(x + 2) = 0$
 $x = \frac{1}{3}$ or $x = -2$
 $y = -\frac{19}{27}$ or $y = 12$

B1 1 term correct
B1 Completely correct (no +c)
M1* Sets their $\frac{dy}{dx} = 0$
M1 dep* Correct method to solve quadratic
A1
A1 **6** **SC** If A0 A0, one correct pair of values, spotted or from correct factorisation **www B1**

(ii) $-2 < x < \frac{1}{3}$

M1 Any inequality (or inequalities) involving both their x values from part (i)
A1 **2** Allow \leq and \geq

(iii) When $x = \frac{1}{2}$, $6x^2 + 10x - 4 = \frac{5}{2}$
 and $2x^3 + 5x^2 - 4x = -\frac{1}{2}$

M1 Substitute $x = \frac{1}{2}$ into their $\frac{dy}{dx}$
B1 Correct y coordinate

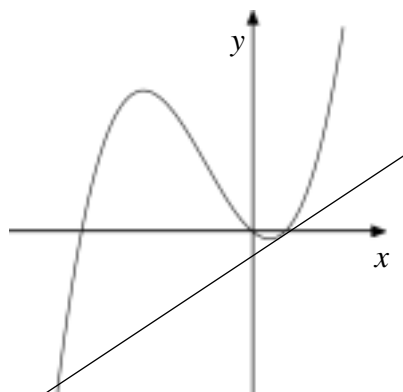
$y + \frac{1}{2} = \frac{5}{2}\left(x - \frac{1}{2}\right)$

M1 Correct equation of straight line using their values. Must use their $\frac{dy}{dx}$ value not e.g. the negative reciprocal

$10x - 4y - 7 = 0$

A1 Shows rearrangement to given equation
4 **CWO** throughout for A1

(iv)



B1 Sketch of a cubic with a tangent which meets it at 2 points only
B1 **2** +ve cubic with max/min points and line with +ve gradient as tangent to the curve to the right of the min
14

SC1
B1 Convincing algebra to show that the cubic $8x^3 + 20x^2 - 26x + 7 = 0$ factorises into $(2x - 1)(2x - 1)(x + 7)$
B1 Correct argument to say there are 2 distinct roots
SC2 B1 Recognising $y = 2.5x - 7/4$ is tangent from part (iii)
B1 As second B1 on main scheme