GCE

Mathematics

Unit 4732: Probability and Statistics 1

Advanced Subsidiary GCE

Mark Scheme for June 2014

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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Annotations and abbreviations

Annotation in scoris	Meaning
BP	Blank Page – this annotation must be used on all blank pages within an answer booklet (structured or
	unstructured) and on each page of an additional object where there is no candidate response.
✓and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
<u>۸</u>	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark	Meaning
scheme	
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
сао	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

Subject-specific Marking Instructions for GCE Mathematics (OCR) Statistics strand

a Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

The following types of marks are available.

Μ

С

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

f

Е

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

Candidates are expected to give numerical answers to an appropriate degree of accuracy. 3 significant figures may often be the norm for this, but this always needs to be considered in the context of the problem in hand. For example, in quoting probabilities from Normal tables, we generally expect *some* evidence of interpolation and so quotation to 4 decimal places will often be appropriate. But even this does not always apply – quotations of the standard critical points for significance tests such as 1.96, 1.645, 2.576 (maybe even 2.58 – but not 2.57) will commonly suffice, especially if the calculated value of a test statistic is nowhere near any of these values. Sensible discretion *must* be exercised in such cases.

Discretion must also be exercised in the case of small variations in the degree of accuracy to which an answer is given. For example, if 3 significant figures are expected (either because of an explicit instruction or because the general context of a problem demands it) but only 2 are given, loss of an accuracy ("A") mark is likely to be appropriate; but if 4 significant figures are given, this

g

h

should not normally be penalised. Likewise, answers which are slightly deviant from what is expected in a very minor manner (for example a Normal probability given, after an attempt at interpolation, as 0.6418 whereas 0.6417 was expected) should not be penalised. However, answers which are *grossly* over- or under-specified should normally result in the loss of a mark. This includes cases such as, for example, insistence that the value of a test statistic is (say) 2.128888446667 merely because that is the value that happened to come off the candidate's calculator. Note that this applies to answers that are given as final stages of calculations; intermediate working should usually be carried out, and quoted, to a greater degree of accuracy to avoid the danger of premature approximation.

The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

Genuine misreading (of numbers or symbols, occasionally even of text) occurs. If this results in the object and/or difficulty of the question being considerably changed, it is likely that all the marks for that question, or section of the question, will be lost. However, misreads are often such that the object and/or difficulty remain substantially unaltered; these cases are considered below.

The simple rule is that *all* method ("M") marks [and of course all independent ("B") marks] remain accessible but at least some accuracy ("A") marks do not. It is difficult to legislate in an overall sense beyond this global statement because misreads, even when the object and/or difficulty remains unchanged, can vary greatly in their effects. For example, a misread of 1.02 as 10.2 (perhaps as a quoted value of a sample mean) may well be catastrophic; whereas a misread of 1.6748 as 1.6746 may have so slight an effect as to be almost unnoticeable in the candidate's work.

A misread should normally attract *some* penalty, though this would often be only 1 mark and should rarely if ever be more than 2. Commonly in sections of questions where there is a numerical answer either at the end of the section or to be obtained and commented on (eg the value of a test statistic), this answer will have an "A" mark that may actually be designated as "cao" [correct answer only]. This should be interpreted *strictly* – if the misread has led to failure to obtain this value, then this "A" mark must be withheld even if all method marks have been earned. It will also often be the case that such a mark is implicitly "cao" even if not explicitly designated as such.

On the other hand, we commonly allow "fresh starts" within a question or part of question. For example, a follow-through of the candidate's value of a test statistic is generally allowed (and often explicitly stated as such within the marking scheme), so that the candidate may exhibit knowledge of how to compare it with a critical value and draw conclusions. Such "fresh starts" are not affected by any earlier misreads.

A misread may be of a symbol rather than a number – for example, an algebraic symbol in a mathematical expression. Such misreads are more likely to bring about a considerable change in the object and/or difficulty of the question; but, if they do not, they should be treated as far as possible in the same way as numerical misreads, *mutatis mutandis*. This also applied to misreads of text, which are fairly rare but can cause major problems in fair marking.

The situation regarding any particular cases that arise while you are marking for which you feel you need detailed guidance should be discussed with your Team Leader.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

S1 June 2014 Mark Scheme Final (without introduction)

Note: "(3 sfs)" means "answer which rounds to ... to 3 sfs". If correct ans seen to \geq 3sfs, ISW for later rounding Penalise over-rounding only once in paper.

C	uestic	on	Answer	Marks	Guidance		
1 1	(i)	on	Answer Median = 7.45 (m) IQR = 7.75 - 6.7 = 1.05 (m) allow 1.175 or 1.18 NOT 1.3	Marks B1 M1 A1	Guidan cao allow 7.775 – 6.6 or 77.5 – 67 or 77.75 – 66 or 7.8 – 6.5 even though this is an incorrect method or 78 – 65 allow 10.5 or 11.75 or 11.8 but <u>only</u> if med = 74.5	ce These pairs of values only, and subtract, for M1 eg 7.45, 7.75 - 6.7 = 1.05 B1M1A1 7.45, 7.775 - 6.6 = 1.175 B1M1A1 7.45, 7.8 - 6.5 = 1.3 B1M1A0 7.45, 7.7 - 6.5 = 1.2 B1M0A0 7.45, 77.5 - 67 = 10.5 B1M1A0	
				[3]		74.5, 77.5 - 67 = 10.5 $B0M1A1$ $74.5, 7.75 - 6.7 = 10.5$ $B0M1A1$ $74.5, 77.75 - 66 = 11.75$ $B0M1A1$ $7.45, 78 - 65 = 13$ $B1M1A0$ $74.5, 78 - 65 = 13$ $B0M1A0$ $74.5, 77 - 65 = 12$ $B0M0A0$	

1 (ii) One correct comment on size: B1. One correct comment on spread or shape: B1. The following are examples only. Ignore any working; mark the statements only. B1* B shorter overall B shorter overall B shorter overall NOT 8 6 means 6.8 (B) and 6.4 (A) allow just 8 6 means 6.8 (B) and 6.4 (A) allow just 8 6 means 6.8 (B) and 6.4 (A) allow just 8 6 means 6.8 (B) and 6.4 (A) allow just 8 6 means 6.8 (B) and 6.4 (A) allow sign and correct digit in one row is aligned with a 3 rd digit in one row is aligned with a 3 rd digit in and correct leaves, ignore order, aligned with a 3 rd digit in and correct leaves or incorrect leaves in aligned with a 3 rd digit in and correct leaves or incorrect leaves in aligned with a 3 rd digit in and correct leaves or incorrect leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in a single or aligned with a 3 rd digit in and correct leaves in a single or aligned with a 3 rd digit in and correct leaves in a single or aligned with a 3 rd digit in and correct leaves in a single or aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct leaves in aligned with a 3 rd digit in and correct aligned with a 3 rd digit in and coreverall NOT A higher han B <th>Question</th> <th>Answer</th> <th>Marks</th> <th>Guidan</th> <th>ICE</th>	Question	Answer	Marks	Guidan	ICE		
1 (iii) One correct comment on size: B1. One correct comment on spread or shape: B1. The following are examples only. Ignore any working; mark the statements only. B1 shorter overall B1 shorter overall B1 sha larger range or IQR or sd Ranges of both are similar A is nearer to normal A is negatively skewed A has a (unique) mode, or modal class or B1 B1 shorter overall B1 Shorter o	1 (ii)	5			Allow a separate diag with leaves to left of stem.		
Complete correct diag including order and key and alignmentB1depkey: eg 8/6/4 means 6.8 (B) and 6.4 (A) allow just 8 6 means 6.8 NOT 8 6 means 6.8 NOT 8 6 means 8.6If all digits are in correct rows a & correct key, award this mark EITHER: I. eg a 2 ^{md} digit in one row is aligned with a 3 rd digit in and 2. 1st, 3rd, 4th & 5 throws ar different lengths, eg because cossing out and replacement1(iii)One correct comment on size: B1. One correct comment on spread or shape: B1. The following are examples only. Ignore any working; mark the statements only.Allow "First set" or "Right" for A, "Second set" or "Left" for B.1(iii)One correct comment on size: B1. One correct comment on spread or shape: B1. The following are examples only. Ignore any working; mark the statements only.Allow "First set" or "Right" for A, "Second set" or "Left" for B.1(iii)One correct and replacement or spread or distributed B more spread out B has larger range or IQR or sd Ranges of both are similar A is nearer to normal A is nequi		$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	B1*	allow one omitted or extra or misplaced or	If only a separate diag is drawn, with leaves to <u>right</u> of stem: all correct including order, alignment and key: B1		
1(iii)One correct comment on size: B1. One correct comment on spread or shape: B1. The following are examples only. Ignore any working; mark the statements only.Allow "First set" or "Right" for A, "Second set" or "Left" for B.A higher overall A has more taller trees or fewer shorter A has higher median (mean, ave, medium)B shorter overall B has layer range or IQR or sd Ranges of both are similar A is negatively skewed A has a (unique) mode, or modal class orB shorter B1B shorter overall B1NOT A higher than B NOT B has shorter trees than A less evenly spread or distributed A has smaller range or IQR or sd Ranges of both are similarB1B less evenly spread or distributed A has a (unique) mode, or modal class orB1B1NOT any reference to outlier NOT any reference to mode or mostNOT any reference to indiv t Ignore any other reference to mode or mostNOT any reference to indivity NOT any reference to indivity		Complete correct diag including order and	Bldep	allow just 8 6 means 6.8 NOT 8 6 means 8.6	 eg a 2nd digit in one row is <u>clearly</u> aligned with a 3rd digit in another OR 1st, 3rd, 4th & 5th rows are <u>very</u> different lengths, eg because of 		
Ignore any working; mark the statements only.Allow "First set" or "Right" for A, "Second set" or "Left" for B.A higher overall A has more taller trees or fewer shorter A has higher median (mean, ave, medium)B shorter overall B has lower median (mean, ave, medium)NOT A higher than B NOT B has shorter trees than Allow just quoting the two m even if wrong, so long as med of A is gter than med of Similarly if quote IQRsB more evenly spread or distributed B more spread out B has larger range or IQR or sd Ranges of both are similar A is negatively skewed A has a (unique) mode, or modal class orB 1A less evenly spread or distributed A las a (unique) mode, or modal class orB1B nore evenly spread or distributed B more spread out B has larger range or IQR or sd Ranges of both are similar A is negatively skewed A has a (unique) mode, or modal class orB1A less evenly spread or distributed A las a (unique) mode, or modal class orB1B nore evenly spread or distributed B nore spread out B has larger range or IQR or sd Ranges of both are similar A is negatively skewed A has a (unique) mode, or modal class orB1A less evenly spread or distributed A las and unique mode, or modal class orB1B1Allow A's heights are more consistent Ignore any other reference to mode or mostNOT any reference to indiv t NOT two comments on size	1 (iii)	One correct comment on size: P1 One corr		ant on surroad or shonor D1. The following are of			
A higher <u>overall</u> A has more taller trees or fewer shorter A has higher median (mean, ave, medium)B shorter <u>overall</u> B has fewer taller trees or more shorter 	· (···)						
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A has a (unique) mode, or modal class or Ignore any other reference to mode or most NOT two comments on size				Not other comment about show			
		6			5		
l l neak: (B doesn't) common NOT two comments on sprey		peak; (B doesn't)		common	NOT two comments on spread		
		peak, (D doesn't)	[2]		eg highest on both is 8.5 B0		

Q	uestic	on	Answer	Marks	Guidance	
2	(a)		$(0^2 \times 0.3) + 2^2 \times 0.4 + 4^2 \times 0.3$	M1	last two terms correct. NOT eg \div 6 or \div 3	$2^{2} \times 0.3 + (0) + 2^{2} \times 0.3$ M2 1st or 3rd term correct M1
			-2^{2} or -4	M1	allow $-(any number)^2$, dep +ve result	
			= 2.4	A1 [3]		÷ 3 M0M0A0
2	(b)	(i)	2k + 3k + 4k + 5k = 1 oe	B1	or $14k = 1$ oe "= 1" is essential	NOT just $2 + 3 + 4 + 5 = 14$ so $k = \frac{1}{14}$
			$(k = \frac{1}{14} \mathbf{AG})$	[1]		Allow verification, eg stating that $\frac{2}{14} + \frac{3}{14} + \frac{4}{14} + \frac{5}{14} = 1$
2	(b)	(ii)	$\frac{2}{14}, \frac{3}{14}, \frac{4}{14}, \frac{5}{14}$ or $\frac{2}{14}, \frac{6}{14}, \frac{12}{14}, \frac{20}{14}$	B1	\geq 3 correct	2k, 6k,12k, 20k B1
			Σxp	M1	\geq 3 correct terms added	2k + 6k + 12k + 20k or $40k$ M1 $\div 4$ M0A0
			$=\frac{20}{7}$ or $2\frac{6}{7}$ or 2.86 (3 sf) oe, eg $\frac{40}{14}$	A1	SC $1 \times \frac{1}{14} + 2 \times \frac{2}{14} + 3 \times \frac{3}{14} + 4 \times \frac{4}{14} (=2.143)$	
				[3]	B0M1A0	

Q	uestio	n	Answer	Marks	Guidar	nce		
3	3 (i)		Use of 5 or 6 instead of 5.5 for last value of x: all M-marks can be scored, but no A-marks. (ans: 5 gives 2.32 and 1.23; 6 gives 2.39 and 1.40) Use of 5 and 6 instead of 5.5 (probably with freqs 19400/2) could lead to correct mean M1A1, but possibly M1M1A0 for sd.					
			$\frac{\Sigma fx}{\Sigma f} \text{ attempted} \qquad \left(= \frac{662000}{280900}\right)$	M1	3 terms of Σfx correct and $\div \Sigma f$ Allow incorrect Σf NOT Σx	$\div 5 \text{ or } \div 6 \text{ M0A0}$		
			$= 2.36 (3 \text{ sf})$ $\frac{\Sigma f x^2}{\Sigma f} \text{ attempted} \qquad (= \frac{2042350}{280900} =$	A1	3 terms of $\Sigma f x^2$ correct and $\div \Sigma f$ Allow incorrect Σf NOT Σx	$\frac{\Sigma f \left(x - \overline{x}\right)^2}{\Sigma f}$		
			7.270737)	M1		3 terms of num correct and $\div \Sigma f$ M2 (86900×1.36 ² +92500×0.36 ² +45000×0.64 ² +37100×1.64 ² +19400×3.1 ²), ($\frac{482210.64}{280900}$)		
						2 terms of num correct and $\div \Sigma f M1$		
			$-"2.36"^2$ (= 1.70 to 1.72, 3	MI	1	Allow incorrect Σf but NOT if $\Sigma f = \Sigma x$ NB $\sqrt{1}$ not requ'd for M1M1		
			sf)	M1	dep +ve result ÷ 5 or ÷ 6 M0M0A0			
			s.d. = 1.31 or 1.30 (3 sf)	A1	allow 1.3	Correct answer(s) without working score full marks		
				[5]				
3	(ii)		2	B1		Ignore working for both, even if		
			3	B1 [2]	allow $IQR = 3 - 1 = 2$, ie $UQ = 3$ implied	Incorrect NB 3, 2 B0B0 unless labelled correctly		

C	Question		Answer	Marks	Guidance				
4	4 If $\frac{2}{3}$ is inte		erpreted consistently as 0.6 or 0.66 or 0.67 or 0.7, max r		narks: (i)(a) M1M1A0 (i)(b) B0 (i)(c) B1ft B1ft (ii) B1M1M1A0				
4	(i)	(a)	Binomial seen or implied	M1	by use of table or ${}^{9}C_{6}$ or $(\frac{2}{3})^{p}(\frac{1}{3})^{q}(p+q=9)$	Eg 0.6228 seen			
			0.6228 - 0.3497	M1	${}^{9}C_{6}(\frac{1}{3})^{3}(\frac{2}{3})^{6}$				
			= 0.273 (3 sf)	A1	$\frac{1792}{6561}$				
				[3]					
4	(i)	(b)	0.3497 or 0.350 (3 sf)	B1	NB 0.3498 (from 0.6228 - 0.273) rounds to 0.350 so B1				
				[1]					
4	(i)	(c)	6	B1ft					
			2	B1ft		NB 2, 6 B0B0 unless labelled correctly			
				[2]					
4	(ii)		27 seen	B1	not necessarily in a statement				
			B(27, $\frac{2}{3}$) seen or implied	M1					
			$^{27}C_{18}(\frac{1}{3})^{9}(\frac{2}{3})^{18}$	M1	or attempt eg $P(X_1 = 1) \times P(X_2 = 8) \times P(X_3 = 9),$ $P(X_1 = 2) \times P(X_2 = 7) \times P(X_3 = 9),$	NB P($X_1 = 6$) × P($X_2 = 6$) × P($X_3 = 6$) = 0.273 ³ = 0.0203 M0M0A0			
					$P(X_1 = 3) \times P(X_2 = 6) \times P(X_3 = 9)$, etc ≥ 3 sets with $X_1 + X_2 + X_3 = 18$ (not nec'y added) M1	$\frac{55}{729}$ (= 0.0754) M0M0A0			
			= 0.161 (3 sf)	A1 [4]					

Q	uestic	on	Answer	Marks	Guidan	се
5	(i)		$S_{xx} = 20400 - \frac{360^2}{8} \qquad (= 4200)$ $S_{yy} = 6.88 - \frac{6.8^2}{8} \qquad (= 1.1)$			
			$S_{yy} = 6.88 - \frac{6.8^2}{8} \qquad (= 1.1)$ $S_{xy} = 241 - \frac{360 \times 6.8}{8} \qquad (= -65)$	M1	Correct sub in a correct S formula	
			$r = \frac{"-65"}{\sqrt{"4200" \times "1.1"}}$	M1	Correct sub in 3 correct <i>S</i> formulae and a correct <i>r</i> formula	
			= -0.956 (3 sf)	A1 [3]	Correct ans with no working M2A1	Ignore comment about $-1 < r < -0.9$
5	(ii)		eg As you move further away, prices drop	B1	High prices go with short distances oe	Both variables must be in context ; miles & £ enough
					Allow " <u>Strong</u> (or high or good or equiv) <u>neg</u> corr'n between price and distance"	Ignore all else, even if incorrect NOT just <u>neg</u> corr'n between price & dist
				[1]		
5	(iii)		None	B1 [1]		Ignore all else, even if incorrect
5	(iv)		$b = \frac{"-65"}{"4200"} \qquad (= -0.0154762)$	M1	ft their S_{xy} & S_{xx} from (i) for M-marks only	or fresh start correct method
			$Y - \frac{6.8}{8} = "-0.0154762"(x - \frac{360}{8}) $ oe	M1	or $a = \frac{6.8}{8} + "0.0154762" \times \frac{360}{8}$ oe	
			y = -0.0155x + 1.55 (3 sf) oe	A1	allow $y = -0.015x + 1.5$ (or figs which round to these)	Must have " <i>y</i> = "
			or $y = \frac{433}{280} - \frac{13}{840}x$ oe		(NOT $y = -0.016x + 1.6$ NOT $y = -0.02x + 1.5$)	Allow figures in equn which round to the correct figures to <u>either</u> 3 sf or 2 sf,
				[3]	NOT $y = -0.02x + 1.5$) Correct ans with no working M2A1	even if they result from arith errors.
5	(v)		Values of <i>x</i> are chosen beforehand or <i>x</i> is independent or controlled	B1	<i>x</i> is fixed or given or set or predetermined oe	Not "x is constant." Not just "y depends on x"
				[1]		Ignore all other, even if incorrect

C	Question		Answer	Marks	Guidan	се
6	(i)		654321	B1		
				[1]		
6	(ii)		$\Sigma d^2 = 0$ for first 6 teams	M1	May be implied by use of $\Sigma d^2 = 2$	
			$\Sigma d^2 = 2$	B1		
			$1 - \frac{6\sum d^2}{8(8^2 - 1)}$	M1	ft their $\Sigma d^2 (\neq 0)$	using ranks from (i) can score 2nd M1 only
			$=\frac{41}{42}$ or 0.976 (3 sf)	A1		
				[4]		
7	(i)		$\frac{n}{n+45} = \frac{5}{8} \text{ or } n: 45 = 5:3 \text{ or } \frac{3}{8}: 45 = \frac{5}{8}:n$	M1	$\frac{3F}{8} = 45 \& n = \frac{5}{8} \times F; 45 \times \frac{8}{3} - 45; 45 \times \frac{8}{3} \times \frac{5}{8}$	correct first step involving <i>n</i> or complete correct method for finding <i>n</i>
			n = 75	A1		
				[2]		
	(ii)		$\frac{45+"75"+52}{45+"75"+52+78}$ alone oe	M1	$1 - \frac{78}{45 + 75' + 52 + 78}$ oe or $\frac{250'' - 78}{250''}$ oe	$\frac{45+"75"}{"250"} + \frac{52+"75"}{"250"} - \frac{"75"}{"250"}$
					Completely correct method	or 0.48 + 0.508 - 0.48×0.508
			$=\frac{86}{125}$ or $\frac{172}{250}$ or 0.688 (3 sf) oe		ft their integer answer to (i)	
			$\frac{1}{125}$ or $\frac{1}{250}$ or 0.000 (5 sr) or	Alft	eg if their (i) is 28, ans 0.616 or $\frac{125}{203}$ M1A1ft	
				[2]		
7	(iii)	(a)	$\frac{10}{25} \times \frac{6}{24} \text{ or } \frac{6}{25} \times \frac{10}{24} \text{ seen } (\text{ or } \frac{2}{5} \times \frac{1}{4} \text{ or } \frac{6}{25} \times \frac{5}{12})$	M1	or $\frac{10}{25} \times \frac{6}{25} + \frac{6}{25} \times \frac{10}{25}$ or $\frac{10}{25} \times \frac{6}{25} \times 2$ oe	ie allow M1 if '2×' is omitted OR if 25 instead of 24, but not both errors
			oe		$\frac{{}^{10}C_1 \times {}^6C_1}{{}^{25}C_2} \text{ oe } \text{ or } \frac{10 \times 6}{300} \text{ oe}$	allow M1 for correct num or denom
			$\left(\frac{10}{25} \times \frac{6}{24} + \frac{6}{25} \times \frac{10}{24} \text{ or } \frac{10}{25} \times \frac{6}{24} \times 2\right)$			
			$=\frac{1}{5}$	A1		
				[2]		NB long methods <u>may</u> be correct, eg $(\frac{14}{25} \times \frac{10}{14}) \times (\frac{11}{24} \times \frac{6}{11})$ same as $\frac{10}{25} \times \frac{6}{24}$

Q	uestic	on	Answer	Marks	Guidan	се
7	(iii)	on (b)	FA + MC or FC + MA <u>Either</u> $\frac{4}{25} \times \frac{5}{24} \times 2$ <u>or</u> $\frac{10}{25} \times \frac{6}{24} \times 2$ NB ft their (iiia)	Marks M1	Guidan Allow $\frac{10}{25} \times \frac{6}{25} \times 2$ or $\frac{4}{25} \times \frac{5}{25} \times 2$ or $\frac{10}{25} \times \frac{6}{24} + \frac{4}{25} \times \frac{5}{24}$ or $\frac{10}{25} \times \frac{6}{25} + \frac{4}{25} \times \frac{5}{25}$ NB ft their (iii)(a)	ce ie allow 25 instead of 24 AND allow one case <u>with</u> × 2 or both cases <u>without</u> × 2 ie allow 25 <u>and</u> one of these two errors cf scheme for (iii)(a)
			$\left(\frac{4}{25} \times \frac{5}{24} \times 2 + \frac{10}{25} \times \frac{6}{24} \times 2 = \frac{1}{5} + \frac{1}{15}\right)$ = $\frac{4}{15}$ or 0.267 (3 sf)	A1	$\frac{{}^{10}C_1 \times {}^{6}C_1}{{}^{25}C_2} + \frac{{}^{4}C_1 \times {}^{5}C_1}{{}^{25}C_2} \text{ oe } \text{ or } \frac{60+20}{300} \text{ oe}$ cao	allow M1 if one of these fracts correct NB $^{25}C_2$ in denom NOT M1 , cf (iii)(a)
				[2]		NB see note on long methods in 7(iiia)
8	(i)		⁵ C ₂ oe seen anywhere or num= 10 alone $\frac{{}^{5}C_{2}}{{}^{8}C_{4}} \text{ oe or } \frac{{}^{5}C_{2} \times 4!}{{}^{8}P_{4}} \text{ oe all correct}$ $= \frac{1}{7} \text{ or } 0.143 (3 \text{ sf})$	M1 M1 A1	$\frac{1}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5} \text{or } \frac{20}{1680} \text{or } \frac{1}{84} \text{ oe seen}$ $\frac{1}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5} \times {}^{4}C_{2} \times 2 \text{ or } \frac{1}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5} \times 4! \div 2 \text{ oe}$ or $\frac{1}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5} \times 12$ oe all correct Correct ans scores M1M1A1 regardless of method	alone or × eg $\frac{2}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5}$ M1 $\frac{4}{8} \times \frac{3}{7} \times \frac{4}{6}$ oe all correct M2 NB $\frac{\text{incorrect}}{{}^{8}C_{4}}$ does not score
8	(ii)		$6! \times 2 \text{ alone or } 5! \times 6 \times 2 \text{ alone oe}$ $= 1440$	[3] M2 A1 [3]	method. M1 for 6! or $5! \times 6$ or ${}^{6}P_{5}$ or 720 seen NB 5! scores M0 unless $5! \times 6$ or $5! \times 12$	M1 for 7! × 2 alone NB 7! scores M0 unless 7! × 2 alone

		$6! \times 4 \text{ alone} \text{ or } 6! \times 2 \times 2 \text{ alone}$ $= 2880$ and 0.7 are interchanged consistently through al 0.3 is calculated incorrectly (eg 0.6 or 0.66 or $\frac{2}{3}$ $0.7^4 \times 0.3 \text{ alone}$ $= 0.0720 (3 \text{ sf}) \text{ or } \frac{7203}{100000} \text{ oe}$	·) consistent		5!: M0 unless 5!×6 or 5!×12 or 5!×24 are available on ft, so long as 0 < ans < 1.
9 9	If 1 – 0 (i)	and 0.7 are interchanged consistently through al 0.3 is calculated incorrectly (eg 0.6 or 0.66 or $\frac{2}{3}$ 0.7 ⁴ × 0.3 alone	[3] l four parts, ·) consistent M1		are available on ft, so long as $0 < ans < 1$.
9 9	If 1 – 0 (i)	0.3 is calculated incorrectly (eg 0.6 or 0.66 or $\frac{2}{3}$ 0.7 ⁴ × 0.3 alone	l four parts,) consistent M1		are available on ft, so long as $0 < ans < 1$.
9	(i)	$0.7^4 \times 0.3$ alone	M1	ly, lose the A-mark in (i) but all other marks	are available on ft, so long as $0 < ans < 1$.
9					
	(ii)	$= 0.0720 (3 \text{ sf}) \text{ or } \frac{7203}{100000} \text{ oe}$			
	(ii)		A1	allow 0.072	
	(ii)	2 2	[2]		
9		$(0.7 + 0.7^2 + 0.7^3) \times 0.3$	M2	M1 for 1 term omitted, wrong or extra. must add terms, not mult.	$(1-0.7^4) - 0.3 \text{ or } 0.7599 - 0.3 \text{ M2}$ $(1-0.7^4) - \dots \text{ or } 1-0.3 - \dots \text{ M1}$ $0.7599 - \dots \text{ or } 0.7 - \dots \text{ M1}$ Just $1-0.7^4$ or $1-0.3$: M0 $(1+0.7+0.7^2+0.7^3) \times 0.3 - 0.3 \text{ M2}$ 1 term omitted, wrong or extra M1
9		$= 0.4599 \text{ or } 0.460 \text{ (3sf) or } \frac{4599}{10000} \text{ oe}$	A1	Allow 0.46	
	(iii)	$1 - 0.7^{6}$	[3] M2	M1 for 0.7^6 alone or $1 - 0.7^5$ (= 0.832)	$0.3(1+0.7+0.7^2+0.7^3+0.7^4+0.7^5)$ M2
	(11)	1-0.7	IVI2	or $1 - 0.7^7$ (= 0.918)	or (ii) + $0.3(1 + 0.7 + 0.7 + 0.7 + 0.7 + 0.7)$ M2 or (ii) + $0.3(1 + 0.7^4 + 0.7^5)$ M2 or (i) + (ii) + $0.3(1 + 0.7^5)$ M2 one term omitted or extra: M1 must add terms, not mult.
		= 0.882 (3 sf)	A1		NB ans 0.832 might be M1M0A0 from omitting last term. Could be, eg, their (ii) $+$ 0.3(1 $+$ 0.7 ⁴) correct working, but subtr from 1: M1

C	Question		Answer	Marks	Guidance	
9	(iv)		$(1 - "0.882")^2 \times "0.882"$ oe	M1	or $(0.7^6)^2 \times (1 - 0.7^6)$ or $0.1176^2 \times (1 - 0.1176)$	Not $0.7^2 \times 0.3$
					or $(0.7^6)^2$ × their "0.882"	
					or $0.3(0.7^{12}+(0.7^{13}+0.7^{14}++0.7^{17}))$	Completely correct method
			= 0.0122 (3 sf)	A1ft	allow 0.0123	ft their "0.882" except if 0.3 or 0.7
				[2]		

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