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1	(•)		D 1	
I	(1)	AD, EB, CF	BI	For these three directed arcs and no
		8+2+7	MI	others
		= 17 litres per second	AI	$8 + 7 + 0$ or $8 + 7 - 2$ seen \Rightarrow M1, A0
				For 17
	(11)			
				A (11 1
			MI	Accept all arrows reversed
			MII	
		r r r r r r r		For no more than three errors
			Δ1	Tor no more than three errors
			111	
		6		For a correct labelling
		C ¹ F		
		-		
	(iii)	SCEBDT	B1	For this path only
	()			1 5
		$A \longrightarrow D$		
		5060 60 322 07	B1	For a correct labelling
		$/$ \times \setminus		
		4		
		$S \qquad B \stackrel{2}{\sim} E \qquad T$		
		0 8 2 0 6 0		
	(:)	$\frac{C}{C} = \frac{F}{F}$	D1	Ear a this put on the put $\{S\}$ $\{A, B, C, D\}$
	(\mathbf{IV})	Cut $\{3, A, B, C, D, E, F\}$ $\{I\} = 13$	DI	For a time cut of the cut $\{S\}$ $\{A, B, C, D, E, E, T\}$ in any form or for 'no more can
				T, T ,
		Diagram in (iii) shows a flow of 13	B1	S', or equivalent.
		litres/second	21	For flow shown = 13 or max flow > 13 >
				min cut
				(but NOT just stating max flow = min
				cut)
]	Value 13 given in question
	(v)	5		
		5		
			B1	For showing this flow, or excess
				capacities and potential backflows
		$S \setminus B \times E = I$		equivalent to this
		\backslash \land \land		
		6 6		
		C F		
		6		
		Max flow is 11 litres per second	B1	
			_	For 11 litres per second (with units)
		Cut $\{S, C, E, F\}$ $\{A, B, D, T\} = 11$	B1	
				For cut or a convincing explanation in
			12	words

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2	(i)		1	A			->	1		
		в • 2								
									B1	For a correct bipartite graph
		D 4								
	(ii)	Den	ny ca	nnot	have a	a song	that	she has	B1	For this reasoning
		chos	sen							
	(iii)	5.0	2 D						MI	Follow through their bipartite graph, if
		5 C	3 D						INI I	possible For this path (or in reverse) not longer path
		A-1, B-2, C-5, D-3, E-4							A1	- if shown on diagram, path must be obvious For this matching, not alternative
	(iv)	A-2,	, В-4,	C-5,	D-1,	E-3			B1	For a different matching from their bipartite graph
	(v)	Hun	garia	n alg	orithm	n finds	mini	mum cost		
		allo	cation	, nee	d to su	ubtrac	t each	score from	BI	For a valid reference to
		Dun	$\frac{1}{2}$	ow is	naxim	nsing ed to i	11110 I make	ninimising. a square	R1	maximising/minimising
		mati	ix.	0 10	sneed		mare	a square		For 'make it square' or equivalent
	(vi)		F	G	Н	J	Κ			
		А	6	1	3	10	3			
		B	4	2	7	2	10			
		C	3	6 4	5	8	3			
		D X	4	4	8	5	9		R1	For setting up initial matrix as described
		21	U	U	0	U	0		DI	i or setting up initial matrix as described
		Reduce rows								
		5 0 2 9 2				M1	For reducing rows (to give a 0 in each row)			
			2	0	5	0	8			
			0	3 1	2	5	0			
			1	1	0	0	0		A1	For correct reduced matrix (cao)
		0 0 0 0 0					Ū			
		Cov	er 0's	usin	g four	lines				
			5	0	2	9	2			
			2	0	5	0	8			
						6		M1	For covering 0's using minimum number of	
			0	0	0	0	0		IVI I	lines
		Augment								
		$\begin{array}{cccccccccccccccccccccccccccccccccccc$				1				
						7		A1		
		$\begin{array}{cccccccccccccccccccccccccccccccccccc$					For correct augmented matrix (cao)			
		0 1 0 1 0				0				
		Complete matching								
		A-G, B-J, C-K. D-F								
			,	, -	,				13	For correct matching (listed)

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3	(i)	D(20)		Durations not necessary
		A(8) $F(12)$ $G(2)$ $N(12)$	M1	For a correct activity network
			A1	For directions indicated correctly
		C(12) F(4)		
	(ii)	⁸⁸ D(20) ^{28 30}		Follow through their network if possible,
		A(8) G(2)		provided not significantly simpler, for the passes
		$\begin{array}{c} 0 \\ \hline \\ B_{8}(4)_{8} \\ \hline \\ E(12)_{20} \\ \hline \\ H(12)_{2} \\ \hline \\ H(12)_{2} \\ \hline \\ \\ \\ H(12)_{2} \\ \hline \\ \\ \\ H(12)_{2} \\ \hline \\ \\ \\ H(12)_{2} \\ \hline \\ \\ \\ H(12)_{2} \\ \hline \\ \\ H(12)_{2} \\ \\ \\ \\ H(12)_{2} \\ \\ \\ \\ H(12)_{2} \\ \\ \\ \\ \\ \\ H(12)_{2} \\ \\ \\ \\ H(12)_{2} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	M1 A1	For forward pass
		C(12) F(4)	M1	For forward pass correct
			A1	For backwards pass For backwards pass correct
		Minimum completion time = 32 minutes Critical activities A F H	B1 B1	For 32 stated not just on diagram (cao)
	(:::	······		For A, E, H stated (not just on diagram (cao)
	(III)			ronow unough then start times it possible
			M1	For structure of chart correct, activities may
		C F		be collected together or on individual rows
		B	A1	For non-critical activities correct (floats optional)
		A E H	A1	
				For critical activities correct
		0 4 8 12 16 20 24 28 32 time(mins)		
	(iv)	e.g.		
		Time John Kerry $0-4$ A		
		$\begin{array}{c ccc} \underline{4-8} & \underline{A} & \underline{B} \\ \hline 8-12 & C & C \end{array}$		
		12 – 16 C C 16 – 20 C C	M1	For structure of schedule correct and all activities
		20 - 24 D D 24 - 28 D D		shown (with H appearing twice)
		28 - 32 D D 32 - 36 D D	Δ1	
		32 = 30 D D 36 = 40 D D 40 = 44 E E	211	For activities A, B, C, D, E and F correct:
		40 - 44 E E 44 - 48 E E		 A=6, B=4, C=12, D=20, E=12, F=4; D after A; E after A, B; F after A, B, C;
		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	A1	• C, D and E done by J and K at same time
		$\begin{array}{cccccccc} 56 - 60 & H & H \\ 60 - 64 & H & H \end{array}$		 For activities G and H correct G = 2 (may see 4), H = 12
		$\begin{array}{cccccccccccccccccccccccccccccccccccc$		• G, H after (D), E, F (not alongside F) • H done by each of L and K
			14	 Total time taken = 70 (minutes)

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4	(•)						1	
4	(1)	stage	state	action	working	maximum		
		1	0	0	4	*		
			1	0	4	*	M1	For structure of table correct
		2	0	0	4 + 4= 8	*	A1	For stage and state columns correct
			1		5 + 4 = 9	*	A1	For action values correct
			 	1	0 + 4 = 10	*		
			2	0	7 + 4 = 11 5 + 4 = 0		M1	For all calculations correct for stages 1
			3	1	5 + 4= 9 6 + 4= 10	*		and 2
		3	0	1	8+10= 18	*		(may be seen as an addition or the result
		5	U	3	6+10=16		Δ1	and may be shown in final column)
			1	0	7+ 9=16		711	Eor subortimal maxima identified
				2	6+11= 17	*		
			2	0	7+ 9=16			(many harding light from most story)
				2	6+11=17			(may be implied from next stage)
				3	8+10= 18	*		
		4	0	0	5+18=23		M1	
			4	1	8+17=25	*		
			1	0	/+18= 25	<u>^</u>	A1	For correct calculations for stage 3
		F	0	2	0+10=23			(follow through from stage 2, if possible)
		Э	0	0	0+25=31 8+25- 33	*		For suboptimal maxima correct (ft their
		_		I	0+23- 33		M1	totals)
								(may be implied from next stage)
							A1	For correct calculations for stages 4 and 5
							111	(follow through from stage 3)
								(Tonow through from stage 5)
		Derete	(0.0)	(1.0)	(0 , 1)	(2,0) $(4,1)$	D1	Coloralations comment for antime table
		Roule	(0;0)	-(1;0)	-(2;1)-((3;0) – (4;1)		Calculations correct for entire table
		- (5;0)		<u> </u>		BI	
		Giles will be able to see 33 plants ii) Minimax						
								(cao) or in reverse
								For 33 (cao)
	(ii)							For 'minimax'
		Route: $(0;0) - (1;0) - (2;3) - (3;0) - (4;0)$ - $(5;0)$ <u>Or</u> $(0;0) - (1;1) - (2;3) - (3;0) - (4;0)$ - $(5;0)$ At stage 5 all paths have at least 6 plants					M1	For a path with at most one path > 6
							A1	plants
							B1	For either correct path
								Or stage 3 or any equivalent argument in
							15	words
		At stage 5 all paths have at least 6 plants						WOLUS

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5	(i)	What one player wins the other loses	B1	For a statement equivalent to 'total won each game is zero'
	(ii)	S and T: $3 > -2$ but $-2 < 1$ (or $-1 < 2$) S and U: $3 > 1$ (or $-1 > -2$) but $-2 < 3$	M1	For considering differences, showing inequalities or considering rows where
		T and U: -2 < 1 (or 1 < 5) but 2 > -2	A1	For a valid explanation
		<i>D</i> and <i>E</i> : $3 > -2$ but $-2 < 1$ (or $1 < 3$) <i>D</i> and <i>F</i> : $3 > -1$ (or $1 > -2$) but $-2 < 2$ <i>E</i> and <i>F</i> : $2 < -1$ (or $1 < 2$) but $2 > -2$	M1	For considering differences, showing inequalities or considering columns where
		<i>E</i> and <i>F</i> : $-2 < -1$ (or $1 < 2$) but $5 > -2$	A1	For a valid explanation
	(iii)	Row minima are -2, -2, -2 \Rightarrow row maximin = -2 Col maxima are 3, 3, 2 \Rightarrow col minimax = 2 $2 \neq -2 \Rightarrow$ not stable	M1 M1 A1	For identifying -2 correctly <u>or</u> identifying all rows For identifying 2 correctly <u>or</u> identifying col <i>F</i> For a valid explanation, or equivalent in
	(iv)	So that for $p_1, p_2, p_3 \ge 0$ we will have $m \ge 0$	B1	words For explaining that this will make $m \ge 0$ (not sufficient to just say that we need to make all the entries non-negative)
	(v)	If Colin plays <i>D</i> , with the augmented payoffs Rhoda will expect to win $5p_1+0p_2+3p_3$, and similarly for when Colin chooses <i>E</i> or <i>F</i> <i>m</i> is the minimum of the augmented	B1 B1	For explaining any of the three expressions on the right hand side of the inequalities For explaining why $m \le$ each expression
	(vi)	^m 3	M1	For a graph of <i>m</i> against p_1 (or <i>m</i> against p_2) with three lines
			A1	For lines (0,0)-(1,5), (0,3)-(1,0), (0,4)-(1,1) or equivalent
		P_1 0 $5p_1 = 3(1-p_1) \Rightarrow p_1 = \frac{3}{8} \text{ (and } p_2 = \frac{5}{8} \text{)}$	B1	For convincingly showing how values were obtained (ie identifying $5p_1 = 3p_2$ or equivalent Or reading off from correct point on graph) Note: $p_1 = \frac{3}{8}$ and $p_2 = \frac{5}{8}$ is given in the question
	(vii)	-0.125	B1	For $-\frac{1}{8}$, or equivalent (cao)
-	(viii)	e.g. Toss the coin three times to give eight equally likely possible outcomes, allocate three outcomes to 'play S' and five to 'play	M1 A1	For a specific example, or a description of any valid method eg HHT, HTH, THH $\rightarrow S$ all other outcomes
		T° In the long run she expects to lose $\frac{1}{8}$ per game	B1 18	$\rightarrow T$ For 'lose (at least) $\frac{1}{8}$ per game'