

Version 1.0 0107



**General Certificate of Education**

**Mathematics 6360**

**MS2B      Statistics 2**

**Mark Scheme**

*2007 examination - January series*

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available to download from the AQA Website: [www.aqa.org.uk](http://www.aqa.org.uk)

Copyright © 2007 AQA and its licensors. All rights reserved.

#### COPYRIGHT

AQA retains the copyright on all its publications. However, registered centres for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to centres to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Set and published by the Assessment and Qualifications Alliance.

## Key to mark scheme and abbreviations used in marking

M	mark is for method		
m or dM	mark is dependent on one or more M marks and is for method		
A	mark is dependent on M or m marks and is for accuracy		
B	mark is independent of M or m marks and is for method and accuracy		
E	mark is for explanation		
√ or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
-x EE	deduct x marks for each error	G	graph
NMS	no method shown	C	candidate
PI	possibly implied	Sf	significant figure(s)
SCA	substantially correct approach	Dp	decimal place(s)

### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

**Otherwise we require evidence of a correct method for any marks to be awarded.**

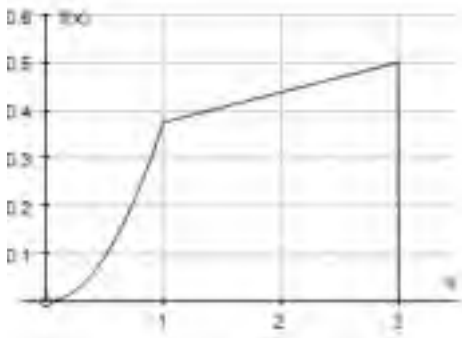
**MS2B**

Q	Solution	Marks	Total	Comments
<b>1</b>	$\bar{x} = 39.5 \quad s = 4.84 \quad (s^2 = 23.4)$ $t_{\text{crit}} = 2.365$ 95% CI for $\mu$ $= \bar{x} \pm t_{\text{crit}} \times \frac{s}{\sqrt{n}}$ $= 39.5 \pm 2.365 \times \frac{4.84}{\sqrt{8}}$ $= 39.5 \pm 4.05$ $= (35.5, 43.5)$	B1B1 B1   M1   A1✓	5	$\sigma = 4.53 \quad (\sigma^2 = 20.5)$      $39.5 \pm 2.365 \times \frac{4.53}{\sqrt{7}}$
	<b>Total</b>		<b>5</b>	
<b>2(a)(i)</b>	$P(A = 4) = \frac{e^{-3.5} \times (3.5)^4}{4!} = 0.189$	M1A1	2	
<b>(ii)</b>	$P(B \leq 6) = 0.762$	B1	1	
<b>(iii)</b>	$T = A + B \sim \text{Po}(8.5)$  $P(T \text{ fewer than } 10) = P(T < 10)$ $= P(T \leq 9)$ $= 0.653$	M1 M1 A1	3	Use of Po (8.5) $T \leq 9$ attempted CAO
<b>(b)</b>	$X \sim B(5, 0.653)$  $P(X \geq 4) = \binom{5}{4} (0.653)^4 (0.347)$ $\quad \quad \quad + (0.653)^5$ $= 0.31547 + 0.11873$ $= 0.434$	B1    M1  A1✓	3	$X \sim B(5, \text{their } p)$      On their $p$ from (a)(iii)
<b>(c)(i)</b>	$\bar{x} = 9.2$ $s^2 = 9.29$	B1 B1	2	$\sigma^2 = 8.36$
<b>(ii)</b>	Mean and variance have similar values which suggests that Poisson distribution may be appropriate	B1✓ B1✓	2	
	<b>Total</b>		<b>13</b>	

**MS2B (cont)**

Q	Solution	Marks	Total	Comments
<b>3</b>	$\bar{x} = 83.5$	B1		
	$s^2 = \frac{1}{99}(15321) = 154.76$			$(154 < s^2 \leq 155)$
	$s = 12.44$	B1		$(12.4 \leq s \leq 12.45)$
	$H_0 : \mu = 85.9$			
	$H_1 : \mu \neq 85.9$	B1		
	Under $H_0$ , $\bar{X} \sim N\left(85.9, \frac{(12.44^2)}{100}\right)$			
$z_{\text{crit}} = \pm 1.96$	B1		$z = 1.96 + 2$ tail test used	
$z = \frac{83.5 - 85.9}{12.44/\sqrt{10}} = -1.929$	M1		$\frac{(\text{their } \bar{x}) - 85.9}{(\text{their } s)/10}$	
	A1			
accept $H_0$ , reject the claim	A1✓			AWFW $-1.94$ to $1.92$ On their $z$
Insufficient evidence to suggest that the mean has changed from 85.9 at the 5% level of significance.	E1✓		8	
	<b>Total</b>		<b>8</b>	
<b>4(a)</b>	$\sum p = 1$ $k = 1 - (0.01 + 0.05 + 0.14 + 0.30 + 0.12)$ $k = 0.38$	B1	1	
<b>(b)(i)</b>	$E(X) = \sum_{\text{all } x} x P(X = x) = 4.35$	B1	1	$\frac{87}{20}$
<b>(ii)</b>	$\text{Var}(X) = \sum_{\text{all } x} x^2 P(X = x) - \mu^2$	M1		$E(X^2)$ attempted
	$= 20.09 - 18.9225$	M1		$\sum x^2 P(X = x) - \mu^2$
	$= 1.1675$	A1	3	$\frac{467}{400}$ (AWFW 1.16 – 1.17)
<b>(c)(i)</b>	$E(Y) = 5E(X) + 2$ $= 5 \times 4.35 + 2$ $= 23.75$	M1	1	Their (b)(i) $\times 5 + 2$
	<b>(ii)</b> $\text{Var}(Y) = 25\text{Var}(X)$ $= 29.1875$ Standard deviation = 5.40	M1		Their (b)(ii) $\times 25$
		m1 A1	3	$\sqrt{\quad}$ (5.40 – 5.41)
	<b>Total</b>		<b>9</b>	

**MS2B (cont)**

Q	Solution	Marks	Total	Comments
<p><b>5(a)</b></p>	<p><math>H_0 : \mu = 30</math>  <math>H_1 : \mu &gt; 30</math>  <math>\bar{x} = 33.5</math> and <math>s = 4.25</math> (<math>s^2 = 18.06</math>)                      Under <math>H_0</math> <math>\bar{X} \sim N\left(30, \frac{(4.25^2)}{10}\right)</math>  <math>t = \frac{33.5 - 30}{4.25/\sqrt{10}} = 2.60</math>  <math>t_{\text{crit}} = 2.821</math>                      do not reject <math>H_0</math>                      Insufficient evidence at the 1% level of significance that Jasmine's teacher is underestimating the time that it takes to complete the homework assignments.</p>	<p>B1                      B1B1                        M1A1                      B1                        E1✓</p>	<p>7</p>	<p><math>\sigma = 4.03</math> (<math>\sigma^2 = 16.25</math>)                        ↓  <math>\frac{33.5 - 30}{4.03/\sqrt{9}}</math> (2.6 - 2.61)</p>
<p><b>(b)</b></p>	<p>Times are Normally distributed</p>	<p>B1</p>	<p>1</p>	
<b>Total</b>			<b>8</b>	
<p><b>6(a)</b></p>		<p>B1                      B1                      B1</p>	<p>3</p>	<p>for curve                      for line                      for axes</p>
<p><b>(b)</b></p>	<p><math>P(T \geq 1) = \frac{1}{2} \times \frac{7}{8} \times 2 = \frac{7}{8}</math></p>	<p>M1A1</p>	<p>2</p>	<p>OE</p>

**MS2B (cont)**

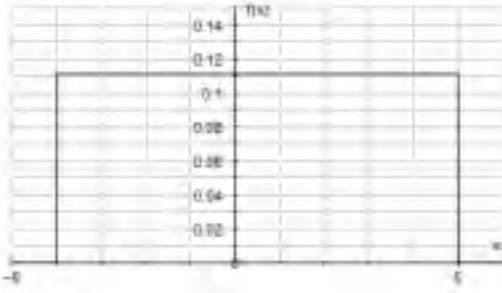
Q	Solution	Marks	Total	Comments
<p><b>6(c)(i)</b></p>	<p>For <math>1 \leq t \leq 3</math></p> $\int_1^t \frac{1}{16}(t+5)dt = \left[ \frac{1}{32}t^2 + \frac{5}{16}t \right]_1^t$ $F(1) = \frac{1}{8}$ $F(t) = \frac{1}{8} + \frac{1}{32}t^2 + \frac{5}{16}t - \frac{11}{32}$ $F(t) = \frac{1}{32}(t^2 + 10t - 7)$ <p><b>Alternative:</b></p> $\int \frac{1}{16}(t+5)dt$ $= \frac{1}{16} \left( \frac{1}{2}t^2 + 5t + c \right)$ $F(1) = \frac{1}{8}$ $\Rightarrow c = -3.5$ $F(t) = \frac{1}{32}(t^2 + 10t - 7)$	<p>M1A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>(M1) (A1)</p> <p>(B1)</p> <p>(M1)</p> <p>(A1)</p> <p>M1</p> <p>A1</p> <p>m1</p> <p>A1</p>	<p>5</p> <p>4</p>	<p>Use of: <math>F(t) = F(1) + \int_1^t \frac{1}{16}(t+5)dt</math></p> <p><b>AG</b></p> <p>(or any valid method)</p> <p>(1.9282)</p>
	<b>Total</b>		<b>14</b>	

**MS2B (cont)**

Q	Solution	Marks	Total	Comments																																																																
<b>7(a)</b>	$H_0$ : No association between the performances at KS3 and GCE	B1																																																																		
	<table border="1"> <thead> <tr> <th><math>O_i</math></th> <th><math>E_i</math></th> <th><math>O_i - E_i</math></th> <th><math>X^2</math></th> </tr> </thead> <tbody> <tr> <td>60</td> <td>63.55</td> <td>-3.55</td> <td>0.1983</td> </tr> <tr> <td>55</td> <td>44.64</td> <td>10.36</td> <td>2.4043</td> </tr> <tr> <td>40</td> <td>46.81</td> <td>-6.81</td> <td>0.9907</td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>55</td> <td>51.25</td> <td>3.75</td> <td>0.2744</td> </tr> <tr> <td>32</td> <td>36.00</td> <td>-4.00</td> <td>0.4444</td> </tr> <tr> <td>38</td> <td>37.75</td> <td>0.25</td> <td>0.0017</td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>47</td> <td>46.33</td> <td>0.67</td> <td>0.0097</td> </tr> <tr> <td>31</td> <td>32.54</td> <td>-1.54</td> <td>0.0733</td> </tr> <tr> <td>35</td> <td>34.13</td> <td>0.87</td> <td>0.0222</td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>43</td> <td>43.87</td> <td>-0.87</td> <td>0.0173</td> </tr> <tr> <td>26</td> <td>30.82</td> <td>-4.82</td> <td>0.7527</td> </tr> <tr> <td>38</td> <td>32.31</td> <td>5.69</td> <td>1.0005</td> </tr> </tbody> </table>	$O_i$	$E_i$	$O_i - E_i$	$X^2$	60	63.55	-3.55	0.1983	55	44.64	10.36	2.4043	40	46.81	-6.81	0.9907					55	51.25	3.75	0.2744	32	36.00	-4.00	0.4444	38	37.75	0.25	0.0017					47	46.33	0.67	0.0097	31	32.54	-1.54	0.0733	35	34.13	0.87	0.0222					43	43.87	-0.87	0.0173	26	30.82	-4.82	0.7527	38	32.31	5.69	1.0005	M1 M1 M1 M1 M1		$E_i$ $O_i - E_i$ $(O_i - E_i)^2 / E_i$ $\Sigma$
	$O_i$	$E_i$	$O_i - E_i$	$X^2$																																																																
	60	63.55	-3.55	0.1983																																																																
	55	44.64	10.36	2.4043																																																																
	40	46.81	-6.81	0.9907																																																																
	55	51.25	3.75	0.2744																																																																
	32	36.00	-4.00	0.4444																																																																
	38	37.75	0.25	0.0017																																																																
	47	46.33	0.67	0.0097																																																																
	31	32.54	-1.54	0.0733																																																																
	35	34.13	0.87	0.0222																																																																
43	43.87	-0.87	0.0173																																																																	
26	30.82	-4.82	0.7527																																																																	
38	32.31	5.69	1.0005																																																																	
	$X^2 = 6.1897$	A1		AWFW 6.05 – 6.35																																																																
	$\nu = 3 \times 2 = 6 \Rightarrow \chi_{90\%}^2 = 10.645$	B1B1✓		on their $\nu$																																																																
	Do not reject $H_0$ No evidence to suggest an association between KS3 results and GCE grades at 10% level of significance.	E1✓	9																																																																	
<b>(b)</b>	More of the students achieving level 7 at KS3 gain grade A's at GCE than expected.	E1	1																																																																	
	<b>Total</b>		<b>10</b>																																																																	



**MS2B (cont)**

Q	Solution	Marks	Total	Comments
8(a)	$f(x) = \begin{cases} \frac{1}{9} & -4 \leq x \leq 5 \\ 0 & \text{otherwise} \end{cases}$	M1 A1	2	
(b)		B1  B1	2	horizontal line from -4 to 5  for drawn at $\frac{1}{9}$
(c)	$P(X > 2) = \frac{1}{9} \times 3$ $= \frac{1}{3}$	M1  A1	2	$F(5) - F(2)$ $= 1 - \frac{2}{3}$ $= \frac{1}{3}$
(d)	$\text{Mean} = \frac{1}{2}$ $\text{Variance} = \frac{1}{12} \times 81$ $= 6.75$	B1  B1	2	
	<b>Total</b>		<b>8</b>	
	<b>TOTAL</b>		<b>75</b>	