

## ADVANCED SUBSIDIARY GCE UNIT MATHEMATICS

Core Mathematics 1 TUESDAY 16 JANUARY 2007

Morning

4721/01

Time: 1 hour 30 minutes

Additional Materials: Answer Booklet (8 pages) List of Formulae (MF1)

## INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer **all** the questions.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- You are not permitted to use a calculator in this paper.

## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- The total number of marks for this paper is 72.

## ADVICE TO CANDIDATES

- Read each question carefully and make sure you know what you have to do before starting your answer.
- You are reminded of the need for clear presentation in your answers.



You are not allowed to use a calculator in this paper.

This document consists of **4** printed pages.

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1 Express 
$$\frac{5}{2-\sqrt{3}}$$
 in the form  $a + b\sqrt{3}$ , where a and b are integers. [3]

2 Evaluate

(i) 
$$6^0$$
, [1]

(ii) 
$$2^{-1} \times 32^{\frac{4}{5}}$$
. [3]

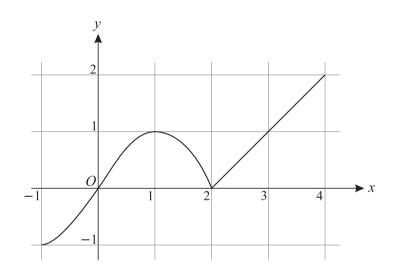
**3** Solve the inequalities

(i) 
$$3(x-5) \le 24$$
, [2]

(ii) 
$$5x^2 - 2 > 78$$
. [3]

4 Solve the equation  $x^{\frac{2}{3}} + 3x^{\frac{1}{3}} - 10 = 0.$ 





The graph of y = f(x) for  $-1 \le x \le 4$  is shown above.

- (i) Sketch the graph of y = -f(x) for  $-1 \le x \le 4$ .
- (ii) The point P(1, 1) on y = f(x) is transformed to the point Q on y = 3f(x). State the coordinates of Q. [2]
- (iii) Describe the transformation which transforms the graph of y = f(x) to the graph of y = f(x + 2). [2]
- 6 (i) Express  $2x^2 24x + 80$  in the form  $a(x-b)^2 + c$ . [4]
  - (ii) State the equation of the line of symmetry of the curve  $y = 2x^2 24x + 80$ . [1]
  - (iii) State the equation of the tangent to the curve  $y = 2x^2 24x + 80$  at its minimum point. [1]

[2]

[5]

3

7 Find  $\frac{dy}{dx}$  in each of the following cases.

(i) 
$$y = 5x + 3$$
 [1]

(ii) 
$$y = \frac{2}{x^2}$$
 [3]

(iii) 
$$y = (2x+1)(5x-7)$$
 [4]

8 (i) Find the coordinates of the stationary points of the curve  $y = 27 + 9x - 3x^2 - x^3$ . [6]

- (ii) Determine, in each case, whether the stationary point is a maximum or minimum point. [3]
- (iii) Hence state the set of values of x for which  $27 + 9x 3x^2 x^3$  is an increasing function. [2]
- 9 A is the point (2, 7) and B is the point (-1, -2).
  - (i) Find the equation of the line through *A* parallel to the line y = 4x 5, giving your answer in the form y = mx + c. [3]
  - (ii) Calculate the length of *AB*, giving your answer in simplified surd form. [3]
  - (iii) Find the equation of the line which passes through the mid-point of AB and which is perpendicular to AB. Give your answer in the form ax + by + c = 0, where a, b and c are integers. [6]
- 10 A circle has equation  $x^2 + y^2 + 2x 4y 8 = 0$ .
  - (i) Find the centre and radius of the circle. [3]
  - (ii) The circle passes through the point (-3, k), where k < 0. Find the value of k. [3]
  - (iii) Find the coordinates of the points where the circle meets the line with equation x + y = 6. [6]

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