General Certificate of Education June 2008 Advanced Subsidiary Examination

MS/SS1B



MATHEMATICS
Unit Statistics 1B

STATISTICS
Unit Statistics 1B

Wednesday 21 May 2008 1.30 pm to 3.00 pm

For this paper you must have:

- an 8-page answer book
- the blue AQA booklet of formulae and statistical tables
- an insert for use in Question 3 (enclosed).

You may use a graphics calculator.

Time allowed: 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The *Examining Body* for this paper is AQA. The *Paper Reference* is MS/SS1B.
- Answer all questions.
- Show all necessary working; otherwise marks for method may be lost.
- The **final** answer to questions requiring the use of tables or calculators should normally be given to three significant figures.
- Fill in the boxes at the top of the insert.

Information

- The maximum mark for this paper is 75.
- The marks for questions are shown in brackets.
- Unit Statistics 1B has a written paper only.

Advice

• Unless stated otherwise, you may quote formulae, without proof, from the booklet.

Answer all questions.

1 The table shows the times taken, y minutes, for a wood glue to dry at different air temperatures, x $^{\circ}$ C.

x	10	12	15	18	20	22	25	28	30
y	42.9	40.6	38.5	35.4	33.0	30.7	28.0	25.3	22.6

(a) Calculate the equation of the least squares regression line y = a + bx.

(4 marks)

(b) Estimate the time taken for the glue to dry when the air temperature is 21 °C.

(2 marks)

2 A basket in a stationery store contains a total of 400 marker and highlighter pens. Of the marker pens, some are permanent and the rest are non-permanent. The colours and types of pen are shown in the table.

	Colour						
Туре	Black	Blue	Red	Green			
Permanent marker	44	66	32	18			
Non-permanent marker	36	53	21	10			
Highlighter	0	41	37	42			

A pen is selected at random from the basket. Calculate the probability that it is:

(a) a blue pen; (1 mark)

(b) a marker pen; (2 marks)

(c) a blue pen or a marker pen; (2 marks)

(d) a green pen, given that it is a highlighter pen; (2 marks)

(e) a non-permanent marker pen, given that it is a red pen. (2 marks)

3 [Figure 1, printed on the insert, is provided for use in this question.]

The table shows, for each of a sample of 12 handmade decorative ceramic plaques, the length, x millimetres, and the width, y millimetres.

Plaque	x	y		
A	232	109		
В	235	112		
С	236	114		
D	234	118		
Е	230	117		
F	230	113		
G	246	121		
Н	240	125		
I	244	128		
J	241	122		
K	246	126		
L	245	123		

- (a) Calculate the value of the product moment correlation coefficient between x and y.

 (3 marks)
- (b) Interpret your value in the context of this question.

(2 marks)

(c) On Figure 1, complete the scatter diagram for these data.

(3 marks)

(d) In fact, the 6 plaques A, B, ..., F are from a different source to the 6 plaques G, H, ..., L.

With reference to your scatter diagram, but without further calculations, estimate the value of the product moment correlation coefficient between x and y for each source of plaque.

(2 marks)

4	The runs scored b	y a cricketer in 11	innings during	the 2006 season	were as follows.
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47 63 0 28 40 51 *a* 77 0 13 35

The exact value of a was unknown but it was greater than 100.

- (a) Calculate the median and the interquartile range of these 11 values. (4 marks)
- (b) Give a reason why, for these 11 values:
 - (i) the mode is **not** an appropriate measure of average;
 - (ii) the range is **not** an appropriate measure of spread. (2 marks)
- 5 When a particular make of tennis ball is dropped from a vertical distance of 250 cm on to concrete, the height, *X* centimetres, to which it first bounces may be assumed to be normally distributed with a mean of 140 and a standard deviation of 2.5.
 - (a) Determine:
 - (i) P(X < 145); (3 marks)
 - (ii) P(138 < X < 142). (4 marks)
 - (b) Determine, to one decimal place, the maximum height exceeded by 85% of first bounces. (4 marks)
 - (c) Determine the probability that, for a random sample of 4 first bounces, the mean height is greater than 139 cm. (4 marks)
- **6** For the adult population of the UK, 35 per cent of men and 29 per cent of women do not wear glasses or contact lenses.
 - (a) Determine the probability that, in a random sample of 40 men:
 - (i) at most 15 do not wear glasses or contact lenses; (3 marks)
 - (ii) more than 10 but fewer than 20 do not wear glasses or contact lenses. (3 marks)
 - (b) Calculate the probability that, in a random sample of 10 women, exactly 3 do not wear glasses or contact lenses. (3 marks)
 - (c) (i) Calculate the mean and the variance for the number who **do** wear glasses or contact lenses in a random sample of 20 women. (3 marks)
 - (ii) The numbers wearing glasses or contact lenses in 10 groups, each of 20 women, had a mean of 16.5 and a variance of 2.50.

Comment on the claim that these 10 groups were **not** random samples. (3 marks)

7 Vernon, a service engineer, is expected to carry out a boiler service in one hour.

One hour is subtracted from each of his actual times, and the resulting differences, x minutes, for a random sample of 100 boiler services are summarised in the table.

Difference	Frequency
$-6 \leqslant x < -4$	4
$-4 \leqslant x < -2$	9
$-2 \leqslant x < 0$	13
0 ≤ x < 2	27
2 ≤ x < 4	21
4 ≤ <i>x</i> < 6	15
6 ≤ <i>x</i> < 8	7
$8 \leqslant x \leqslant 10$	4
Total	100

- (a) (i) Calculate estimates of the mean and the standard deviation of these differences.

 (4 marks)
 - (ii) Hence deduce, in minutes, estimates of the mean and the standard deviation of Vernon's actual service times for this sample. (3 marks)
- (b) (i) Construct an approximate 98% confidence interval for the mean time taken by Vernon to carry out a boiler service. (4 marks)
 - (ii) Give a reason why this confidence interval is approximate rather than exact.

 (1 mark)
- (c) Vernon claims that, more often than not, a boiler service takes more than an hour and that, on average, a boiler service takes much longer than an hour.

Comment, with a justification, on **each** of these claims. (2 marks)

END OF QUESTIONS

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Surname		0	Other Names					
Centre Number				Candidate Number				
Candidate Signature	9							

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ASSESSMENT and QUALIFICATIONS
ALLIANCE

MATHEMATICS
Unit Statistics 1B

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STATISTICS
Unit Statistics 1B

Insert

Insert for use in **Question 3**.

Fill in the boxes at the top of this page.

Fasten this insert securely to your answer book.

Turn over for Figure 1

Figure 1 (for use in Question 3)

Decorative Plaques

