

Centre Number						Candidate Number				
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For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
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TOTAL	



General Certificate of Education
Advanced Subsidiary Examination
June 2015

Mathematics

MFP1

Unit Further Pure 1

Friday 5 June 2015 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



J U N 1 5 M F P 1 0 1

Answer **all** questions.

Answer each question in the space provided for that question.

- 1** The quadratic equation $2x^2 + 6x + 7 = 0$ has roots α and β .
- (a)** Write down the value of $\alpha + \beta$ and the value of $\alpha\beta$. **[2 marks]**
- (b)** Find a quadratic equation, with integer coefficients, which has roots $\alpha^2 - 1$ and $\beta^2 - 1$. **[5 marks]**
- (c)** Hence find the values of α^2 and β^2 . **[2 marks]**

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3 (a) Show that $(2 + i)^3$ can be expressed in the form $2 + bi$, where b is an integer. **[3 marks]**

(b) It is given that $2 + i$ is a root of the equation

$$z^3 + pz + q = 0$$

where p and q are real numbers.

(i) Show that $p = -11$ and find the value of q . **[4 marks]**

(ii) Given that $2 - i$ is also a root of $z^3 + pz + q = 0$, find a quadratic factor of $z^3 + pz + q$ with real coefficients. **[2 marks]**

(iii) Find the real root of the equation $z^3 + pz + q = 0$. **[2 marks]**

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5 (a) The matrix **A** is defined by $\mathbf{A} = \begin{bmatrix} -2 & c \\ d & 3 \end{bmatrix}$.

Given that the image of the point (5, 2) under the transformation represented by **A** is (−2, 1), find the value of *c* and the value of *d*.

[4 marks]

(b) The matrix **B** is defined by $\mathbf{B} = \begin{bmatrix} \sqrt{2} & \sqrt{2} \\ -\sqrt{2} & \sqrt{2} \end{bmatrix}$.

(i) Show that $\mathbf{B}^4 = k\mathbf{I}$, where *k* is an integer and **I** is the 2×2 identity matrix.

[2 marks]

(ii) Describe the transformation represented by the matrix **B** as a combination of two geometrical transformations.

[5 marks]

(iii) Find the matrix \mathbf{B}^{17} .

[2 marks]

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6 A curve C_1 has equation

$$\frac{x^2}{9} - \frac{y^2}{16} = 1$$

- (a)** Sketch the curve C_1 , stating the values of its intercepts with the coordinate axes.

[2 marks]

- (b)** The curve C_1 is translated by the vector $\begin{bmatrix} k \\ 0 \end{bmatrix}$, where $k < 0$, to give a curve C_2 .

Given that C_2 passes through the origin $(0, 0)$, find the equations of the asymptotes of C_2 .

[3 marks]

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7 (a) The equation $2x^3 + 5x^2 + 3x - 132\,000 = 0$ has exactly one real root α .

(i) Show that α lies in the interval $39 < \alpha < 40$.

[2 marks]

(ii) Taking $x_1 = 40$ as a first approximation to α , use the Newton–Raphson method to find a second approximation, x_2 , to α . Give your answer to two decimal places.

[3 marks]

(b) Use the formulae for $\sum_{r=1}^n r^2$ and $\sum_{r=1}^n r$ to show that

$$\sum_{r=1}^n 2r(3r + 2) = n(n + p)(2n + q)$$

where p and q are integers.

[5 marks]

(c) (i) Express $\log_8 4^r$ in the form λr , where λ is a rational number.

[1 mark]

(ii) By first finding a suitable cubic inequality for k , find the greatest value of k for which

$$\sum_{r=k+1}^{60} (3r + 2) \log_8 4^r \text{ is greater than } 106\,060.$$

[4 marks]

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8 A curve C has equation

$$y = \frac{x(x - 3)}{x^2 + 3}$$

(a) State the equation of the asymptote of C . **[1 mark]**

(b) The line $y = k$ intersects the curve C . Show that $4k^2 - 4k - 3 \leq 0$. **[5 marks]**

(c) **Hence** find the coordinates of the stationary points of the curve C .
(No credit will be given for solutions based on differentiation.) **[5 marks]**

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END OF QUESTIONS



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