

## INSTRUCTIONS TO CANDIDATES

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do **not** write in the bar codes.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- The acceleration due to gravity is denoted by  $g \,\mathrm{m \, s^{-2}}$ . Unless otherwise instructed, when a numerical value is needed, use g = 9.8.
- You are permitted to use a graphical calculator in this paper.

## **INFORMATION FOR CANDIDATES**

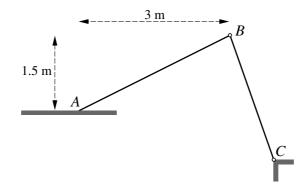
- The number of marks is given in brackets [] at the end of each question or part question.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is 72.
- This document consists of 8 pages. Any blank pages are indicated.

2

- 1 A smooth sphere of mass 0.3 kg bounces on a fixed horizontal surface. Immediately before the sphere bounces the components of its velocity horizontally and vertically downwards are  $4 \text{ m s}^{-1}$  and  $6 \text{ m s}^{-1}$  respectively. The speed of the sphere immediately after it bounces is  $5 \text{ m s}^{-1}$ .
  - (i) Show that the vertical component of the velocity of the sphere immediately after impact is  $3 \text{ m s}^{-1}$ , and hence find the coefficient of restitution between the surface and the sphere. [3]
  - (ii) State the direction of the impulse on the sphere and find its magnitude. [3]

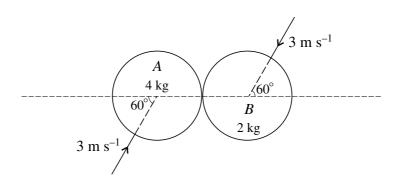
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Two uniform rods, AB and BC, are freely jointed to each other at B, and C is freely jointed to a fixed point. The rods are in equilibrium in a vertical plane with A resting on a rough horizontal surface. This surface is 1.5 m below the level of B and the horizontal distance between A and B is 3 m (see diagram). The weight of AB is 80 N and the frictional force acting on AB at A is 14 N.

- (i) Write down the horizontal component of the force acting on *AB* at *B* and show that the vertical component of this force is 33 N upwards. [4]
- (ii) Given that the force acting on *BC* at *C* has magnitude 50 N, find the weight of *BC*. [4]



Two uniform smooth spheres A and B, of equal radius, have masses 4 kg and 2 kg respectively. They are moving on a horizontal surface when they collide. Immediately before the collision both spheres have speed  $3 \text{ m s}^{-1}$ . The spheres are moving in opposite directions, each at  $60^{\circ}$  to the line of centres (see diagram). After the collision A moves in a direction perpendicular to the line of centres.

- (i) Show that the speed of *B* is unchanged as a result of the collision, and find the angle that the new direction of motion of *B* makes with the line of centres. [8]
- (ii) Find the coefficient of restitution between the spheres.

[2]

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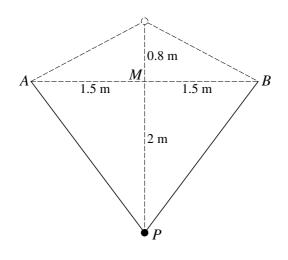
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4 A motor-cycle, whose mass including the rider is 120 kg, is decelerating on a horizontal straight road. The motor-cycle passes a point A with speed  $40 \text{ m s}^{-1}$  and when it has travelled a distance of x m beyond A its speed is  $v \text{ m s}^{-1}$ . The engine develops a constant power of 8 kW and resistances are modelled by a force of  $0.25v^2$  N opposing the motion.

(i) Show that 
$$\frac{480v^2}{v^3 - 32\,000} \frac{dv}{dx} = -1.$$
 [5]

(ii) Find the speed of the motor-cycle when it has travelled 500 m beyond A. [6]

5



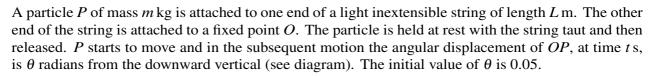
Each of two identical strings has natural length 1.5 m and modulus of elasticity 18 N. One end of one of the strings is attached to A and one end of the other string is attached to B, where A and B are fixed points which are 3 m apart and at the same horizontal level. M is the mid-point of AB. A particle P of mass  $m \, \text{kg}$  is attached to the other end of each of the strings. P is held at rest at the point 0.8 m vertically above M, and then released. The lowest point reached by P in the subsequent motion is 2 m below M (see diagram).

(i) Find the maximum tension in each of the strings during <i>P</i> 's motion.	[3]
(ii) By considering energy,	

- (a) show that the value of m is 0.42, correct to 2 significant figures, [5]
- (b) find the speed of P at M. [3]

4





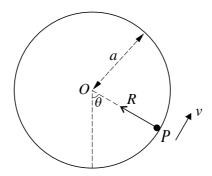
(i) Show that 
$$\frac{d^2\theta}{dt^2} = -\frac{g}{L}\sin\theta$$
. [2]

- (ii) Hence show that the motion of *P* is approximately simple harmonic. [2]
- (iii) Given that the period of the approximate simple harmonic motion is  $\frac{4}{7}\pi$  s, find the value of L.

[2]

- (iv) Find the value of  $\theta$  when t = 0.7 s, and the value of t when  $\theta$  next takes this value. [4]
- (v) Find the speed of P when t = 0.7 s. [3]





A hollow cylinder has internal radius *a*. The cylinder is fixed with its axis horizontal. A particle *P* of mass *m* is at rest in contact with the smooth inner surface of the cylinder. *P* is given a horizontal velocity *u*, in a vertical plane perpendicular to the axis of the cylinder, and begins to move in a vertical circle. While *P* remains in contact with the surface, *OP* makes an angle  $\theta$  with the downward vertical, where *O* is the centre of the circle. The speed of *P* is *v* and the magnitude of the force exerted on *P* by the surface is *R* (see diagram).

- (i) Find  $v^2$  in terms of u, a, g and  $\theta$  and show that  $R = \frac{mu^2}{a} + mg(3\cos\theta 2)$ . [7]
- (ii) Given that P just reaches the highest point of the circle, find  $u^2$  in terms of a and g, and show that in this case the least value of  $v^2$  is ag. [4]
- (iii) Given instead that *P* oscillates between  $\theta = \pm \frac{1}{6}\pi$  radians, find  $u^2$  in terms of *a* and *g*. [2]

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8