

## **INSTRUCTIONS TO CANDIDATES**

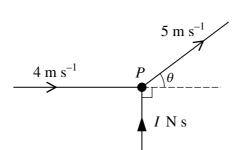
- Write your name, centre number and candidate number in the spaces provided on the answer booklet. Please write clearly and in capital letters.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the bar codes.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- The acceleration due to gravity is denoted by  $g \text{ m s}^{-2}$ . Unless otherwise instructed, when a numerical value is needed, use g = 9.8.
- You are permitted to use a scientific or graphical calculator in this paper.

## **INFORMATION FOR CANDIDATES**

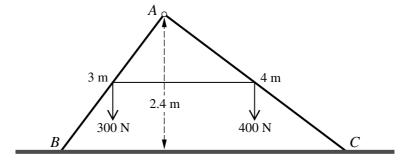
- The number of marks is given in brackets [] at the end of each question or part question.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is **72**.
- This document consists of 4 pages. Any blank pages are indicated.

[3]

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A particle *P* of mass 0.3 kg is moving in a straight line with speed  $4 \text{ m s}^{-1}$  when it is deflected through an angle  $\theta$  by an impulse of magnitude *I* N s. The impulse acts at right angles to the initial direction of motion of *P* (see diagram). The speed of *P* immediately after the impulse acts is  $5 \text{ m s}^{-1}$ . Show that  $\cos \theta = 0.8$  and find the value of *I*. [4]



Two uniform rods AB and AC, of lengths 3 m and 4 m respectively, have weights 300 N and 400 N respectively. The rods are freely jointed at A. The mid-points of the rods are joined by a light inextensible string. The rods are in equilibrium in a vertical plane with the string taut and B and C in contact with a smooth horizontal surface. The point A is 2.4 m above the surface (see diagram).

- (i) Show that the force exerted by the surface on AB is 374 N and find the force exerted by the surface on AC. [4]
- (ii) Find the tension in the string.
- (iii) Find the horizontal and vertical components of the force exerted on *AB* at *A* and state their directions. [3]
- 3 A particle *P* of mass 0.25 kg is projected horizontally with speed  $5 \text{ m s}^{-1}$  from a fixed point *O* on a smooth horizontal surface and moves in a straight line on the surface. The only horizontal force acting on *P* has magnitude  $0.2v^2$  N, where  $v \text{ m s}^{-1}$  is the velocity of *P* at time *t* s after it is projected from *O*. This force is directed towards *O*.

(i) Find an expression for 
$$v$$
 in terms of  $t$ . [5]

The particle *P* passes through a point *X* with speed  $0.2 \text{ m s}^{-1}$ .

(ii) Find the average speed of *P* for its motion between *O* and *X*. [5]

2

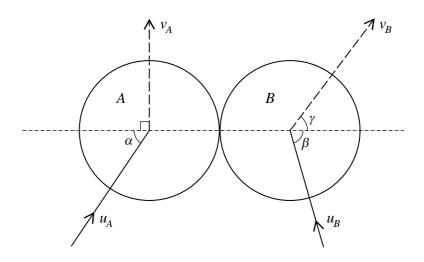
5

3

- 4 One end of a light inextensible string of length 2 m is attached to a fixed point *O*. A particle *P* of mass 0.2 kg is attached to the other end of the string. *P* is held at rest with the string taut so that *OP* makes an angle of 0.15 radians with the downward vertical. *P* is released and *t* seconds afterwards *OP* makes an angle of  $\theta$  radians with the downward vertical.
  - (i) Show that  $\frac{d^2\theta}{dt^2} = -4.9 \sin \theta$  and give a reason why the motion is approximately simple harmonic. [3]

Using the simple harmonic approximation,

- (ii) obtain an expression for  $\theta$  in terms of t and hence find the values of t at the first and second occasions when  $\theta = -0.1$ , [5]
- (iii) find the angular speed of OP and the linear speed of P when t = 0.5. [3]

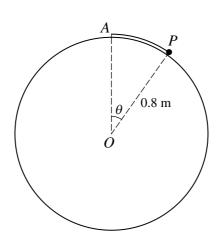


Two uniform smooth identical spheres A and B are moving towards each other on a horizontal surface when they collide. Immediately before the collision A and B are moving with speeds  $u_A \text{ m s}^{-1}$  and  $u_B \text{ m s}^{-1}$  respectively, at acute angles  $\alpha$  and  $\beta$ , respectively, to the line of centres. Immediately after the collision A and B are moving with speeds  $v_A \text{ m s}^{-1}$  and  $v_B \text{ m s}^{-1}$  respectively, at right angles and at acute angle  $\gamma$ , respectively, to the line of centres (see diagram).

- (i) Given that  $\sin \beta = 0.96$  and  $\frac{v_B}{u_B} = 1.2$ , find the value of  $\sin \gamma$ . [2]
- (ii) Given also that, before the collision, the component of *A*'s velocity parallel to the line of centres is  $2 \text{ m s}^{-1}$ , find the values of  $u_B$  and  $v_B$ . [5]
- (iii) Find the coefficient of restitution between the spheres. [3]
- (iv) Given that the kinetic energy of A immediately before the collision is 6.5m J, where m kg is the mass of A, find the value of  $v_A$ . [2]

## [Questions 6 and 7 are printed overleaf.]

4



A particle *P* of weight 6 N is attached to the highest point *A* of a fixed smooth sphere by a light elastic string. The sphere has centre *O* and radius 0.8 m. The string has natural length  $\frac{1}{10}\pi$  m and modulus of elasticity 9 N. *P* is released from rest at a point *X* on the sphere where *OX* makes an angle of  $\frac{1}{4}\pi$  radians with the upwards vertical. *P* remains in contact with the sphere as it moves upwards to *A*. At time *t* seconds after the release, *OP* makes an angle of  $\theta$  radians with the upwards vertical (see diagram). When  $\theta = \frac{1}{6}\pi$ , *P* passes through the point *Y*.

- (i) Show that as *P* moves from *X* to *Y* its gravitational potential energy increases by  $2.4(\sqrt{3} \sqrt{2}) J$  and the elastic potential energy in the string decreases by  $0.4\pi J$ . [5]
- (ii) Verify that the transverse acceleration of *P* is zero when  $\theta = \frac{1}{6}\pi$ , and hence find the maximum speed of *P*. [6]
- 7 One end of a light inextensible string of length 0.8 m is attached to a fixed point *O*. A particle *P* of mass 0.3 kg is attached to the other end of the string. *P* is projected horizontally from the point 0.8 m vertically below *O* with speed 5.6 m s<sup>-1</sup>. *P* starts to move in a vertical circle with centre *O*. The speed of *P* is  $v \text{ m s}^{-1}$  when the string makes an angle  $\theta$  with the downward vertical.
  - (i) While the string remains taut, show that  $v^2 = 15.68(1 + \cos \theta)$ , and find the tension in the string in terms of  $\theta$ . [7]
  - (ii) For the instant when the string becomes slack, find the value of  $\theta$  and the value of v. [3]
  - (iii) Find, in either order, the speed of *P* when it is at its greatest height after the string becomes slack, and the greatest height reached by *P* above its point of projection. [4]



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