

General Certificate of Education Advanced Subsidiary Examination June 2012

Mathematics

MPC1

Unit Pure Core 1

Wednesday 16 May 2012 9.00 am to 10.30 am

For this paper you must have:

• the blue AQA booklet of formulae and statistical tables.

You must **not** use a calculator.



Time allowed

• 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The use of calculators is **not** permitted.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

更多咨询请登录

群尧咨询

(2 marks)

2

1 Express
$$\frac{5\sqrt{3}-6}{2\sqrt{3}+3}$$
 in the form $m + n\sqrt{3}$, where *m* and *n* are integers. (4 marks)

- **2** The line *AB* has equation 4x 3y = 7.
 - (a) (i) Find the gradient of *AB*.
 - (ii) Find an equation of the straight line that is parallel to AB and which passes through the point C(3, -5), giving your answer in the form px + qy = r, where p, q and r are integers. (3 marks)
 - (b) The line AB intersects the line with equation 3x 2y = 4 at the point D. Find the coordinates of D. (3 marks)
 - (c) The point *E* with coordinates (k-2, 2k-3) lies on the line *AB*. Find the value of the constant *k*. (2 marks)
- **3** The polynomial p(x) is given by

$$p(x) = x^3 + 2x^2 - 5x - 6$$

(a) (i) Use the Factor Theorem to show that x + 1 is a factor of p(x). (2 marks)

- (ii) Express p(x) as the product of three linear factors. (3 marks)
- (b) Verify that p(0) > p(1). (2 marks)
- (c) Sketch the curve with equation $y = x^3 + 2x^2 5x 6$, indicating the values where the curve crosses the x-axis. (3 marks)



3

4 The diagram shows a solid cuboid with sides of lengths x cm, 3x cm and y cm.



The total surface area of the cuboid is 32 cm^2 .

- (a) (i) Show that $3x^2 + 4xy = 16$. (2 marks)
 - (ii) Hence show that the volume, $V \text{ cm}^3$, of the cuboid is given by

$$V = 12x - \frac{9x^3}{4} \qquad (2 \text{ marks})$$

(b) Find
$$\frac{\mathrm{d}V}{\mathrm{d}x}$$
. (2 marks)

(c) (i) Verify that a stationary value of V occurs when $x = \frac{4}{3}$. (2 marks)

(ii) Find $\frac{d^2 V}{dx^2}$ and hence determine whether V has a maximum value or a minimum value when $x = \frac{4}{3}$. (2 marks)



4

- **5 (a) (i)** Express $x^2 3x + 5$ in the form $(x p)^2 + q$. (2 marks)
 - (ii) Hence write down the equation of the line of symmetry of the curve with equation $y = x^2 3x + 5$. (1 mark)
 - (b) The curve C with equation $y = x^2 3x + 5$ and the straight line y = x + 5 intersect at the point A(0, 5) and at the point B, as shown in the diagram below.



(i) Find the coordinates of the point *B*. (3 marks)

- (ii) Find $\int (x^2 3x + 5) dx$. (3 marks)
- (iii) Find the area of the shaded region R bounded by the curve C and the line segment AB. (4 marks)



6

(1 mark)

5

The circle with centre C(5, 8) touches the y-axis, as shown in the diagram.



(a) Express the equation of the circle in the form

$$(x-a)^2 + (y-b)^2 = k$$
 (2 marks)

- (b) (i) Verify that the point A(2, 12) lies on the circle.
 - (ii) Find an equation of the tangent to the circle at the point A, giving your answer in the form sx + ty + u = 0, where s, t and u are integers. (5 marks)
- (c) The points P and Q lie on the circle, and the mid-point of PQ is M(7, 12).
 - (i) Show that the length of CM is $n\sqrt{5}$, where n is an integer. (2 marks)
 - (ii) Hence find the area of triangle *PCQ*. (3 marks)

7 The gradient, $\frac{dy}{dx}$, of a curve C at the point (x, y) is given by

$$\frac{\mathrm{d}y}{\mathrm{d}x} = 20x - 6x^2 - 16$$

- (a) (i) Show that y is increasing when $3x^2 10x + 8 < 0$. (2 marks)
 - (ii) Solve the inequality $3x^2 10x + 8 < 0$. (4 marks)
- (b) The curve C passes through the point P(2, 3).
 - (i) Verify that the tangent to the curve at *P* is parallel to the *x*-axis. (2 marks)
 - (ii) The point Q(3, -1) also lies on the curve. The normal to the curve at Q and the tangent to the curve at P intersect at the point R. Find the coordinates of R. (7 marks)

Copyright © 2012 AQA and its licensors. All rights reserved.

