4728

Mark Scheme

January 2005

1	(i)	$R = W \cos \alpha$	M1		For resolving forces perpendicular to the plane
		Magnitude is 96 N	A1	2	
[(ii)	Magnitude is 24 N	B1	1	AG From correct work.
[(iii)	$P = 100 \times 0.28 - 24$	M1		For resolving 3 forces parallel to the plane (either
		$P = 100 \times 0.28 + 24$			case)
		(a) $P = 4$	A1		
		(b) $P = 52$	A1	3	

2	(i)	Momentum of A and B before			Alternatively: Momentum lost by $A = 0.4 \times (6 - v)$
		collision = $0.4 \times 6 - 1.2 \times 2$	B1		B1
		Momentum of A and B after			Momentum gained by B
		collision = $0.4v + 1.2 \times 1$	B1		$= 1.2 \times (1+2)$ B1
		$0.4 \times 6 - 1.2 \times 2 = 0.4v + 1.2 \times 1$	M1		For using the principle of conservation of
		(v = -3)			momentum
		Speed is 3 ms ⁻¹	A1		Positive answer only
		Direction is away from <i>B</i>	A1 ft	5	ft from <i>v</i>
[(ii)	$1.2 \times 1 - 4m = -1.2 \times 0.5 + 2m$			For momentum equation :-
		or $1.2 \times 1 + 1.2 \times 0.5 = 4m + 2m$			
			B1		with lhs correct
			B1		with rhs correct
	_	m = 0.3	B1	3	
		_			SR If mgv used for momentum instead of mv,
					then
					(i) Speed is 3 ms^{-1} B1
					Direction is away from <i>B</i> B1 ft
					(ii) m = 0.3 B1

3	(i)(a)		M1		For resolving 3 forces parallel to the <i>x</i> -axis
		$X = 2 \times 8\cos 30^{\circ} - 5\sin 40^{\circ}$ Component is 10.6 N	A1 A1 ft		ft for 4.17 from sin/cos mix only
	(i)(b)	$Y = 5\cos 40^{\circ}$	B1		
		Component is 3.83 N	B1 ft	5	ft for 3.21 from sin/cos mix only
	(ii)	$R^2 = 10.64^2 + 3.83^2$	M1		For using $R^2 = X^2 + Y^2$
		Magnitude is 11.3 N	A1 ft		
		$\tan \theta = 3.83/10.64$	M1		For using $\tan \theta = Y/X$
		Direction is 19.8° anticlockwise			
		from +ve <i>x</i> -axis	A1 ft	4	

4728

4	(i)		M1		For using $a = \dot{v}(t)$
		Acceleration is $1 + 0.2t$	A1	2	
	(ii)		M1		For solving $a(t) = 2.8$ for t
		t = 9	A1		
			M1*		For integrating $v(t)$ to find $s(t)$
			A1		For $t^2 \div 2$ correct in $s(t)$
			A1		For $t^3 \div 30$ correct in $s(t)$
		$s(9) = 9^2 \div 2 + 9^3 \div 30 - (0+0)$	dep*M1		For correct use of limits or equivalent
		(=40.5+24.3)			
		Distance is 64.8 m	A1 ft	7	ft their $a = \dot{v}(t)$ from (i)

5	(i)	Heights are $7t - \frac{1}{2}gt^2$ and			
		$10.5t - \frac{1}{2}gt^2$	B1	1	
	(ii)	Expression is 3.5 <i>t</i>	B1	1	From correct (i)
[(iii)	0 = 7 - 9.8t	M1		For using $v = u - gt$ with $v = 0$
		t = 5/7 or 0.714	A1		
		Difference is 2.5 m	A1 ft	3	ft value of t
[(iv)	t = 1	B1 ft		For using ans(ii) = 3.5 correctly
		Greater than 5/7 (may be implied)	M1		For comparing this <i>t</i> with the time to greatest
		or 7 - $g \times 1$ is -ve			height or considering the sign of v_A for this t
		Direction is downwards	A1	3	
[(v)	$h_{\rm A} = 7 \times 1 - \frac{1}{2} 9.8 \times 1^2$	M1		For using $h = ut - \frac{1}{2}gt^2$ with relevant t
		Height is 2.1 m	A1	2	

4728

Mark Scheme

January 2005

6	(i)		M1		For using the idea that the gradient represents acceleration or for using v = u + at
		Accelerating for 4 s	A1	2	
	(ii)		M1		For using the idea that the distance is represented by the area of the trapezium or using suitable formulae for the two stages of the journey
		$AB = \frac{1}{2}(16 + 20)8$	A1ft		
		Distance is 144 m	A1	3	
	(iii)		B1		Graph is single valued and continuous and consists of two straight line segments with one segment from the origin and the other parallel to the <i>t</i> axis
			51		Graph for Q is the reflection of the graph for P in
			B1	2	the t axis
	(iv)				Graph is single valued and continuous and consists of two parts, one of which is a straight line segment, with <i>x</i> increasing from 0 for the
			B1		interval $0 < t < 20$
			B1		$x_{\rm P}(20)$ appears to be equal to $x_{\rm O}(0)$
			B1		Graph for <i>P</i> appears to be the reflection in $x =$
				3	$ans(ii) \div 2$ of graph for Q
	(v)	$t = 20 - (\frac{1}{2} \ 144 \div 8)$ or 16 + 8(t-4) = 128 - 8(t-4) or equivalent	M1		For complete method of finding the required time
		Value of <i>t</i> is 11	A2	3	SR Allow B1 for t = 11 without explanation

7	(i)		M1		For applying Newton's second law to either
					particle
		T - F = 0.3a	A1		
		$0.2g\sin 70^{\circ} - T = 0.2a$	A1		
		R = 0.3g	B1		
		F = 0.4(0.3g)	M1		For using $F = \mu R$
		$0.2g\sin 70^{\circ} - 0.4(0.3g) = 0.5a$ Acceleration is 1.33 ms ⁻²	M1		For eliminating <i>F</i> and <i>T</i> or <i>a</i>
		Acceleration is 1.33 ms ⁻²	A1		
		Tension is 1.58 N	A1	8	
	(ii)	a = -0.4g	B1		May be scored in (iii)
		$0 = 1.5^2 - 2 \times 3.92s$	M1		For using $v^2 = u^2 + 2as$ with $v = 0$
		Distance is 0.287 m	A1	3	
	(iii)		M1		For using $v = u + at$ or equivalent with $v = 0$ for A
		0 = 1.5 - 3.92t	A1ft		ft value of <i>a</i> from (ii)
		t = 0.383 (may be implied)	A1		
		$a = g \sin 70^{\circ}$	B1		For acceleration of <i>B</i>
		$s = 1.5(0.383) + \frac{1}{2}9.8\sin 70^{\circ}(0.383)^2$	M1		For using $s = ut + \frac{1}{2} at^2$ or equivalent with $u \neq 0$
		(=0.574+0.674)			
		Distance is 1.25 m	A1	6	