

Mark Scheme 4728

January 2007

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|---|------|------------------------------|--|--|
| 1 | (i) | Net force on trailer is | B1 | |
| | | $\pm(700 - R_T)$ | M1 | For applying Newton's second law to the trailer with 2 terms on LHS (no vertical forces) |
| | | $700 - R_T = 600 \times 0.8$ | A1ft | ft cv ($\pm(700 - R_T)$) |
| | (ii) | Resistance is 220N | A1 | 4 |
| | | M1 | For applying Newton's second law to the car or to the whole, with $a = \pm 0.8$ (no vertical forces) | |
| | | $2100 - 700 - R_C =$ | A1ft | |
| | | 1100×0.8 | | |
| | | or | | ft cv(220) |
| | | $2100 - (R_C + 220) =$ | | |
| | | $(1100 + 600) \times$ | | |
| | | 0.8 | | |
| | | Resistance is 520N | A1 | 3 |

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|---|-------|---|------|--|
| 2 | (i) | | M1 | For resolving forces vertically |
| | | 15×0.28 and 11×0.8 | A1 | Allow use of $\sin = 16.3$ and $\cos = 53.1$ |
| | | $Y = 15 \times 0.28 + 11 \times 0.8 - 13$ | A1ft | Ft cv(15×0.28 and 11×0.8) |
| | | Component is zero | A1 | 4 |
| | | AG | | SR $15 \sin + 11 \sin - 13 = 0$ gets M1A0A1ftA0 |
| | (ii) | | M1 | For resolving forces horizontally |
| | | $X = 15 \times 0.96 - 11 \times 0.6$ | A1 | Allow use of $\sin = 16.3$ and $\cos = 53.1$ |
| | | Magnitude is 7.8N | A1 | 3 |
| | (iii) | Direction is that of the | B1 | 1 |
| | | (+ve) x -axis | | Do not allow horizontal, 90° from vertical. Do not award if $\sin = 16.3$ and $\cos = 53.1$ have been used. |

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| 3 | (i) | $T = 0.3g$ | B1 | At particle (or $0.3g - T = 0.3a$) |
| | | $F = T$ | B1 | Or $F = cv(T \text{ at particle})$ (or $T - F = 0.4a$) |
| | | $R = 0.4g$ | B1 | |
| | | | M1 | For using $F = \mu R$ |
| | (ii) | Coefficient is 0.75 | A1 | 5 |
| | | $X = 0.3g + 0.3g$ | M1 | For resolving 3 relevant forces on B horizontally, $a=0$ |
| | | | A1ft | Ft $X = 0.3g + cv(\mu)$ |
| | | | | cv(R) |
| | | $X = 5.88N$ | A1 | 3 |

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|---|---------|---|---------|---|--|
| 4 | (i) | Momentum before collision $= +/- (0.8 \times 4 - 0.6 \times 2)$ | B1 | 4 | Or momentum change L $0.8 \times 4 +/- 0.8 v_L$ Accept inclusion of g in both terms |
| | | Momentum after collision $= +/- 0.8 v_L + 0.6 \times 2$ | B1 | | Momentum change N $0.6 \times 2 + 0.6 \times 2$ Accept inclusion of g in both terms |
| | | Speed is 1 ms^{-1} | M1 | | For using the principle of conservation of momentum even if g is included throughout |
| | | | A1 | | Accept -1 from correct work (g not used). |
| | (ii)(a) | $0.6 \times 2 - 0.7 \times 0.5$ | M1 | 4 | Must be a difference. SR $0.6 \times 1 - 0.7 \times 0.5$ M1 |
| | | Total is 0.85 kgms^{-1} | A1 | | Must be positive |
| | | <u>Total</u> momentum +ve after the collision. If N continues in its original direction, both particles have a negative momentum. N must reverse its direction. | DM 1 | | Or $0.6v + 0.7w$ is positive, confirming that the momentum is shared between two particles. No reference need be made to the physically impossible scenario where M and N both might continue in their original directions. |
| | | | A1 | | |
| | (ii)(b) | $0.6 \times 2 - 0.7 \times 0.5 (= 0.85) = 0.7v$ | A1ft | 2 | ft cv (0.85). Award M1 if not given in ii(a). |
| | | Speed is 1.21 ms^{-1} | A1 | | Positive. Accept (a.r.t) 1.2 from correct work |

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|---|-------|---|----------------------|---|--|
| 5 | (i) | $1.8t^2/2$ (+C) | M*1 | 3 | For using $v = \int adt$ |
| | | (t = 0, v = 0) C = 0 Expression is $1.8t^2/2$ | B1 A1 | | May be awarded in (ii). Accept c written and deleted. also for $1.8t^2 + c$ |
| | (ii) | $0.9t^3/3$ (+K) | M1 A1 | 4 | For using $s = \int vdt$ |
| | | 0.3×64 19.2m AG | M1 A1 | | SR Award B1 for (s = 0, t = 0) K = 0 if not already given in (i), or +K included and limits used. For using limits 0 to 4 (or equivalent) |
| | (iii) | $u = 0.9 \times 4^2$ | D* M1 | 5 | For using 'u' = v(4) |
| | | $s = 14.4 \times 3 + \frac{1}{2} \times 7.2 \times 3^2$ | M1 A1 | | For using $s = ut + \frac{1}{2} at^2$ with non-zero u (s = 75.6) |
| | | $19.2 + 75.6$ Displacement is 94.8m | M1 A1 | | For adding distances for the two distinct stages |
| | | OR $v = \int 7.2dt$ | D* M1 | | For finding v(4) Integration and finding non-zero integration constant Nb Using t=4, v=14.4 gives c = -14.4 |
| | | t = 0, v = 14.4, c = 14.4 $s = \int 7.2t + 14.4dt$ | | | $s = \int 7.2t - 14.4dt$ |
| | | t = 0, s = 0, k = 0 | | | Integration and finding integration constant. Nb t=4 with s=19.2 and v=7.2t-14.4 gives k=19.2 |
| | | $s = 3.6 \times 3^2 + 14.4 \times 3$ $19.2 + 75.6 = 94.8$ Displacement is 94.8m | M1 A1 M1 A1 | | Substituting t = 3 (OR 7 into $s = 3.6t^2 - 14.4t + 19.2$) (s=75.6) (OR $s = 3.6 \times 7^2 - 14.4 \times 7 + 19.2$) Adding two distinct stages OR $s = 3.6 \times 7^2 - 14.4 \times 7 + 19.2 = 94.8$ final M1A1 |

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|---|-----|---|-----|--|
| 6 | (i) | $\frac{1}{2} 25v_m = 8$ or $\frac{1}{2} T v_m + \frac{1}{2} (25 - T)v_m =$ | B*1 | Do not accept solution based on isosceles or right angled triangle |
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| | 8 | | | |
| | Greatest speed is | D*B | 2 | |
| | 0.64 | 1 | | |
| (ii) | ms ⁻¹ | M1 | | For using $v = u + at$ or the idea that gradient represents acceleration |
| | $V = 0.02 \times 40$ | A1 | | |
| | $V = 0.8$ | A1 | 3 | |
| (iii) | | M1 | | For using the idea that the area represents displacement. nb trapezium area is $16+8+8$ |
| | | M1 | | For $A = \frac{1}{2}(L_1 + L_2)h$ or other appropriate breakdown |
| | $\frac{1}{2}(70 + T) \times 0.8 = 40 - 8$ | A1ft | | $\frac{1}{2}(30 + T) \times 0.8 = 40 - 8 - \frac{1}{2} \times 40 \times 0.8$ ft cv(0.8) |
| | 8 | | | |
| | Duration is 10s | A1 | 4 | |
| (iv) | | M1 | | For using $v = u + at$ or the idea that gradient represents acceleration |
| | $0=0.8+a(30-10)$ | A1ft | | ft cv(10) and cv(0.8) |
| | Deceleration is | A1 | 3 | Accept -0.04 from correct work |
| | 0.04ms^{-2} | | | |
| | Or | M1 | | Using the idea that the area represents displacement. |
| | $40-8-\frac{1}{2} \times 40 \times 0.8-$ | A1ft | | Ft cv(0.8 and 10) |
| | 10×0.8 | A1 | | Accept -0.04 from correct work. $d=-0.04$ A0 |
| | $=0.8(30-10)-a(30-$ | | | |
| | $10)^2/2$ | | | |
| | Deceleration is | | | |
| | 0.04ms^{-2} | | | |

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|-----------------------------------|----------------|--|---|---|---|
| 7 | (i) | $R = 0.5g\cos 40^\circ$ | B1 | $R = 3.7536$ | |
| | | $F = 0.6 \times 0.5g\cos 40^\circ$ | M1 | For using $F = \mu R$ | |
| | | Magnitude is 2.25N AG | A1 | 3 | |
| | (ii) | | M1 | For applying Newton's second law (either case) //slope, two forces | |
| | | $-/+0.5g\sin 40^\circ - F = 0.5a$ | A1 | Either case | |
| | | (a) Acceleration is – 10.8ms^{-2} | A1 | Accept 10.8 from correct working (both forces have the same sign) | |
| | | (b) Acceleration is 1.79ms^{-2} | A1 | 4 | Accept -1.79 from correct working (the forces have opposite sign) Accept ! 1.8(0) |
| | (iii)a) | $0 = 4 + (-10.8)T_1$ | M1 | Requires appropriate sign | |
| | | $T_1 = 0.370(3)$ | A1 | Accept 0.37 | |
| | b) | | M1 | For complete method of finding distance from A to highest point using a(up) with appropriate sign | |
| | | $0 = 4^2 + 2(-10.8)s$ or $s = (0 + 4) \times 0.37/2$ or $s = 4(0.370) + \frac{1}{2}(-10.8)(0.370)^2$ | A1 ft | ft a(up) and/or T_1 ($s = 0.7405$) | |
| | | | M1 | For method of finding time taken from highest point to A and not using a(up) | |
| $0.7405 = \frac{1}{2}(1.79)T_2^2$ | | A1ft | ft a(down) and cv(0.7405) ($T_2 = 0.908$ approx) | | |
| $0.370 + 0.908 = 1.28\text{s}$ | | M1 A1 | Using $T = T_1 + T_2$ with different values for T_1, T_2 3 significant figures cao | 8 | |