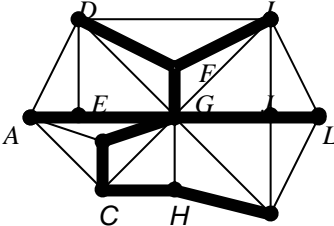


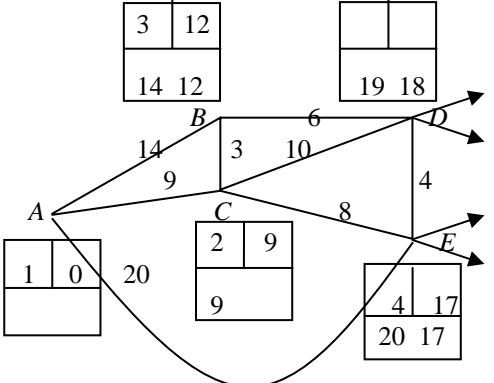
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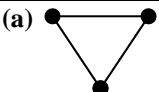
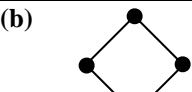
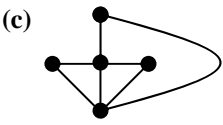
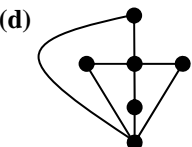
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|  |                                       |  |
|--|---------------------------------------|--|
| <p><b>1</b></p> <p>BC = 3<br/>                 FG = 4<br/>                 JL = 5<br/>                 EG = 6<br/>                 AE = 7<br/>                 BG = 7<br/> <del>AB = 8</del><br/>                 CH = 8<br/>                 DF = 8<br/>                 GJ = 8<br/>                 HK = 8<br/> <del>AC = 9</del><br/> <del>DE = 9</del><br/>                 FI = 9<br/> <del>GH = 9</del><br/> <del>H = 9</del><br/> <del>JK = 9</del><br/>                 AD = 10<br/>                 DG = 10<br/> <del>GK = 10</del><br/> <del>H = 10</del><br/>                 KL = 10<br/> <del>GI = 11</del><br/> <del>CG = 12</del><br/> <del>DI = 12</del></p>  <p style="text-align: right;">Total weight = 73</p> | <p>M1<br/>A1<br/>M1<br/>A1<br/>B1</p> | <p>For selecting all arcs up to <i>AB</i> and deleting <i>AB</i> in list<br/>                 For deleting <i>AC, DE</i> in list and selecting arcs for tree correctly, indicated in any way<br/>                 For a spanning tree drawn<br/>                 For correct (minimum) spanning tree drawn<br/>                 For total = 73</p> |
|--|---------------------------------------|--|

|   |  |   |
|---|--|---|
| <p><b>2</b></p>  | <p>M1<br/>M1<br/>A1<br/>B1<br/>M1<br/>A1</p> | <p>For temporary labels at <i>B</i> correct, no extras<br/>                 For temporary labels at <i>E</i> correct, no extras<br/>                 For permanent labels correct at <i>B, C</i> and <i>E</i> (dependent on both M marks)<br/>                 For order of labelling correct at <i>C, B</i> and <i>E</i><br/>                 For temporary labels at <i>D</i> correct<br/>                 For no permanent label at <i>D</i></p> |
|---|--|---|

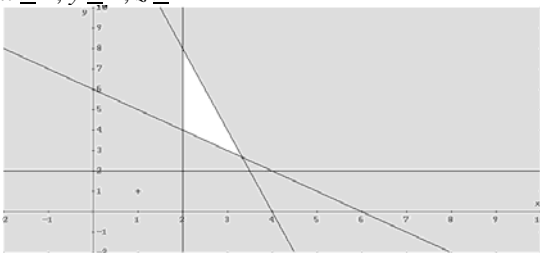
|   |  |   |
|---|--|---|
| <p><b>3</b></p> <p>(i) (a) </p> <p>(b) </p> <p>(c) </p> <p>(d) </p> <p>(ii) <math>2n</math> if <math>n</math> is even<br/> <math>2n + 1</math> if <math>n</math> is odd</p> | <p>B1<br/>B1<br/>B1<br/>B1<br/>(4)<br/>M1 (2)<br/>A1</p> | <p>For a correct graph for (a)<br/>                 For a correct graph for (b)<br/>                 For a clearly correct graph for (c)<br/>                 For a clearly correct graph for (d)<br/>                 For treating the cases <math>n</math> odd and <math>n</math> even separately<br/>                 For both rules correct</p> |
|---|--|---|

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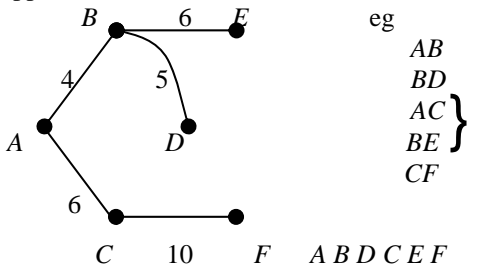
| <b>4</b> | <b>(i)</b>  | <table border="1"> <tr><th><math>P</math></th><th><math>x</math></th><th><math>y</math></th><th><math>z</math></th><th><math>s</math></th><th><math>t</math></th><th></th></tr> <tr><td>1</td><td>-5</td><td>4</td><td>3</td><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>2</td><td>-3</td><td>4</td><td>1</td><td>0</td><td>10</td></tr> <tr><td>0</td><td>6</td><td>5</td><td>4</td><td>0</td><td>1</td><td>60</td></tr> </table> | $P$   | $x$  | $y$ | $z$ | $s$ | $t$ |   | 1 | -5   | 4 | 3   | 0 | 0 | 0 | 0 | 2  | -3 | 4  | 1 | 0  | 10 | 0   | 6 | 5 | 4 | 0 | 1 | 60 | M1 | For overall structure correct, including two slack variable columns |
|----------|---|--|---|--|-----|-----|-----|-----|---|---|------|---|-----|---|---|---|---|----|----|----|---|----|----|---|---|---|---|---|---|----|----|---|
|          |   | $P$  | $x$   | $y$  | $z$ | $s$ | $t$ |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          |   | 1  | -5  | 4  | 3   | 0   | 0   | 0   |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          |   | 0  | 2   | -3   | 4   | 1   | 0   | 10  |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          | 0   | 6  | 5   | 4  | 0   | 1   | 60  |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          | A1  | For a correct initial tableau, with no extra constraints added   |   |  |     |     |     |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          | (2)   |  |   |  |     |     |     |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          | <b>(ii)</b>   | Pivot on 2 in $x$ column<br>$r1 = r1 + 5npr$<br>$r2 = r2 \div 2$<br>$r3 = r3 - 6npr$   | M1  | For the correct pivot choice for their tableau |     |     |     |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          | <table border="1"> <tr><td>1</td><td>0</td><td>-3.5</td><td>13</td><td>2.5</td><td>0</td><td>25</td></tr> <tr><td>0</td><td>1</td><td>-1.5</td><td>2</td><td>0.5</td><td>0</td><td>5</td></tr> <tr><td>0</td><td>0</td><td>14</td><td>-8</td><td>-3</td><td>1</td><td>30</td></tr> </table> | 1  | 0   | -3.5   | 13  | 2.5 | 0   | 25  | 0 | 1 | -1.5 | 2 | 0.5 | 0 | 5 | 0 | 0 | 14 | -8 | -3 | 1 | 30 | A1 | For dealing with the pivot row correctly (formula or numerical) |   |   |   |   |   |    |    |   |
|          | 1   | 0  | -3.5  | 13   | 2.5 | 0   | 25  |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
| 0        | 1   | -1.5   | 2   | 0.5  | 0   | 5   |     |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
| 0        | 0   | 14   | -8  | -3   | 1   | 30  |     |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          |   | M1   | For dealing with the other rows correctly (formulae or numerical) |  |     |     |     |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          |   | A1   | For a correct tableau (not ft)                                    |  |     |     |     |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          | $x = 5, y = 0, z = 0$<br>$P = 25$   | B1 (6)   | For reading off $x, y$ and $z$ from their tableau                 |  |     |     |     |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |
|          |   | B1 <b>8</b>  | For reading off $P$ from their tableau                            |  |     |     |     |     |   |   |      |   |     |   |   |   |   |    |    |    |   |    |    |   |   |   |   |   |   |    |    |   |

|          |              |  |  |  |
|----------|--------------|--|--|--|
| <b>5</b> | <b>(i)</b>   | $x =$ number of lengths swum using breaststroke<br>$y =$ number of lengths swum using backstroke<br>$z =$ number of lengths swum using butterfly | B1   | For defining variables as 'number of lengths swum' using each stroke, or equivalent                      |
|          |              | Maximise $2x + y + 5z$   | B1 (2)   | For a correct expression using their variables   |
|          |              | <b>(ii)</b>  | $x + y + z \geq 8$<br>$2x + 0.5y + z \leq 10$<br>$x \geq 2, y \geq 2, z \geq 2$                    | B1   |
|          | <b>(iii)</b> |    | B1 (3)   | For correct expressions using their variables  |
|          |              | $(2, 4), (2, 8), (3.3, 2.7)$   | M1   | For plotting the sloping lines correctly   |
|          |              |  | A1   | For completely correct shading   |
|          |              | $2 \times 2 + 8 = 12$<br>$2 \times 3.33 + 2.67 = 9.33$   | M1   | For two correct vertices from their graph  |
|          |              | So maximum is when $x = 2$ and $y = 8$   | A1   | For all three vertices correct to at least 1 dp  |
|          | <b>(iv)</b>  | Swim 2 lengths using breaststroke, 8 lengths using backstroke and 2 lengths using butterfly  | M1   | For calculating $P$ at vertices or using a valid line of constant profit or writing down their max point |
|          |              | Total = 22 style marks   | A1 (6)   | For the correct values   |
|          |              | B1   | For interpreting their solution in the context of the original problem (at least for $x$ and $y$ ) |  |
|          |              | B1 (2)   | For calculating the number of marks for their solution   |  |
|          |              | <b>13</b>  |  |  |

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| <p><b>6</b> (i) <i>A-B-D-E-G-F-C-A</i><br/>42 minutes<br/><i>A-B-D-C-F-G-E-A</i><br/>46 minutes<br/>Upper bound = 42 minutes</p> <p>(ii)  eg <math>\left. \begin{array}{l} AB \\ BD \\ AC \\ BE \\ CF \end{array} \right\}</math><br/><i>ABDCEF</i><br/>or <i>ABDECF</i><br/>Total weight of tree = 31 minutes<br/>Two least weight arcs from G have weight 5+5 = 10 minutes<br/>Lower bound = 31 + 10 = 41 minutes</p> <p>(iii) Odd nodes: <i>B D E F</i></p> <p><math>BD = 5 \quad BE = 6 \quad BF = 16</math><br/><math>EF = \underline{10} \quad DF = \underline{14} \quad DE = \underline{7}</math><br/><math>\quad \quad \quad 15 \quad \quad 20 \quad \quad 23</math><br/>120 minutes<br/>Travel <i>BD, EG</i> and <i>FG</i> twice (accept <i>BD, EGF</i>)<br/>3 times</p> | <p>M1<br/>A1<br/>B1<br/>B1<br/>B1ft(5)</p> <p>M1<br/>A1</p> <p>B1</p> <p>A1 ft</p> <p>M1<br/>A1 (6)</p> <p>B1</p> <p>M1<br/>A1<br/>B1 (5)<br/>B1 <b>16</b></p> | <p>For <i>A-B-D-E-G-F-C</i>, with or without closing tour<br/>For 42<br/>For <i>A-B-D-C-F-G-E</i>, with or without closing tour<br/>For 46<br/>For the smaller of their two times</p> <p>For a diagram or listing showing a tree connecting the vertices <i>A, B, C, D, E</i> and <i>F</i>, but not <i>G</i><br/>For a diagram showing this tree (vertices need to be labelled, but arc weights are not needed)</p> <p>For a valid vertex or arc order</p> <p>For the total weight of their tree stated</p> <p>For stating or using <i>GE, GF</i> or 5+5 or 10<br/>For 41 or 10 + their 31 calculated</p> <p>For identifying or using <i>B D E F</i></p> <p>For calculating 5+10 or 6+14 or 16+7 (may be implied from correct pair chosen)<br/>For 120 (unsupported 120 scores 0 marks)<br/>For correct arcs listed and no others<br/>For 3</p> |
|--|--|---|

|  |   |   |
|--|---|---|
| <p><b>7</b> (i) Original list: 34 42 27 31 12 48 24 37<br/>1<sup>st</sup> pass: 34 27 31 12 42 24 37 <u>48</u><br/>2<sup>nd</sup> pass: 27 31 12 34 24 37 <u>42</u> <u>48</u><br/>3<sup>rd</sup> pass: 27 12 31 24 34 <u>37</u> <u>42</u> <u>48</u><br/>4<sup>th</sup> pass: 12 27 24 31 <u>34</u> <u>37</u> <u>42</u> <u>48</u><br/>5<sup>th</sup> pass: 12 24 27 <u>31</u> <u>34</u> <u>37</u> <u>42</u> <u>48</u><br/>6<sup>th</sup> pass: 12 24 27 31 34 37 42 48</p> <p>Swaps = 5+5+2+2+1 = 15<br/>Comparisons = 7+6+5+4+3+2 = 27</p> <p>(ii) Original list: 95 74 61 87 71 82 53 57<br/>1<sup>st</sup> pass: 74 95 <u>61</u> <u>87</u> <u>71</u> <u>82</u> <u>53</u> <u>57</u><br/>2<sup>nd</sup> pass: 61 74 95 <u>87</u> <u>71</u> <u>82</u> <u>53</u> <u>57</u><br/>3<sup>rd</sup> pass: 61 74 87 95 <u>71</u> <u>82</u> <u>53</u> <u>57</u><br/>4<sup>th</sup> pass: 61 71 74 87 95 <u>82</u> <u>53</u> <u>57</u><br/>5<sup>th</sup> pass: 61 71 74 82 87 95 <u>53</u> <u>57</u><br/>6<sup>th</sup> pass: 53 61 71 74 82 87 95 <u>57</u><br/>7<sup>th</sup> pass: 53 57 61 71 74 82 87 95</p> <p>Swaps = 1+2+1+3+2+6+6 = 21<br/>Comparisons = 1+2+2+4+3+6+7 = 25</p> <p>(iii) Each script is looked at once<br/>so the time taken is roughly proportional to the number of scripts</p> <p>(iv) Splitting 100 scripts takes 50 seconds<br/>so splitting 500 scripts takes about 250 seconds<br/>Sorting 50 scripts takes 250 seconds = <math>0.1 \times 50^2</math><br/>Sorting 250 scripts takes about <math>0.1 \times 250^2</math><br/>= 6250 seconds<br/>Total = 6500 seconds or 108 minutes 20 seconds</p> | <p>M1<br/>M1<br/>M1<br/>A1<br/>B1<br/>B1 (6)</p> <p>M1<br/>M1<br/>M1<br/>A1<br/>B1<br/>B1 (6)</p> <p>B1<br/>B1<br/>(2)</p> <p>M1<br/>M1 } (4)<br/>A1 }<br/>A1 <b>18</b></p> | <p>nb decreasing or numbers misread <math>\Rightarrow</math> M only<br/>For result of first pass correct (underlined entries may be omitted)<br/>For second and third passes correct, must be using bubble sort<br/>For fourth and fifth passes correct, must be using bubble sort<br/>For sixth pass correct, from correct method<br/>For 15, from correct method<br/>For 27, from correct method</p> <p>nb decreasing or numbers misread <math>\Rightarrow</math> M only<br/>For result of first pass correct (underlined entries may be omitted)<br/>For second and third passes correct, must be using shuttle sort<br/>For fourth and fifth passes correct, must be using shuttle sort<br/>For seventh pass correct, from correct method<br/>For 21, from correct method<br/>For 25, from correct method</p> <p>For 'each script is looked at once', or equivalent<br/>For 'proportional', or equivalent</p> <p>250 (but not for 250 + 50)<br/>(500<math>\div</math>2)<sup>2</sup>, (250)<sup>2</sup>, (100<math>\div</math>2)<sup>2</sup> or equivalent<br/>For 6250, dependent on previous M only<br/>For 6500 or equivalent</p> |
|--|---|---|