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Version 1.0



General Certificate of Education (A-level) January 2011

Mathematics

MFP2

(Specification 6360)

Further Pure 2



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Mark Scheme – General Certificate of Education (A-level) Mathematics – Further Pure 2 – January 2011

М	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
А	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
\checkmark or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
– <i>x</i> EE	deduct <i>x</i> marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

Key to mark scheme abbreviations

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

Mark Scheme – General Certificate of Education	(A-level) Mathematics – Further Pure 2 –	- January 2011
Mark Scheme – General Certificate of Education	$(\Lambda - 1 = v = 1)$ what the that the that $1 = 1$ with the three $Z = 1$	January 2011

MFP2					
Q	Solution	Marks	Total	Comments	
1(a)	y Circle P x Circle correct centre through (0, 0)	B1 B1 B1	3		
(b)(i)	z_1 correctly chosen	B1F	1	ft if circle encloses (0, 0)	
(ii)	$ z_1 = 8$	B1F	1	ft if centre misplotted	
	Total		5		
2(a)	$u_r - u_{r-1} =$ $\frac{1}{6}r(r+1)(4r+11) - \frac{1}{6}(r-1)r(4r+7)$ Correct expansion in any form, eg	M1			
	$\frac{1}{6}r(4r^2+15r+11-4r^2-3r+7)$	A1			
	= r(2r+3)	A1	3	AG	
(b)	Attempt to use method of differences $S_{100} = u_{100} - u_0$ = 691850	M1 A1 A1	3	САО	
	Total		6		
3 (a)	$(1+i)^2 = 2i \text{ or } (1+i) = \sqrt{2} e^{\frac{\pi i}{4}}$	B1	2		
	21(1+1) = 21 - 2	BI	2	AG Alternative method: $(1+i)^3 = 1 + 3i + 3i^2 + i^3$ B1 = 2i - 2 B1	
(b)(i)	Substitute $z = 1 + i$ Correct expansion k = -5	M1 A1 A1	3	allow for correctly picking out either the real or the imaginary parts	
(ii)	$\beta + \gamma = 5 + i - \alpha = 4$	B1	1	AG	
(iii)	$\alpha\beta\gamma = 5(1+i)$ $\beta\gamma = 5$	M1 A1F		allow if sign error ft incorrect <i>k</i>	
	$z^{2} - 4z + 5 = 0$ Use of formula or $(z - 2)^{2} = -1$ $z = 2 \pm i$ NB allow marks for (b) in whatever order they appear	M1 A1F A1F	5	No ft for real roots if error in <i>k</i>	
	Total		11		

MFP2 (cont)					
Q	Solution	Marks	Total	Comments	
4 (a)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 12\sinh x - 8\cosh x - 1$	B1		The B1 and M1 could be in reverse order if put in terms of e first	
	$12\frac{(e^{x}-e^{-x})}{2}-8\frac{(e^{x}+e^{-x})}{2}-1=0$	M1		M0 if $\sinh x$ and $\cosh x$ in terms of e^x are interchanged	
	$2e^{2x} - e^{x} - 10 = 0$	A1F		ft slips of sign	
	$(2e^{x}-5)(e^{x}+2)=0$	M1A1F		ft provided quadratic factorises	
	$e^x \neq -2$	E1		some indication of rejection needed	
	$x = \ln \frac{5}{2}$ one stationary point	A1F	7	Condone $e^x = \frac{5}{2}$ with statement provided	
				quadratic factorises	
				Special Case	
				If $\frac{dy}{dx} = 12 \sinh x - 8 \cosh x$ B0	
				For substitution in terms of e^x M1	
				leading to $e^{2x} = 5$ A1	
				Then M0	
(b)	$b = 12 \frac{\left(\frac{5}{2} + \frac{2}{5}\right)}{2} - 8 \frac{\left(\frac{5}{2} - \frac{2}{5}\right)}{2} - \ln \frac{5}{2}$	M1A1F		for substitution into original equation	
	$=\frac{174}{10}-\frac{84}{10}-\ln\frac{5}{2}$	A1		CAO	
	=9-a	A1	4	AG; accept $b = 9 - a$	
	Total		11		
5(a)	$\frac{du}{dx} = \frac{1}{2} \left(1 - x^2 \right)^{-\frac{1}{2}}$	B1			
	$\times (-2x)$	B1	2		
(b)	$\int \sin^{-1} x dx = x \sin^{-1} x - \int \frac{x}{\sqrt{1 - x^2}} dx$	M1 A1A1		A1 for each part of the integration by parts	
	$\int -\frac{x}{\sqrt{1-x^2}} \mathrm{d}x = \sqrt{1-x^2} \mathrm{used}$	A1F		ft sign error in $\frac{\mathrm{d}u}{\mathrm{d}x}$	
	$\frac{\sqrt{3}}{2}\frac{\pi}{3} + \sqrt{1 - \frac{3}{4}} - 1$	m1		substitution of limits	
	$\frac{1}{6}\sqrt{3}\pi - \frac{1}{2}$	A1	6	CAO	
	Total		8		

MFP2 (cont)			
Q	Solution	Marks	Total	Comments
6(a)	$\frac{\mathrm{d}x}{\mathrm{d}t} = \sec t - \cos t$	B1,B1		use of FB for sec <i>t</i> ; if done from first principles, allow B1 when sec <i>t</i> is arrived at
	Use of $1 - \cos^2 t = \sin^2 t$	M1		
	$\frac{\mathrm{d}x}{\mathrm{d}t} = \sin t \tan t$	A1	4	AG
(b)	$\dot{x}^2 + \dot{y}^2 = \sin^2 t \tan^2 t + \sin^2 t$	M1A1		sign error in $\frac{dy}{dt}$ A0
	Use of $1 + \tan^2 t = \sec^2 t$	m1		
	$\sqrt{\dot{x}^2 + \dot{y}^2} = \tan t$	A1F		ft sign error in $\frac{dy}{dt}$
	$\int_{0}^{\frac{\pi}{3}} \tan t dt = \left[\ln \sec t\right]_{0}^{\frac{\pi}{3}}$	A1F		ft sign error in $\frac{dy}{dt}$
	$=\ln 2$	A1	6	CAO
	Total		10	
7(a)	f(k+1) - 5f(k)			
	$=12^{k+1}+2\times 5^{k}-5(12^{k}+2\times 5^{k-1})$	M1		
	$=12^{k+1} + 2 \times 5^{k} - 5 \times 12^{k} - 2 \times 5^{k}$	A1		for expansion of bracket $5 \times 5^{k-1} = 5^k$ used
	$=12\times12^{k}-5\times12^{k}=7\times12^{k}$	A1	3	clearly shown
(b)	Assume $f(k) = M(7)$			
	Then $f(k+1) = 5f(k) + M(7)$	M1		Not merely a repetition of part (a)
	=M(7)	A1		clearly shown
	f(1) = 12 + 2 = 14 = M(7)	B1		
	Correct inductive process	E1	4	(award only if all 3 previous marks earned)
	Total		7	

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MFP2 (cont)				
Q	Solution	Marks	Total	Comments
8(a)(i)	$4\left(1+i\sqrt{3}\right) = 8\left(\frac{1}{2}+i\frac{\sqrt{3}}{2}\right)$	M1		for either $4(1+i\sqrt{3})$ or $4(1-i\sqrt{3})$ used
	$=8e^{\frac{\pi i}{3}}$	A1		If either $r \text{ or } \theta$ is incorrect but the same value in both (i) and (ii) allow A1 but for θ only if it is given as $\frac{\pi}{6}$
(ii)	$4\left(1-i\sqrt{3}\right)=8e^{\frac{-\pi i}{3}}$	A1	3	
(b)	$z^3 - 4 = \pm \sqrt{-48}$	M1		taking square root
	$z^3 = 4 \pm 4\sqrt{3}i$	A1	2	AG
(c)(i)	$z = 2e^{\frac{\pi i}{3} + 2k\pi i}$ or $z = 2e^{\frac{-\pi i}{3} + 2k\pi i}$	B1F M1		for the 2; ft incorrect 8, but no decimals for either, PI
(ii)	$z = 2e^{\frac{\pi i}{9}}, 2e^{\frac{7\pi i}{9}}, 2e^{\frac{5\pi i}{9}}$ $= 2e^{\frac{-\pi i}{9}}, 2e^{\frac{-7\pi i}{9}}, 2e^{\frac{-5\pi i}{9}}$ Radius 2 Plotting roots	A3,2,1F B1F B2,1	5	Allow A1 for any 2 roots not +/- each other Allow A2 for any 3 roots not +/- each other Allow A3 for all 6 correct roots Deduct A1 for each incorrect root in the interval; ignore roots outside the interval ft incorrect <i>r</i> clearly indicated; ft incorrect <i>r</i> allow B1 for 3 correct points condone lines
(d)(i)	Sum of roots = 0 as coefficient of $z^5 = 0$	E1	1	OE
(ii)	Use of, say, $\frac{1}{2} \left(e^{\frac{\pi i}{9}} + e^{\frac{-\pi i}{9}} \right) = \cos \frac{\pi}{9}$	M1		
	$\cos\frac{3\pi}{9} = \frac{1}{2}$ used	A1		
	$\cos\frac{\pi}{9} + \cos\frac{3\pi}{9} + \cos\frac{5\pi}{9} + \cos\frac{7\pi}{9} = \frac{1}{2}$	A1	3	AG
	Total		17	
	TOTAL		75	