



General Certificate of Education

Mathematics 6360

MPC2 Pure Core 2

Mark Scheme

2010 examination - January series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available to download from the AQA Website: www.aqa.org.uk

Copyright © 2010 AQA and its licensors. All rights reserved.

COPYRIGHT

AQA retains the copyright on all its publications. However, registered centres for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to centres to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Set and published by the Assessment and Qualifications Alliance.

The Assessment and Qualifications Alliance (AQA) is a company limited by guarantee registered in England and Wales (company number 3644723) and a registered charity (registered charity number 1073334). Registered address: AQA, Devas Street, Manchester M15 6EX Dr Michael Cresswell Director General

Key to mark scheme and abbreviations used in marking

| М | mark is for method | | | | | | |
|------------|--|---|----------------------------|--|--|--|--|
| m or dM | mark is dependent on one or more M marks and is for method | | | | | | |
| А | mark is dependent on M or m marks and is for accuracy | | | | | | |
| В | mark is independent of M or m marks and is for method and accuracy | | | | | | |
| E | mark is for explanation | | | | | | |
| | | | | | | | |
| or ft or F | follow through from previous | | | | | | |
| | incorrect result | MC | mis-copy | | | | |
| CAO | correct answer only | MR | mis-read | | | | |
| CSO | correct solution only | RA | required accuracy | | | | |
| AWFW | anything which falls within | anything which falls within FW further work | | | | | |
| AWRT | anything which rounds to ISW ignore subsequent work | | | | | | |
| ACF | any correct form | FIW | from incorrect work | | | | |
| AG | answer given | BOD | given benefit of doubt | | | | |
| SC | special case | WR | work replaced by candidate | | | | |
| OE | or equivalent | FB | formulae book | | | | |
| A2,1 | 2 or 1 (or 0) accuracy marks | NOS | not on scheme | | | | |
| –x EE | deduct <i>x</i> marks for each error | G | graph | | | | |
| NMS | no method shown | с | candidate | | | | |
| PI | possibly implied | sf | significant figure(s) | | | | |
| SCA | substantially correct approach | dp | decimal place(s) | | | | |

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

| QSolutionMarksTotalCommentsI(a)(i)[Area of sector =] $\frac{1}{2}r^2\theta$ M1Stated or explicitly used $= \frac{1}{2} \times 15^2 \times 1.2 = 135 (cm^2)$ A12AG Must see some substitution(ii)(Are =) $r\theta$ M12(b) $PB = 5$ (cm)B1Accept even if only on a diagram or within an expression for the perimeter $(AP^2 =) 15^2 + 10^2 - 2 \times 15 \times 10 \cos 1.2$ m1RHS of cosine rule used $(AP^2 =) 15^2 + 10^2 - 2 \times 15 \times 10 \cos 1.2$ m1Correct oder of evaluation PT $A1 = 2$ M1PI $AP^2 = 4, 7,008$ m1APerimeter $= 5 + 18 + 14, 7, = 37.7$ (cm)A15 $A1 = 5$ Soft obetterStated or exet (blow through on non-integer X) PT $Total$ 92(a) $\sqrt{x^5} = x^{\frac{3}{2}}$ B11Accept $k = 2.5$ Index 'k' raised by 1 in integrating x^8 T'' term correct follow through on non-integer X For $-4x$ as integral of -4 $y = 2x^{2^3} - 4x + c$ (*)B1F $y = c^*$ sanswer to (b) with '+ c' $(y = 2x^{3^3} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include ' $y = '$ $y = 2x^{3^3} - 4x + 5$ A13Accept $c = 5$ after correct logn * which must include ' $y = '$ (b) $\log_a n^2 = \log_a 18(n-4)$ M1A valid law of logs applied to correct log A second valid law of logs applied to correct log A second valid law of logs applied to correct log A second valid law of logs applied to correct logs $n = -12$ A15Both va | MPC2 | | | | |
|---|-----------------|---|-------|-------|--|
| $ \begin{array}{ c c c c c c c c c c c c c c c c c c c$ | | Solution | Marks | Total | Comments |
| $\begin{array}{ c c c c c c c c c c c c c c c c c c c$ | 1(a)(i) | {Area of sector =} $\frac{1}{2}r^2\theta$ | M1 | | Stated or explicitly used |
| $\begin{array}{c c c c c c c c c c c c c c c c c c c $ | | $=\frac{1}{2}\times 15^2\times 1.2 = 135 \text{ (cm}^2)$ | A1 | 2 | AG Must see some substitution |
| (b) $PB = 5 \text{ (cm)}$ B1Accept even if only on a diagram or within an expression for the perimeter RHS of cosine rule used Correct order of evaluation PI eg within an expression for perimeter 3sf or better $AP = 14.7(068)$ $A1$ P Perimeter = $5 + 18 + 14.7 = 37.7 (cm)$ $A1$ P $2(a)$ $\sqrt{x^3} = x^2$ $B1$ 1 $\sqrt{x^5} = x^2$ $B1$ 1 Accept $k = 2.5$ (b) $\int (7\sqrt{x^5} - 4) dx = \frac{7}{3.5}x^{3.5} - 4x (+c)$ $M1$ A1F B1 $A1F$ 1^* term correct follow through on non- integer k (c) $y = 2x^{3.5} - 4x + c$ $(*)$ $B1F$ $y = c^*$ answer to (b) with $* + c^*$ $(*) = *P1$ by next line)When $x = 1, y = 3 \Rightarrow 3 = 2 - 4 + c$ M1 $Subst. (1, 3)$ in attempt to find constant o integration $y = 2x^{3.5} - 4x + 5$ A13 (a) $(x =)$ $B1$ 1 (a) $(x =)$ $B1$ (a) (b) (a) | (ii) | | | | PI |
| (b) $PS = 3$ (cm)B1within an expression for the perimeter $(AP^2 =) 15^2 + 10^2 - 2 \times 15 \times 10 \cos 1.2$ M1RHS of cosine rule used $= 325 - 300\cos 1.2 = 216.2926$ m1Correct of cf valuation $AP = 14.7(068)$ A15Perimeter $= 5 + 18 + 14.7 = 37.7$ (cm)A15 Total 92(a) $\sqrt{x^5} = x^2$ B11 $Accept k = 2.5$ M1Index 'k' raised by 1 in integrating x^k (b) $\int (7\sqrt{x^5} - 4) dx = \frac{7}{3.5}x^{35} - 4x (+c)$ M1Index 'k' raised by 1 in integrating x^k B13For $-4x$ as integral of -4 Y = c's answer to (b) with '+ c'(c) $y = 2x^{3.5} - 4x + c$ (*)B1FY = c's answer to (b) with '+ c' $y = 2x^{3.5} - 4x + 5$ A13Subst. (1, 3) in attempt to find constant o $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which $y = 2x^{3.5} - 4x + 5$ A1A1Accept $c = 5$ after correct eqn * which $y = 2x^{3.5} - 4x + 5$ A1A1Accept $c = 5$ after correct eqn * which $y = 2x^{3.5} - 4x + 5$ A1A1Accept $c = 5$ after correct eqn * which $y = 2x^{3.5} - 4x + 5$ A1A1Accept $c = 5$ after correct eqn * which $y = 2x^{3.5} - 4x + 5$ | | = 18 (cm) | A1 | 2 | |
| $\begin{array}{ c c c c c c c c c c c c c c c c c c c$ | (b) | $PB = 5 (\mathrm{cm})$ | B1 | | |
| $AP = 14.7(068)$ Perimeter $= 5 + 18 + 14.7 = 37.7 (cm)$ A1 A1PI eg within an expression for perimeter 3st or betterTotalTotal9Z(a) $\sqrt{x^5} = x^{\frac{5}{2}}$ B11Accept $k = 2.5$ (b) $\int (7\sqrt{x^2} - 4) dx = \frac{7}{3.5}x^{x^3} - 4x (+c)$ M1 A1F A1F B1Index 'k' raised by 1 in integrating x^k 1" term corect follow through on non- integer k (c) $y = 2x^{3.5} - 4x + c$ (*)B1F $y = c'$ s answer to (b) with '+ c' ('y =' PI by next line)When $x = 1$, $y = 3 \Rightarrow 3 = 2 - 4 + c$ M1Subst. (1, 3) in attempt to find constant o integration $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include 'y =' Coefficients must be tidiedWhen $x = 1$, $y = 3 \Rightarrow 3 = 2 - 4 + c$ M1Subst. (1, 3) in attempt to find constant o integration $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include 'y =' Coefficients must be tidiedTotal7(ii) $(x =) 1$ B11CAO(iii) $(x =) 3$ B11CAO(b) $\log_a n^2 = \log_a 18(n-4)$ M1 M1A valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ A15Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | | ${AP^{2} =} 15^{2} + 10^{2} - 2 \times 15 \times 10 \cos 1.2$ | M1 | | RHS of cosine rule used |
| Perimeter = 5 + 18 + 14.7 = 37.7 (cm)A153st or betterTotal92(a) $\sqrt{x^5} = x^{\frac{5}{2}}$ B11Accept $k = 2.5$ (b) $\int (7\sqrt{x^5} - 4) dx = \frac{7}{3.5}x^{35} - 4x (+ c)$ M1 A1F B1Index 'k' raised by 1 in integrating x^t 1" term correct follow through on non- integer k (c) $y = 2x^{35} - 4x + c$ (*)B1F $y = c$'s answer to (b) with '+ c' ('y =' PI by next line)When $x = 1$, $y = 3 \Rightarrow 3 = 2 - 4 + c$ M1Subst. (1, 3) in attempt to find constant o integration $y = 2x^{35} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include 'y =' Coefficients must be tidiedTotal73(a)(i)(x =) 1B11CAO(b) $\log_a n^2 = \log_a 18(n-4)$ M1 M1A valid law of logs applied to correct log A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ A15Both values required SC NXB max (out of 5) B3 for both 6 and 12 without uniqueness considered; must 21 without uniqueness considered; must 21 without uniqueness considered; must 21 without uniqueness considered; must 21 only | | | | | |
| Total92(a) $\sqrt{x^5} = x^2$ B11Accept $k = 2.5$ (b) $\int (7\sqrt{x^3} - 4) dx = \frac{7}{3.5}x^{3.5} - 4x (+ c)$ M1 A1FIndex 'k' raised by 1 in integrating x^k 1^{16} term correct follow through on non- integr k For $-4x$ as integral of -4 (c) $y = 2x^{3.5} - 4x + c$ (*)B1F $y = c$'s answer to (b) with '+ c' ('y =' PI by next line)When $x = 1, y = 3 \Rightarrow 3 = 2 - 4 + c$ M1Subst. (1, 3) in attempt to find constant o integration $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include 'y =' Coefficients must be tidied $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include 'y =' Coefficients must be tidied $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include 'y =' Coefficients must be tidied $y = 2x^{3.5} - 4x + 5$ A1B11CAO(ii) $(x =) 1$ B11CAO(b) $\log_n n^2 = \log_n 18(n - 4)$ M1 M1A valid law of logs applied to correct log A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ A1ACF of these terms eg $n^2 - 18n = -72$ $(n - 6)(n - 12) = 0$ m1Valid method to solve quadratic, dep on both the previous Ms $n = 6, n = 12$ A15Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | | | | 5 | |
| $ \begin{aligned} \textbf{(b)} & \int \left(7\sqrt{x^5} - 4\right) dx = \frac{7}{3.5}x^{3.5} - 4x \ (+c) \\ & \text{M1} \\ \text{A1F} \\ & \text{B1} \\ \textbf{(c)} & y = 2x^{3.5} - 4x + c \\ & (*) \\ & \text{When } x = 1, \ y = 3 \Rightarrow 3 = 2 - 4 + c \\ & \text{W1} \\ & y = 2x^{3.5} - 4x + 5 \\ & \text{M1} \\ & y = 2x^{3.5} - 4x + 5 \\ & \text{M1} \\ & y = 2x^{3.5} - 4x + 5 \\ & \text{M1} \\ & y = 2x^{3.5} - 4x + 5 \\ & \text{M1} \\ & y = 2x^{3.5} - 4x + 5 \\ & \text{M1} \\ & $ | | | AI | | |
| Integer k B1B13Integer k For - 4x as integral of -4(c) $y = 2x^{3.5} - 4x + c$ (*)B1F $y = c$'s answer to (b) with '+ c' ('y =' PI by next line)When $x = 1, y = 3 \Rightarrow 3 = 2 - 4 + c$ M1Subst. (1, 3) in attempt to find constant or integration $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include 'y =' Coefficients must be tidiedTotal73(a)(i) $(x =) 1$ B11(ii) $(x =) 3$ B11(b) $\log_a n^2 = \log_a 18(n-4)$ M1 M1A valid law of logs applied to correct logs A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ A1ACF of these terms eg $n^2 - 18n = -72$ $(n - 6)(n - 12) = 0$ m1Valid method to solve quadratic, dep on both the previous Ms $n = 6, n = 12$ A15Both values required sc NM max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | | | B1 | 1 | Accept $k = 2.5$ |
| B13For $-4x$ as integral of -4 (c) $y = 2x^{3.5} - 4x + c$ (*)B1F $y = c$'s answer to (b) with '+ c' ('y =' PI by next line)When $x = 1, y = 3 \Rightarrow 3 = 2 - 4 + c$ M1Subst. (1, 3) in attempt to find constant or integration $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include 'y =' Coefficients must be tidiedTotal73(a)(i) $(x =) 1$ B11(ii) $(x =) 3$ B11(b) $\log_a n^2 = \log_a 18(n-4)$ M1 M1A valid law of logs applied to correct log A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ $(n-6)(n-12) = 0$ M1 M1ACF of these terms eg $n^2 - 18n = -72$ $n = 6, n = 12$ A15Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | (b) | $\int \left(7\sqrt{x^5} - 4\right) dx = \frac{7}{3.5}x^{3.5} - 4x \ (+c)$ | | | 1 st term correct follow through on non- |
| When $x = 1, y = 3 \Rightarrow 3 = 2 - 4 + c$ M1('y =' PI by next line) $y = 2x^{3.5} - 4x + 5$ A13Subst. (1, 3) in attempt to find constant or integration $y = 2x^{3.5} - 4x + 5$ A13Accept $c = 5$ after correct eqn * which must include 'y =' Coefficients must be tidied Total 7 3(a)(i) $(x =) 1$ B11(ii) $(x =) 3$ B11(b) $\log_a n^2 = \log_a 18(n-4)$ M1A valid law of logs applied to correct log A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ A1ACF of these terms eg $n^2 - 18n = -72$ $(n-6)(n-12) = 0$ m1Valid method to solve quadratic, dep on both the previous Ms $n = 6, n = 12$ A15Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | | | B1 | 3 | |
| $y = 2x^{3.5} - 4x + 5$ A13integrationintegrationTotal3Accept $c = 5$ after correct eqn * which must include ' $y =$ ' Coefficients must be tidiedTotal73(a)(i) $(x =) 1$ B11CAO(ii) $(x =) 3$ B11CAO(b) $\log_a n^2 = \log_a 18(n-4)$ M1 M1A valid law of logs applied to correct log A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ A1ACF of these terms eg $n^2 - 18n = -72$ $(n-6)(n-12) = 0$ m1Valid method to solve quadratic, dep on both the previous Ms $n = 6, n = 12$ A15Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | (c) | $y = 2x^{3.5} - 4x + c \qquad (*)$ | B1F | | |
| Image: Solution of the previous MsImage: Solution of the previous Ms <th></th> <th>When $x = 1$, $y = 3 \implies 3 = 2 - 4 + c$</th> <th>M1</th> <th></th> <th>Subst. (1, 3) in attempt to find constant of integration</th> | | When $x = 1$, $y = 3 \implies 3 = 2 - 4 + c$ | M1 | | Subst. (1, 3) in attempt to find constant of integration |
| Total7 $3(a)(i)$ $(x =) 1$ B11CAO(ii) $(x =) 3$ B11CAO(b) $\log_a n^2 = \log_a 18(n-4)$ M1A valid law of logs applied to correct log A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ A1ACF of these terms eg $n^2 - 18n = -72$ $(n-6)(n-12) = 0$ m1Valid method to solve quadratic, dep on both the previous Ms $n = 6, n = 12$ A15Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | | $y = 2x^{3.5} - 4x + 5$ | A1 | 3 | must include 'y =' |
| $3(a)(i)$ $(x =) 1$ $B1$ 1 CAO (ii) $(x =) 3$ $B1$ 1 CAO (b) $\log_a n^2 = \log_a 18(n-4)$ $M1$ $M1$ A valid law of logs applied to correct log A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ $A1$ $A1$ ACF of these terms eg $n^2 - 18n = -72$ $(n-6)(n-12) = 0$ $m1$ $A1$ 5 Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | | Total | | 7 | |
| (b) $\log_a n^2 = \log_a 18(n-4)$ M1 M1A valid law of logs applied to correct log A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ A1ACF of these terms eg $n^2 - 18n = -72$ $(n-6)(n-12) = 0$ m1Valid method to solve quadratic, dep on both the previous Ms $n = 6, n = 12$ A15Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | 3 (a)(i) | | B1 | | CAO |
| C_a C_a C_a M_1 A second valid law of logs applied to correct logs $n^2 - 18n + 72 = 0$ A1ACF of these terms eg $n^2 - 18n = -72$ $(n-6)(n-12) = 0$ m1Valid method to solve quadratic, dep on both the previous Ms $n = 6, n = 12$ A15Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | (ii) | (x =) 3 | B1 | 1 | CAO |
| (n-6)(n-12) = 0 $n = 6, n = 12$ $n = 12$ n | (b) | $\log_a n^2 = \log_a 18(n-4)$ | | | ÷ |
| n = 6, n = 12A15both the previous MsA15Both values required SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | | $n^2 - 18n + 72 = 0$ | A1 | | ACF of these terms eg $n^2 - 18n = -72$ |
| SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; max B1 for either 6 or 12 only | | (n-6)(n-12) = 0 | m1 | | A A |
| | | n = 6, n = 12 | A1 | 5 | SC NMS max (out of 5) B3 for both 6 and 12 without uniqueness considered; |
| Total 7 | | Total | | 7 | |

| MPC2 (cont) | | 26.1 | T () | a |
|-----------------------|--|-------|--------------|---|
| Q | Solution | Marks | Total | Comments |
| 4 (a) | $\{S_{31} = \} \frac{31}{2} [2a + (31 - 1)d]$ | M1 | | |
| | 31(a+15d) = 310 | m1 | | Forming eqn and eliminating fraction or bracket |
| | a + 15d = 310/31; a + 15d = 10 | A1 | 3 | AG Completion to printed answer |
| (b) | a + (21 - 1)d = 2[a + (16 - 1)d] | M1 | | a + (n-1)d used for at least one term |
| | $\Rightarrow a = -10d; \Rightarrow -10d + 15d = 10$ | m1 | | Solving $a + 15d = 10$ simultaneously with an eqn in a and d obtained from a+20d = k[a+15d] with $k=2$ or with $k=1/2$ |
| | <i>d</i> = 2 | A1 | 3 | |
| (c) | $u_1 = a = -20$ | B1F | | ft on c's value for d in $a + 15d = 10$ or in another correct (dep on m1) equation in a and $dThe value for a must appear within c'ssoln for (c)$ |
| | $\sum_{n=1}^{k} u_n = S_k = \frac{k}{2} [2a + (k-1)d]$ | M1 | | Condone n for k in M1 and A1F lines provided n replaced by k at a later stage |
| | $\frac{k}{2}[-40+2k-2] = 0$ | A1F | | '= 0' can be implied by later line; ft on c's non-zero values for a and d |
| | <i>k</i> = 21 | A1 | 4 | Condone presence of $k = 0$ SC NMS $k = 21$ and with $d = 2$ found earlier award B2. If $k = 21$ but never see d = 2, award $0/4$ |
| | Total | | 10 | |

| | MPC2 (cont) | | | | | | |
|------|--|-------|-------|--|--|--|--|
| Q | Solution | Marks | Total | Comments | | | |
| 5(a) | $\frac{1}{x^3} = x^{-3}$ | B1 | | PI by its correct derivative | | | |
| | $\frac{\mathrm{d}y}{\mathrm{d}x} = -3x^{-4} + 48$ | M1 | | A power decreased by 1; could be the +48 or the ft after B0 | | | |
| | | A1 | 3 | | | | |
| (b) | $-3x^{-4} + 48 = 0$ $x^{-4} = 16$ | M1 | | c's answer to (a) equated to 0 | | | |
| | $x^{-4} = 16$ | A1F | | To $x^p = q$ but only ft on eqns of the form $ax^{2k} + 48 = 0$, where <i>a</i> and <i>k</i> are negative integers | | | |
| | $x = \pm \frac{1}{2}$ | A1 | | | | | |
| | Eqns of tangents: $y = 32$ and $y = -32$ | A1F | 4 | Only ft if answer is of the form $y = \pm k$ | | | |
| (c) | When $x = 1$, $\frac{dy}{dx} = -3 + 48 = 45$ | M1 | | Attempt to find value of $\frac{dy}{dx}$ at $x = 1$ | | | |
| | Gradient of normal at (1, 49) is $-\frac{1}{45}$ | m1 | | Correct use of $m \times m' = -1$ with c's value of $\frac{dy}{dx}$ when $x = 1$ | | | |
| | Normal at (1, 49): $y - 49 = -\frac{1}{45}(x - 1)$ | A1 | 3 | CSO. Apply ISW after ACF; accept 49.02 or better in place of $49\frac{1}{45}$ | | | |
| | Total | | 10 | | | | |

| MPC2 (cont) | | | | | | |
|---------------|---|----------|-------|--|--|--|
| Q | Solution | Marks | Total | Comments | | |
| 6(a) | (0, 1) | B1 B1 | 2 | Shape with some indication of asymptotic behaviour in 2nd quadrant below pt of intersection with <i>y</i>-axis Only intersection is with <i>y</i>-axis at (0, 1) stated/indicated (accept 1 on <i>y</i>-axis as equivalent) | | |
| (b)(i) | $h = 0.5$ $f(x) = 2^x$ | B1 | | PI | | |
| | $I \approx h/2\{\}$ {} = f(0)+f(2)+2[f(0.5)+f(1)+f(1.5)] | M1 | | OE summing of areas of the 4 'trapezia' | | |
| | $\{\ldots\} = 1 + 4 + 2(\sqrt{2} + 2 + \sqrt{8}) \\ = 5 + 2 \times 6.2426 = 17.485$ | A1 | | OE Accept 2dp (rounded or truncated) as evidence for surds | | |
| | $(I \approx)$ 4.3713 = 4.37 (to 3sf) | A1 | 4 | CAO Must be 4.37 SC for those who use 5 strips, max possible is B0M1A1A0 | | |
| (ii) | Increase the number of ordinates | E1 | 1 | OE | | |
| (c) | Translation; | B1; | | Accept 'translat' as equivalent [T or Tr is NOT sufficient] | | |
| | $\begin{bmatrix} -7\\3 \end{bmatrix}$ | B1;B1 | 3 | B1 for each component of the vector. Condone if the equiv 2 vectors are given. Accept full equivalent to vector(s) in words provided linked to 'translation/ move/shift' and correct directions. (No marks if different transformations) | | |
| (d) | $8 = 2^k + 3 \implies 2^k = 5$ | M1 | | Correct subst. and an attempted rearrangement to $2^k = N$. PI by $k = \frac{\log 5}{\log 2}$ | | |
| | $k = \log_2 5$ | A1 | 2 | Accept $m = 2, n = 5$ | | |
| | Total | | 12 | | | |

| MPC2 (cont | MPC2 (cont) | | | | | |
|------------|---|--------|-------|--|--|--|
| Q | Solution | Marks | Total | Comments | | |
| 7(a) | $(1+2x)^{7} = 1 + {\binom{7}{1}}(2x)^{1} + {\binom{7}{2}}(2x)^{2} + {\binom{7}{3}}(2x)^{3} +$ | M1 | | Any valid method. PI by a correct value for either a or b or c | | |
| | $= 1 + 14x + 84x^{2} + 280x^{3} + \dots$ {a = 14, b = 84, c = 280} | A1 × 3 | 4 | A1 for each of a, b, c SC $a = 7, b = 21, c = 35$ either explicitly or within expn (M1A0) | | |
| (b) | $\left(1 - \frac{1}{2}x\right)^2 = 1 - x + \frac{1}{4}x^2$ | B1 | | Correct expansion stated explicitly or used later | | |
| | x^{3} terms from expn of $\left(1-\frac{1}{2}x\right)^{2}\left(1+2x\right)^{7}$ are cx^{3} and $-x(bx^{2})$ and $\frac{1}{4}x^{2}(ax)$ | M1 | | Any one of the three, or ft on c's non-zero values for a, b or c . Must be from products of terms using c's two expansions | | |
| | $cx^3 - x(bx^2) + \frac{1}{4}x^2(ax)$ | A1F | | ft c's two expansions provided all three combinations of terms are present | | |
| | Coefficient of x^3 is $c - b + 0.25a = 199.5$ | A1 | 4 | OE eg 399/2 Condone $199.5x^3$ | | |
| | Total | | 8 | | | |

| MPC2 | (cont) |
|------|--------|
| | |

| Q | Solution | Marks | Total | Comments |
|---------------|--|-------|-------|---|
| 8 (a) | $x + 52^{\circ} = (22^{\circ}), 180^{\circ} + 22^{\circ}; 360^{\circ} + 22^{\circ}$ | M1;M1 | | x + 52 = 180 + AWRT 22, 360 + AWRT 22 OE |
| | (x = 180 + 22 - 52; x = 360 + 22 - 52) | | | (max of M1 if extras in range) LHS could be any letter but not <i>x</i> unless |
| | | | | final answer shows recovery |
| | | | | Ms can be PI |
| | | | | |
| | $x = 150^{\circ}$, 330° | A1 | 3 | Both CAO with no extras in $0^{\circ} \le x \le 360^{\circ}$ |
| | | | | Ignore anything outside $0^\circ \le x \le 360^\circ$ |
| | $2\tan\theta = \frac{8}{2} \Rightarrow 2\sin\theta = 8$ | M1 | | $\sin \theta$ $\sin \theta$ |
| (b)(i) | $3 \tan \theta = \frac{8}{\sin \theta} \implies 3 \frac{\sin \theta}{\cos \theta} = \frac{8}{\sin \theta}$ | M1 | | $\tan \theta = \frac{\sin \theta}{\cos \theta} \text{used/seen}$ |
| | $\frac{3(1-\cos^2\theta)}{\cos\theta} = 8$ | M1 | | $\sin^2\theta = 1 - \cos^2\theta$ used |
| | | WII | | $\sin \theta = 1 \cos \theta$ used |
| | $\Rightarrow 3 - 3\cos^2\theta = 8\cos\theta$ | | | |
| | $\Rightarrow 3\cos^2\theta + 8\cos\theta - 3 = 0$ | A1 | 3 | CSO AG Completion |
| (ii) | $(3\cos\theta - 1)(\cos\theta + 3) = 0$ | M1 | | Any valid method to solve the quadratic |
| | $\cos\theta = \frac{1}{3}$ | A1 | 2 | CSO Must only be the one value |
| | 3 | | | |
| | . 1 | | | Using (ii) OE to get or use $\cos 2x = k$ |
| (iii) | $\cos 2x = \frac{1}{3}$ | M1 | | where $-1 \le k \le 1$ |
| | | | | |
| | (2x =) 70.528 | B1 | | Award for $\cos^{-1}(1/3) =$ value from 70 to |
| | | | | 71 inclusive, even if θ used. PI |
| | $2x = 360^{\circ} - 70.528 (= 289.47)$ | m1 | | $2x = 360 - \cos^{-1}(c's k)$ OE |
| | | | | No extras inside the range |
| | $x = 35^{\circ}$, 145° (to the nearest degree) | A1 | 4 | Both, condoning greater accuracy, with |
| | | | • | no extras in $0^{\circ} \le x \le 180^{\circ}$ |
| | | | | Ignore anything outside $0^{\circ} \le x \le 180^{\circ}$ |
| | | | | SC for (b)(iii) only when c's answer for |
| | | | | (b)(ii) is $\cos\theta = -\frac{1}{3}$: |
| | | | | max mark M1B1 (val 70-71 or val |
| | | | | 109-110 inclusive) m1A0 |
| | Total | | 12 | |
| | TOTAL | | 75 | |