[^0]| 1 | （i） | Method is biased because many pupils cannot be chosen | $\begin{array}{ll} \hline \text { B1 } \\ & \\ \hline \end{array}$ | ＂Biased＂or equivalent stated，allow＂not random＂ Valid relevant reason |
| :---: | :---: | :---: | :---: | :---: |
|  | （ii） | Allocate a number to each pupil Select using random numbers | $\begin{array}{ll}  & \\ \text { B1 } & \\ \text { B1 } & \\ \hline \end{array}$ | State＂list numbered＂ <br> Use random numbers［not＂hat＂］ |
| 2 |  | $\begin{aligned} & \frac{20-25}{\sigma}=\Phi^{-1}(0.25)=-0.674 \\ & \sigma=5 \div 0.674 \\ & \quad=7.42 \end{aligned}$ | M1  <br> B1  <br> M1  <br> A1 4 | Standardise and equate to $\Phi^{-1} \quad$［not ． 7754 or ．5987］ $z$ in range［ $-0.675,-0.674]$ ，allow + <br> （ $\pm$ ） $5 \div z$－value［not $\Phi(z)$ or 0.75 ］ Answer in range［7．41，7．42］，no sign fudges <br> ［SR：$\quad \sigma^{2}: \quad$ M1B1M0A0 <br> cc：M1B1M1A0］ |
| 3 | （a） | $\operatorname{Po}(1.2)$ <br> Tables or correct formula used $0.8795$ | $\begin{array}{\|ll\|} \hline \text { B1 } & \\ \text { M1 } & \\ \text { A1 } & 3 \\ \hline \end{array}$ | Po（1．2）stated or implied Correct method for Poisson probability，allow＂ 1 －＂ Answer， 0.8795 or 0.879 or $0.88(0)$ |
|  |  | $\begin{aligned} & \left.\left.\begin{array}{l} \mathrm{N}(30,30) \\ \frac{38.5-30}{\sqrt{30}} \end{array}\right]=1.55\right] \\ & {[\Phi(1.55)=]} \end{aligned}$ | B1  <br> B1  <br> M1  <br> A1  <br> A1 $\mathbf{5}$ | Normal，mean 30 stated or implied <br> Variance 30 stated or implied，allow $\sqrt{ } 30$ or $30^{2}$ <br> Standardise using $\sigma^{2}=\mu$ ，allow $\sqrt{ }$ or cc errors <br> $\sqrt{ } \mu$ and 38.5 both correct <br> Answer in range［0．939，0．94（0）］ |
| 4 | （i） | $\hat{\sigma}^{2}=\frac{50}{49} \times 0.0967=0.0987$ | $\begin{array}{\|ll\|} \hline \text { M1 } & \\ \text { A1 } & 2 \\ \hline \end{array}$ | Use $\frac{n}{n-1} \times s$ or $s^{2}$ ，allow $\sqrt{ }$ Answer，a．r．t． 0.0987 |
|  | （ii） <br> $\alpha, \beta:$ <br> $\alpha$ ： | $\mathrm{H}_{0}: \mu=1.8, \mathrm{H}_{1}: \mu \neq 1.8$ <br> where $\mu$ is the population mean $\begin{aligned} & z=\frac{(1.72-1.8)}{\hat{\sigma} / \sqrt{50}}=-1.8(006) \\ & -1.8<-1.645 \end{aligned}$ | B1B1 <br> M1 <br> A1 <br> B1 $\sqrt{ }$ | Hypotheses correctly stated in terms of $\mu$ SR：$\mu$ wrong／omitted：B1 both，but $\bar{X}$ ：B0 <br> Standardise with $\sqrt{ } n$ ，allow + ，biased $\sigma, \sqrt{ }$ errors $z=-1.80 \pm 0.01$ ，don＇t allow＋ <br> Compare $\pm z$ with $\pm 1.645$ ，signs consistent |
|  |  | $\Phi(-1.8)=1-0.9641<0.05$ | B1 | Explicitly compare $\Phi(z)$ with 0.05 ，correct tail |
|  |  | $\begin{aligned} & \text { CV } 1.8-k \cdot \sigma / \sqrt{ } 50 \\ & k=1.645, \mathrm{CV}=1.727 \\ & 1.72<1.727 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \sqrt{ } \\ & \text { B1 } \sqrt{ } \end{aligned}$ | Correct expression for CV，－or $\pm, k$ from $\Phi^{-1}$ $C V=1.727$ ，$\sqrt{ }$ on their $k$ ，ignore upper limit $k=1.645$ and compare CV with 1.72 |
|  | $\text { Reject } \mathrm{H}_{0}$ <br> Significant evidence that mean height is not 1.8 |  | M1 <br> A1 $\sqrt{ } 7$ | Reject $\mathrm{H}_{0} \sqrt{ }$ ，correct method，needs $\sqrt{ } 50, \mu=1.8$ ； allow cc，$\sqrt{ }$ or $k$ error or biased $\sigma$ estimate Conclusion stated in context ［SR：1．8， 1.72 interchanged：B0B0M1A0B1M0］ |
| 5 | （i） | $\begin{aligned} & { }^{30} \mathrm{C}_{10}(0.4)^{10}(0.6)^{20} \text { or } 0.2915-0.1763 \\ & =0.1152 \end{aligned}$ | $\begin{array}{ll} \text { M1 } \\ \text { A1 } \end{array}$ | Correct formula or use of tables Answer，a．r．t． 0.115 |
|  |  | $\begin{aligned} & 30 p>5 \text { so } p>\frac{1}{6} \\ & 30 q>5 \text { so } q>\frac{1}{6} \\ & \frac{1}{6}<p<\frac{5}{6} \end{aligned}$ | $\begin{array}{ll} \text { M1 } & \\ \text { M1 } & \\ \text { A1 } & 3 \end{array}$ | $30 p$ or $30 p q$ used <br> $30 q$ or both solutions from 30pq used <br> Either $\frac{1}{6}<p<\frac{5}{6}$ or $\left[\frac{1}{2}-\frac{\sqrt{3}}{6}<p<\frac{1}{2}+\frac{\sqrt{3}}{6}\right]$ <br> ［0．211＜p＜0．789］，allow $\leq$ |
|  | （iii） | $\begin{aligned} & \frac{\mathrm{N}(12,7.2)}{\frac{10.5-n p}{\sqrt{n p q}} \text { and } \frac{9.5-n p}{\sqrt{n p q}}} \\ & \Phi(-0.559)-\Phi(-0.9317) \\ & =0.8243-0.7119=0.1124 \end{aligned}$ | B1 <br> B1 <br> M1 <br> A1 $\sqrt{ }$ <br> M1 <br> A1 6 | 12 seen <br> 7.2 or 2.683 seen，allow $7.2^{2}$ <br> Both standardised，allow wrong／no cc，$n p q$ <br> $\sqrt{ } n p q, 10.5$ and 9.5 correct，$\sqrt{ }$ on their $n p, n p q$ <br> Correct use of tails <br> Answer，in range［0．112，0．113］ <br> ［SR：$\frac{1}{\sqrt{2 \pi \times 7.2}} e^{-\frac{1}{2} \frac{(10-12)^{2}}{7.2}}$ M1A1，answer A2］ |




[^0]:    Mark Scheme 4733 June 2005

