

Mark Scheme (Results)

June 2011

GCE Decision D2 (6690) Paper 1



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EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
 - M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
 - A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
 - B marks are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper
- L The second mark is dependent on gaining the first mark



| June 2011 |
|-------------------------------------|
| Decision Mathematics D2 6690 |
| Mark Scheme |

| 1. (a) $ \begin{array}{c c c c c c c c c c c c c c c c c c c $ | Question Number | Scheme | Marks |
|---|--------------------|--|--------------------|
| (b) A C B E F D A $11 \ 8 \ 17 \ 17 \ 31 \ 23 \ = \ 107$ (c) Delete A A f f f f f f f f | 1. (a) | A B C D E F A - 19 11 23 20 37 B 19 - 8 42 17 32 C 11 8 - 34 9 26 D 23 42 34 - 27 31 E 20 17 9 27 - 17 F 37 32 26 31 17 - | B3, 2, 1, 0 (3) |
| (c) Delete A A D D D D D D D D | (b) | $\begin{array}{ccccccc} A & C & B & E & F & D & A \\ 11 & 8 & 17 & 17 & 31 & 23 & = 107 \end{array}$ | M1 A1 A1 (3) |
| $1 \qquad \qquad \text{MIAI} \qquad \qquad \text{MIAI}$ | (c) | Delete A A 19 11 9 9 E 19 9 B 9 E 17 F F 17 F 17 F 17 F 17 F 17 F 17 F 17 17 F 17 17 F 17 | M1 A1 M1 A1 |



| Question Number | Scheme | Marks |
|--|---|-----------------------------|
| (a)1B1 2B1 3B1 (b)M1 1A1 2A1 (c)1M1 1A1 2M1 2A1 | Notes:One double entry correctTwo double entries correctThree double entries correctNN route, each letter appearing once, condone lack of return vertexCAOCAOFinding my RMST – accept 61 for both marksEither 8 + 9 + 17 + 27 or 61 seenAdding on two least arcs, accept 11 and 19 or AC and AB91 CAO | |
| 2. (a) | Adds a column of four zeros and 10. | B1 (1) |
| | Shadow costs3142479ABCD | |
| | 0 1 x -13 -15 -9 -9 2 x x -11 0 -15 3 9 x x 6 -9 4 1 -7 x x | M1 A1 M1 A1 (4) |
| (b) | ABCD1 $20 - \theta$ θ 2 $15 + \theta$ $7 - \theta$ 3 $18 + \theta$ $2 - \theta$ 42810 | M1 A1ft |
| (c) | A B C D 1 18 2 1 2 17 5 1 3 20 10 | DM1 A1 (4) 9 |



| Question | Scheme | Marks |
|-----------|---|--------------------------------|
| NULLE | Notos | |
| (a) | 1B1: cao | |
| (b) | 1M1: Finding all 8 shadow costs 1A1: cao 2M1: Finding missing four improvement indices – no extra zeros 2A1: cao | |
| (c) | 1M1: A valid route, their most negative II chosen, only one empty square used, θ's balance. 1A1ft: consistent; their entering and exiting cells stated clearly 2DM1: An improved solution 7 entries only, (so must now be using one of my negative indices as the entering cell). Must ft from their valid route. 2A1: cao | |
| 3. (a) | P - 7x + z + 4s = 320 | M1 A1 (2) |
| (b) | $\begin{array}{c c c c c c c c c c c c c c c c c c c $ | |
| | $y \frac{1}{2} 1 \frac{3}{4} 0 \frac{1}{4} 0 5$ | |
| | $t = \frac{1}{2}$ 0 1 0 $-\frac{1}{4}$ 1 4 | |
| | P -7 0 1 0 4 0 320 | |
| | hy r y z r s t Value Rowons | |
| | r 0 0 3 1 $-\frac{3}{4}$ 1 14 $R_1 + \frac{1}{2}R_3$ | 2M1 2A1ft |
| | y 0 1 $-\frac{1}{4}$ 0 $\frac{1}{2}$ -1 1 R ₂ $-\frac{1}{2}$ R ₃ | |
| | x 1 0 2 0 $-\frac{1}{2}$ 2 8 $R_3 \div \frac{1}{2}$ | 1M1 2A1 |
| | P 0 0 15 0 $\frac{1}{2}$ 14 376 $R_4 + 7R_3$ | 3A1 |
| | | (5) |
| (c) | P = 376 $x = 8$ $y = 1$ $z = 0$ $r = 14$ $s = 0$ $t = 0$ | M1 A1ft A1 (3) 10 |



| Question Number | Scheme | Marks |
|--------------------|---|-------|
| (a) | <u>Notes:</u> 1M1: One equal sign, P and 320 present 1A1: cao | |
| (b) | 1M1: correct pivot located, attempt to divide row. If choosing negative pivot M0M0 in (b) 1A1: pivot row correct including change of b.v. 2M1: (ft) Correct row operations used at least once or stated correctly. 2A1ft: Looking at non zero-and-one columns, one column ft correct 3A1: cao. | |
| (c) | 1M1: At least 4 values stated. Reading off bottom row, or negative values get M0. 1A1ft: Their four basic variables correct ft from their table. 2A1: cao | |



| 4. S plays 1 S plays 2 S plays 3 L plays 1 -4 -1 1 L plays 2 3 -1 -2 L plays 3 -3 0 2 Row 3 dominates row 1 so row 1 may be deleted. $\boxed{L \ plays 2 \ 3 \ -3 \ 0 \ 2}$ S plays 3 $L \ plays 2 \ 3 \ -3 \ 0 \ 2$ S plays 3 $L \ plays 3 \ -3 \ 0 \ 2$ M1 Let Laura play 2 with probability p and 3 with probability (1- p) If Sam plays 1: Laura's gain is $3p - 3(1-p) = -3 + 6p$ M1 If Sam plays 2: Laura's gain is $-p + 0$ (1- $p) = -p$ A1 (b) 4^{-1} $-\frac{1}{4}$ | (3) |
|---|----------|
| If Sam plays 2: Laura's gain is $-p + 0 (1-p) = -p$ A1 If Sam plays 3: Laura's gain is $-2p + 2 (1-p) = 2 - 4p$ A1 (b) 4 - -4 -4 | (3) |
| (b) 4 4 | |
| B2,1ft,0 | (2) |
| (c) $\begin{array}{c c} -3+6p=-p \\ 7p=3 \\ p=\frac{3}{7} \end{array}$ Laura should play row 1: never, row 2: $\frac{3}{7}$ of the time and row 3: $\frac{4}{7}$ of the time and the value of the game is $-\frac{3}{7}$ to her. A1 | (4) 9 |



| Question | Scheme | Marks |
|----------|--|-------|
| number | Notes: | |
| | <u></u> | |
| (a) | 1M1: Matrix reduced correctly. Could be implicit from equations. | |
| | 2M1: Setting up three probability equations, implicit definition of p. | |
| (b) | 1A1: CAU 1B1ft: Δt least two lines correct accent $n > 1$ or $n < 0$ here. Must both be | |
| (0) | function of p. | |
| | 2B1: 3 lines cao, $0 \le p \le 1$, scale clear (or 1 line = 1), condone lack | |
| | of labels. Rulers used. | |
| (c) | 3M1: Finding their correct optimal point, must have three lines, and | |
| | setting up an equation to find $0 \le p \le 1$. | |
| | 2A1ft: All three options listed must ft from their p. check page 1, no | |
| | negatives. | |
| | 3A1: CAO | |
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| Question | Scheme | Mark | S |
|--------------|--|------------------|-----------|
| 5. (a) | a = 1 $b = 5$ $c = 13$ Flow = 49 | B1, B1 B1, B1 | (4) |
| (b) | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ | M1 A1 | (2) |
| (c) | e.g. SBEHT - 7 together with either SBEHDAFGT – 2 or SBCEHDAFGT - 2 | M1 A1 A2,1,0 | (4) |
| (d) | 58 | B1 | (1) |
| (e) | e.g. C 11 0 7 10 10 7 10 10 10 10 12 10 | M1 A1 | (2) |
| (f) | Max flow = min cut Cut through HT, HG, GF, FT Value 58 | M1 A1 | (2) 15 |



| Notes: 1B1: $a = 1$ cao 2B1: $b = 5$ cao 3B1: $c = 13$ cao 4B1: 49 cao | |
|--|---|
| 1M1: Two numbers on each arc 1A1: cao | |
| 1M1: One valid flow augmenting route found and value stated.1A1: Flow increased by at least 22A1: A second correct flow3A1: Flow increased by 9 and no more | |
| 1B1: cao | |
| 1M1: Consistent flow pattern > 51 1A1: cao | |
| 1M1: Must have attempted (e), S to T, and made an attempt at a cut. 1A1: cut correct – may be drawn. Refer to max flow-min cut theorem three words out of four. | |
| | Notes: BI: a = 1 cao BI: b = 5 cao BI: c = 13 cao HI: Two numbers on each arc A1: cao IM: One valid flow augmenting route found and value stated. A1: Flow increased by at least 2 A1: A second correct flow BA1: Flow increased by 9 and no more IB1: cao IM1: Consistent flow pattern > 51 A1: cao IM1: Must have attempted (e), S to T, and made an attempt at a cut. A1: cut correct – may be drawn. Refer to max flow-min cut theorem hree words out of four. |



| Question Number | Scheme | | | | | Marks | | |
|--------------------|--|---|---------------------------------|--------------------|-----------------------------|-------------------|--|--|
| 6. | | Task A | Task B | Task C | | | | |
| (a) | Worker D | 27 | 21 | 25 | | | | |
| | Worker O | 27 | 30 | 34 | | | | |
| | Worker R | 35 | 29 | 32 | | | | |
| | Let $x_{ij} = \begin{cases} 1 \text{ if worker does the task} \\ 0 \text{ otherwise} \end{cases}$ Where x_{ii} indicates worker i being assigned to task j, $i \in \{P, Q, R\}$, | | | | | | | |
| | $j \in \{A, B, C\}$ | | | | | | | |
| | Minimise $27x_{PA} + 31x_{PB} + 2$ Subject to: $x_{PA} + x_{PB} + x_{PC}$ $x_{QA} + x_{QB} + x_{QC}$ $x_{RA} + x_{RB} + x_{RC}$ $x_{PA} + x_{QA} + x_{RA}$ $x_{PB} + x_{QB} + x_{RE}$ $x_{PC} + x_{QC} + x_{RC}$ | $25x_{PC} + 26x_{QA}$ $c = 1$ $c = 1$ $c = 1$ $a = 1$ $b = 1$ $c = 1$ | + 30 <i>x</i> _{QB} + 3 | $34x_{QC} + 35x_R$ | $x_A + 29x_{RB} + 32x_{RC}$ | B1 B1 M1 A1 A1 | | |
| | ~ | | | | | (7) | | |
| (b) | Since we need to | o maximise fir | st subtract | all entries fr | om some $n \ge 41$ | M1 | | |
| | | Task A | Task B | Task C | <u>'</u> | | | |
| | Worker P | 8 | 4 | 10 | | | | |
| | Worker Q Worker R | 9 | 5 | | | AI (2) | | |
| | WOIKU K | | 0 | |] | (2) 9 | | |



| Question | | Sc | heme | | Marks | |
|-----------|---|--|---|---|--|--|
| Number | Notes: | | | | | |
| (a) | 1B1: defining varia 2B1: defining varia 3B1: minimise 4B1: cao 1M1: At least 3 equ should be precisely 1A1: cao 3 equatio 2A1: cao 6 equatio | | | | | |
| (b) | 1M1: subtracting fi 1A1: correct | from some $n \ge 4$ | l condone | up to two errors | | |
| 7. (a) | Stage State 0 H 1 F 1 F 2 C 2 C 0 D 2 C 3 A B - 4 London Optimal expected i | ActionH- LondonI - LondonFHFIGHGICFCGDFDGEFEGACADAEBCBDBELondon - ALondon - Bncome is £10 60 | Dest. London H I H I F G F G F G F G F G C D E E C D E E C D E E A B D O | Value $36 - 5 = 31^*$ $38 - 4 = 34^*$ $29 - 6 + 31 = 54$ $29 - 7 + 34 = 56^*$ $27 - 5 + 31 = 53$ $27 - 6 + 34 = 55^*$ $42 - 6 + 56 = 92^*$ $42 - 5 + 55 = 92^*$ $41 - 6 + 56 = 91$ $41 - 3 + 55 = 93^*$ $39 - 4 + 56 = 91^*$ $39 - 4 + 55 = 90$ $22 - 5 + 92 = 109$ $22 - 5 + 92 = 109$ $22 - 4 + 93 = 111^*$ $17 - 4 + 92 = 105$ $17 - 4 + 93 = 106^*$ $17 - 3 + 91 = 105$ $-5 + 111 = 106^*$ $-3 + 106 = 103$ | 1M1 1A1 (2) 2M1 2A1 3A1 (3) 3M1 4A1ft 5A1ft (3) 4M1 6A1ft 7A1ft | |
| (b) | Optimal schedules London – A – D – London – A – E – | are: G – I – Londor F – I – Londor | n (or v.v.) n (or v.v) | | (3) B1ft B1 (2) 13 | |



| Question Number | Scheme | Marks |
|--------------------|---|-------|
| | <u>Notes:</u> Throughout section (a): Condone lack of destination column and/or reversed stage numbers throughout. Only penalise incorrect result in Value – ie ignore working values. Penalise absence of state or action column with first two A marks earned only Penalise empty/errors in stage column with first A mark earned only. | |
| (a) | 1M1: First stage completed. 1A1: CAO Penalise * errors only once in the question on the first occurrence 2M1: Second stage completed. Penalise reversed states here and at end. Bod if something in each cell. 2A1: Any 2 states correct. (Penalise * errors only once in the question). 3A1: All 3 states correct. (Penalise * errors only once in the question). 3M1: 3rd stage completed. Bod if something in each cell. 4A1ft: A or B state correct. (Penalise * errors only once in the question). 5A1ft: A and B states correct. (Penalise * errors only once in the question). 4M1: 4th stage completed. Bod if something in each cell. 6A1ft: Final, state correct. (Penalise * errors only once in the question). | |
| (b) | 1B1ft: 1 route correct, consistent with their working penalise reversed states again here. Condone absence of London 2B1: both routes cao. London to London. | |

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